

# TEMPERATURE, VISCOSITY, AND CHARGE DENSITY EFFECTS ON THE VELOCITY PROFILE OF A NANOCCHANNEL ELECTRO-OSMOTIC FLOW

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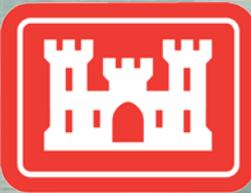
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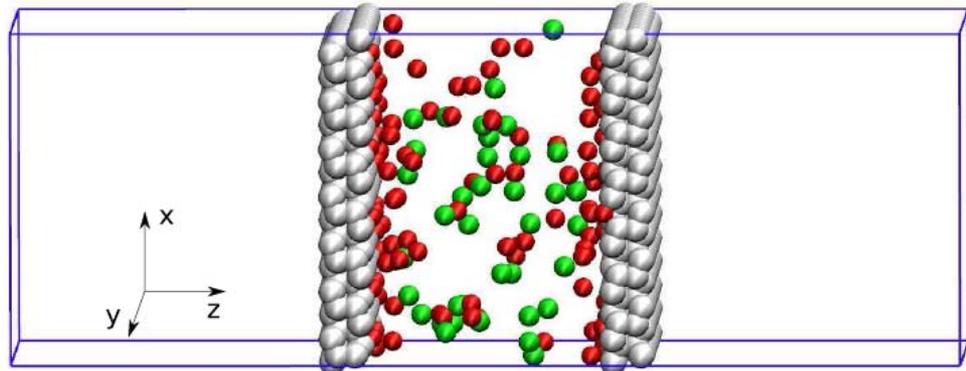
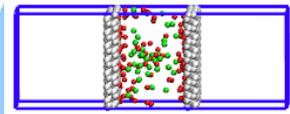
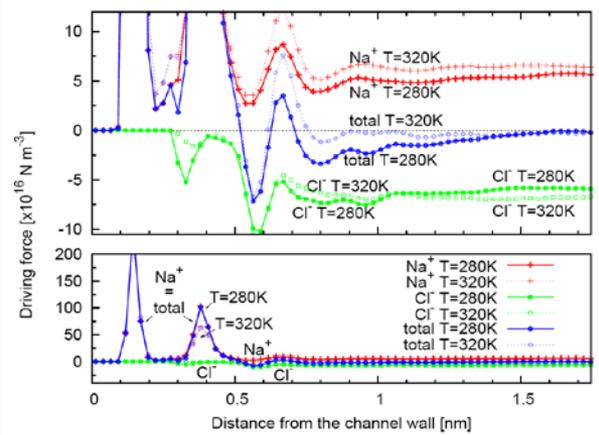
Senior Research Scientists  
GSL, U.S. Army ERDC Vicksburg, MS



MISSISSIPPI STATE  
UNIVERSITY  
**CAVS**

US Army Corps of Engineers  
**BUILDING STRONG**

$$\vec{F}_d(z) = e[c_{Na^+}(z) - c_{Cl^-}(z)]\vec{E}_{ext}$$



# Electrokinetic process - definitions

**Electrokinetic phenomena:** electric field related effects occurring in heterogeneous fluids in porous materials

**Electroosmosis:** motion of fluid under the influence of electric field

**Electrophoresis:** motion of particles under the influence of electric field

**Streaming potential:** electric potential generated by moving fluid

Cause: **Double layer** of charges on solid-liquid interface

**Applications:** dewatering of concrete structures, decontamination, nanoscale devices, even source of electric energy?



# Atomic system configuration

**Na<sup>+</sup>** and **Cl<sup>-</sup>** ions solvated in **water**,

confined between two negatively charged Si walls

Applied **electric field** parallel to the walls

Measured **velocity profiles** and **ionic concentrations**

Final goal: obtain effective diffusion coefficients and ionic mobilities to supplement continuum level model

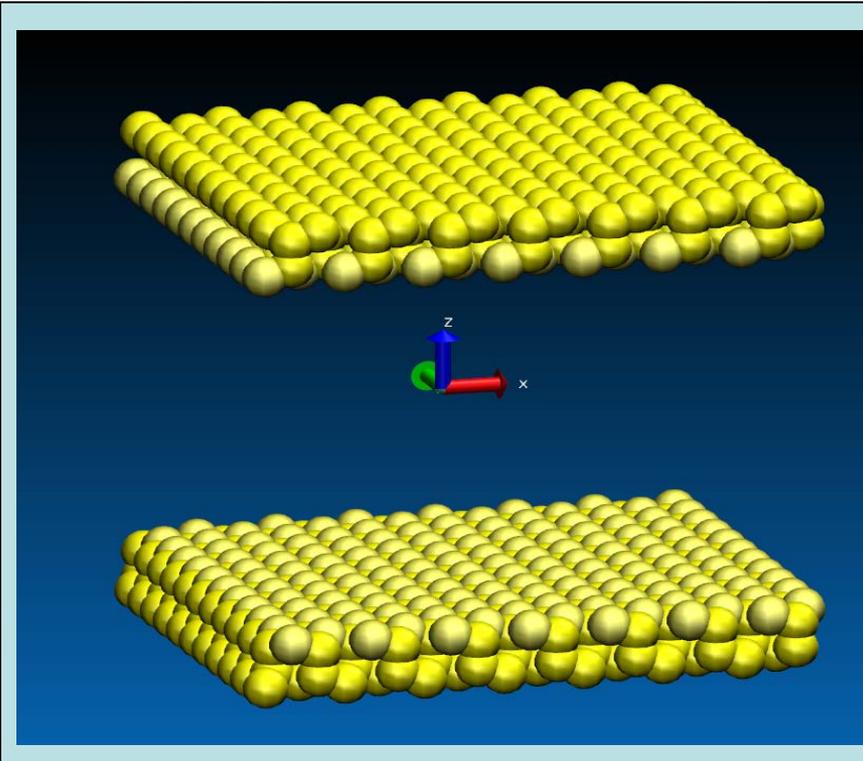
## References:

R. Qiao and N. R. Aluru: Charge Inversion and Flow Reversal in a Nanochannel Electro-osmotic Flow, PRL 92 (19) 2004

R. Qiao and N. R. Aluru: Multiscale Simulation of Electroosmotic Transport Using Embedding Techniques, International Journal for Multiscale Computational Engineering 2 (2) 2004



# Construction of simulation cell



Channel walls of silicon crystal surface in (111) direction

Dimensions 4.66x4.22x3.49 nm

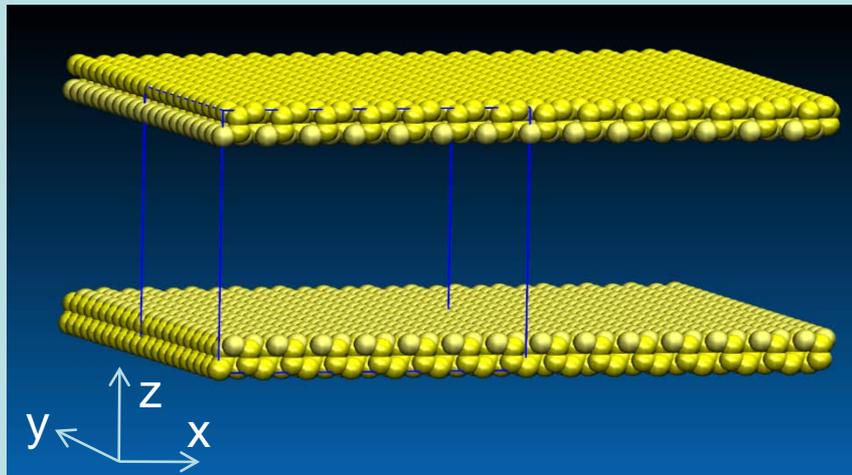
Uniform negative charge on inner surface layers

Walls: 924 uncharged Si atoms

308 neg. charged Si atoms

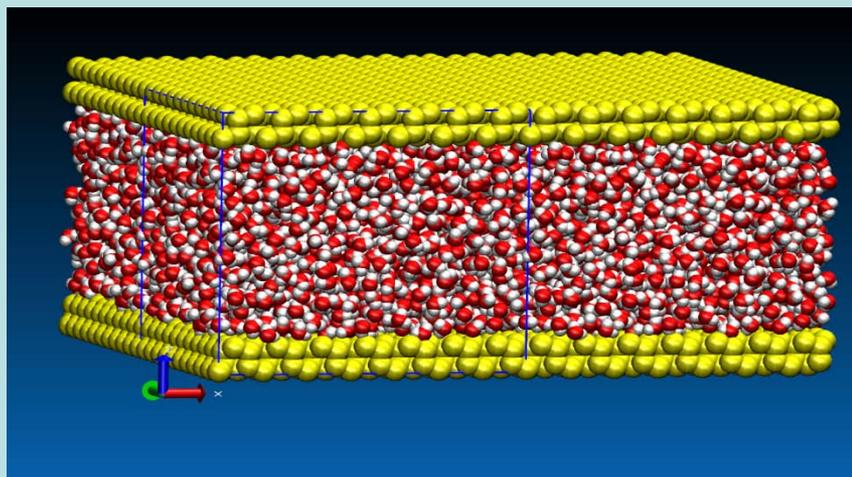


# Construction of simulation cell



Periodic boundary conditions in x and y directions => slab with infinite surface area

Studied variation along z direction

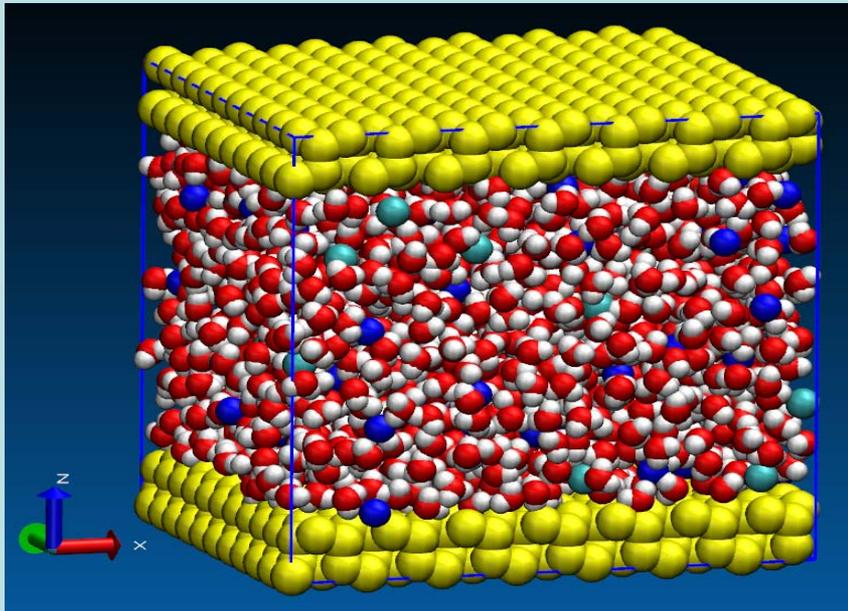


Solvation:

Randomly inserted 2290 water molecules

Avoided overlap, even across PBC boundaries

# Construction of simulation cell



Insertion of ions:

Replaced random water molecules with  $\text{Na}^+$  and  $\text{Cl}^-$  ions

Ionic solution:

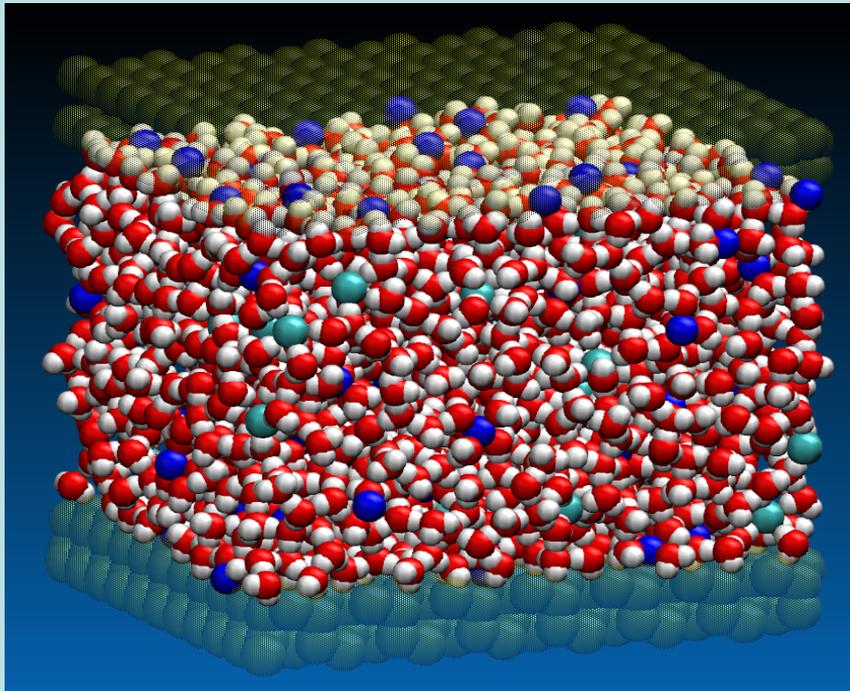
2144 water molecules

108  $\text{Na}^+$  ions

38  $\text{Cl}^-$  ions



# Energy minimization



Molecules reorient and settle to local minimum of energy position

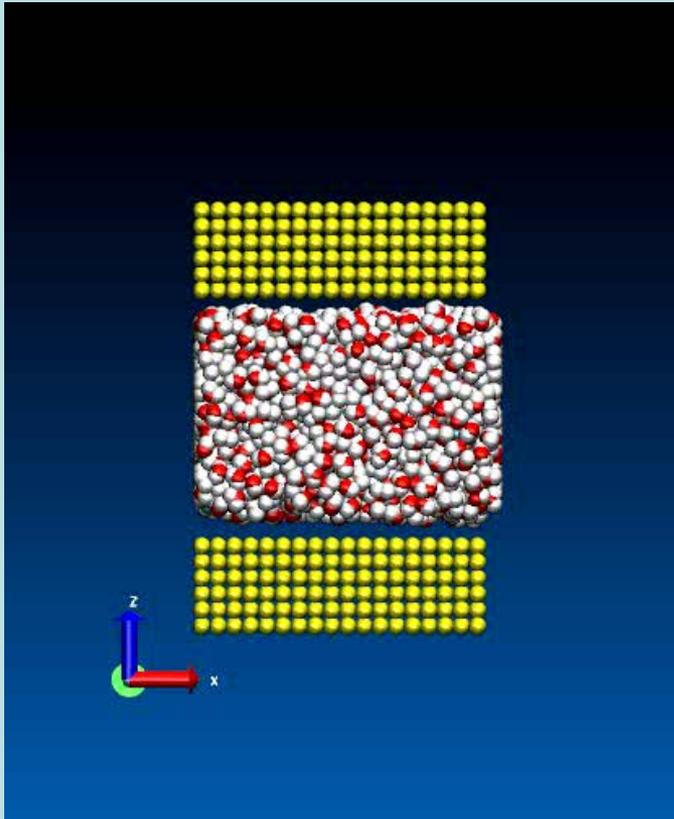
H from  $\text{H}_2\text{O}$  molecules points to the negative surface

$\text{Na}^+$  ions move slightly closer to the negatively charged surface

$\text{Cl}^-$  ions move slightly away from the negatively charged surface



# Pressure adjustment



Bottom wall is fixed

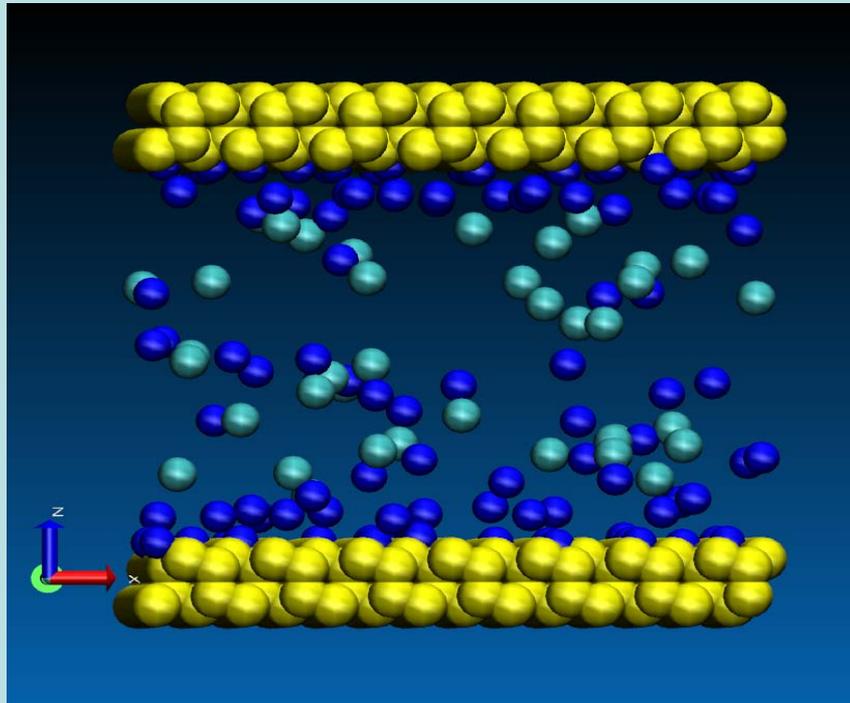
External force is applied on the top wall atoms in the downward direction

Magnitude of the external force is calculated so that the total force on each atom corresponds to the desired pressure

External force is balanced by the fluid pressure



# Equilibration of atomic system



Equilibration:

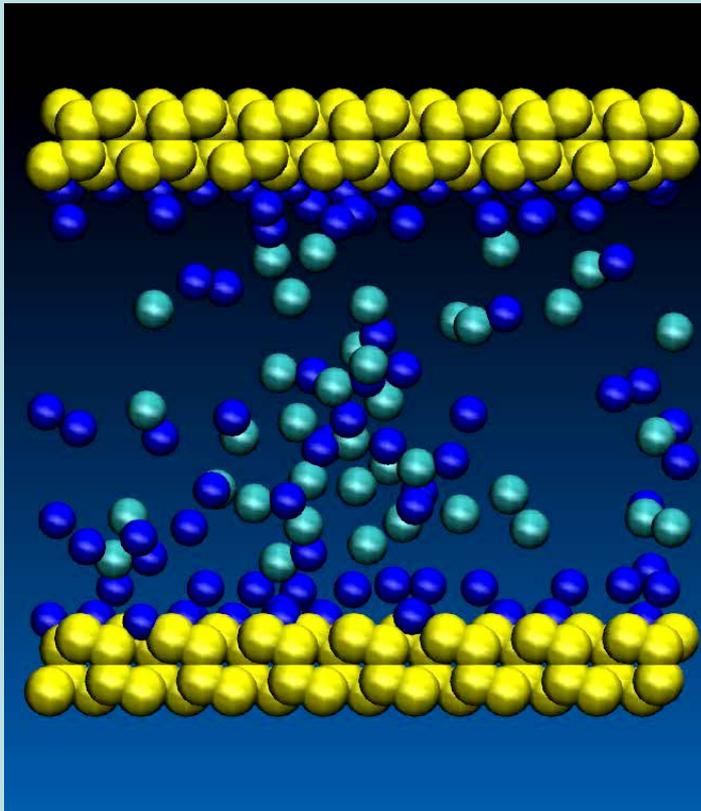
MD simulation,  $t = 2$  ns  
without ext. electric field

$T = 300$  K

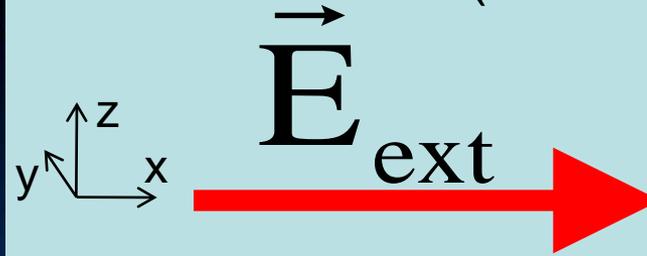
Result:

ionic concentration profile  
is formed along the z  
direction

# Simulation with applied electric field



Electric field applied in the +x  
direction (to the right)



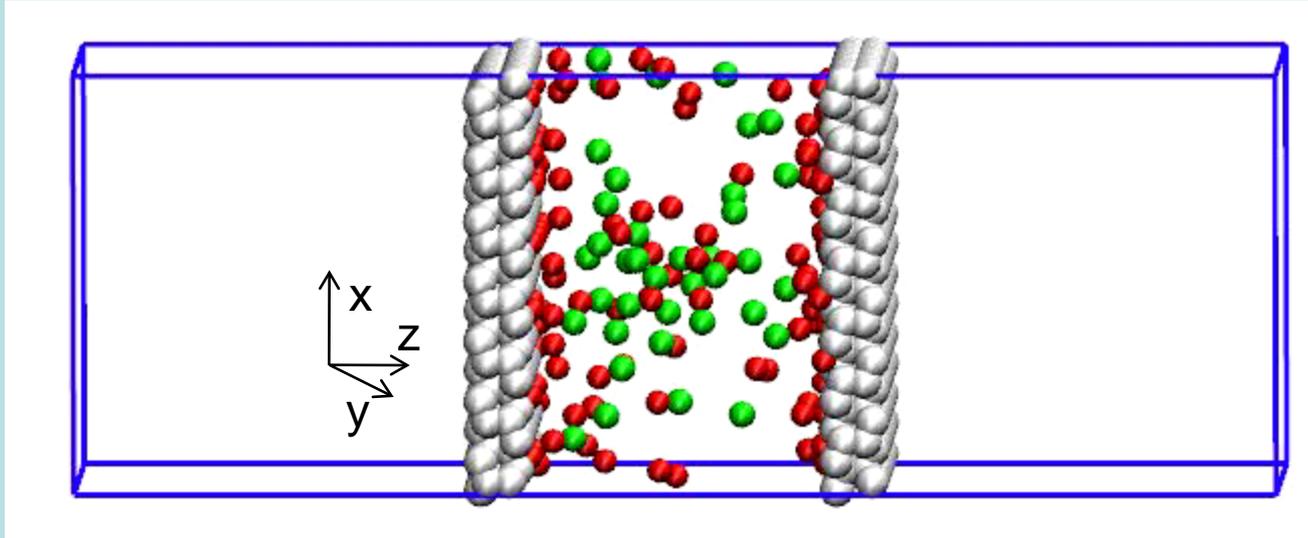
Na<sup>+</sup> ions (dark blue):

move in the direction of  $\vec{E}_{\text{ext}}$   
or adsorb at the negatively  
charged surface

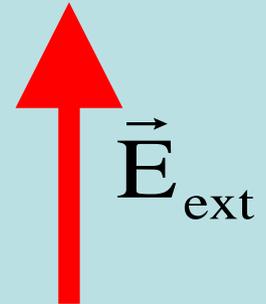
Cl<sup>-</sup> ions (light blue):

move opposite to  $\vec{E}_{\text{ext}}$

# Simulation with applied electric field



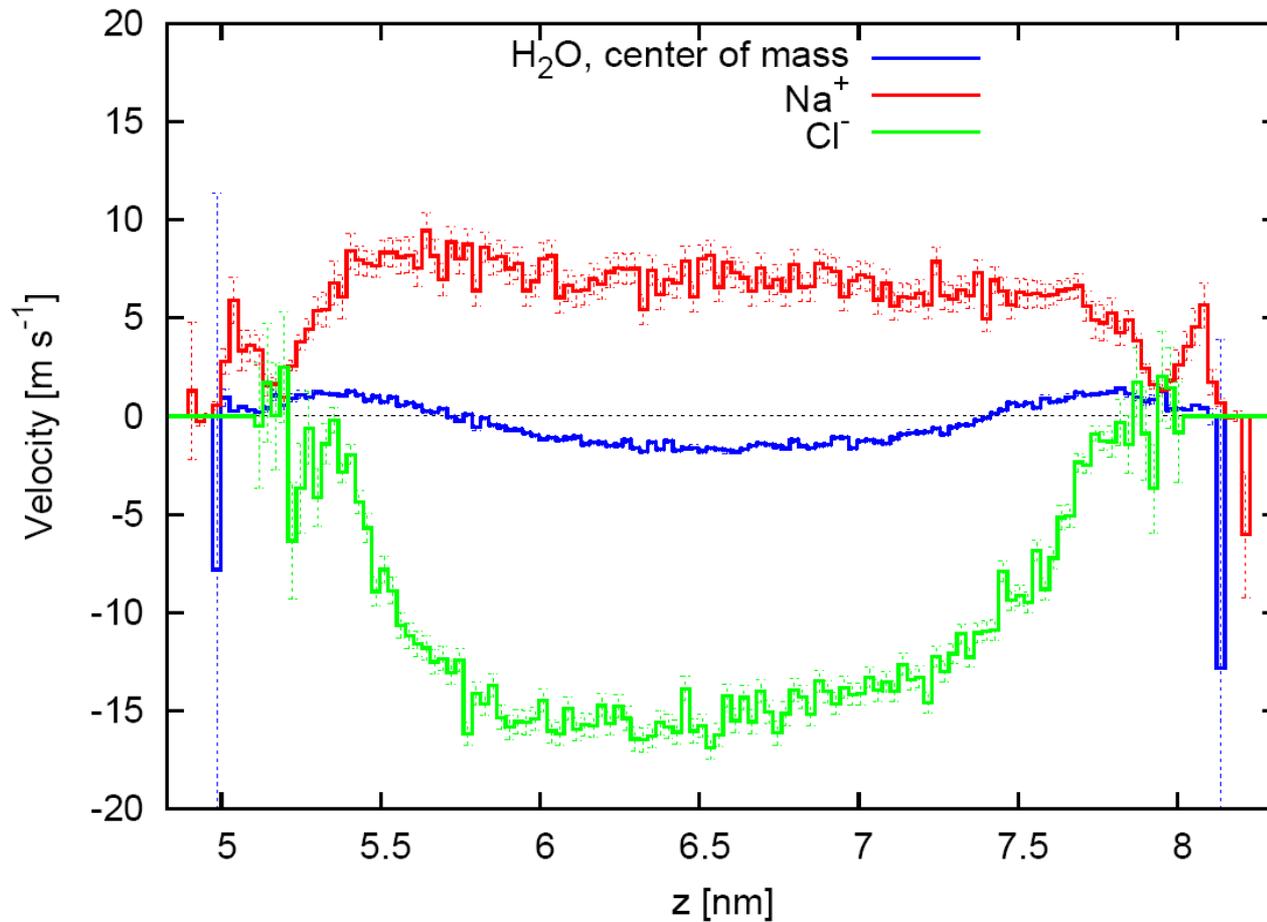
Electric field



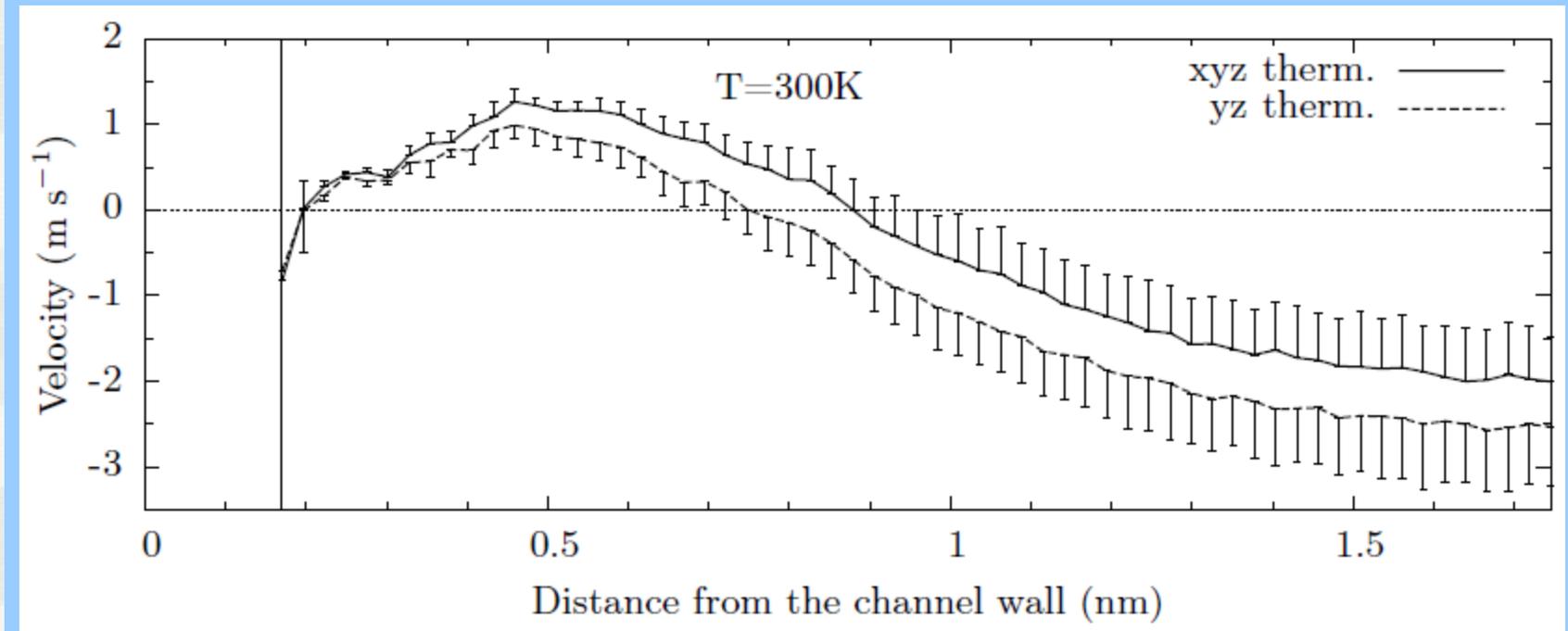
**Na<sup>+</sup>** adsorb at the negatively charged surface  
or move in the direction of  $\vec{E}_{\text{ext}}$

**Cl<sup>-</sup>** move opposite to  $\vec{E}_{\text{ext}}$

# Velocity profiles



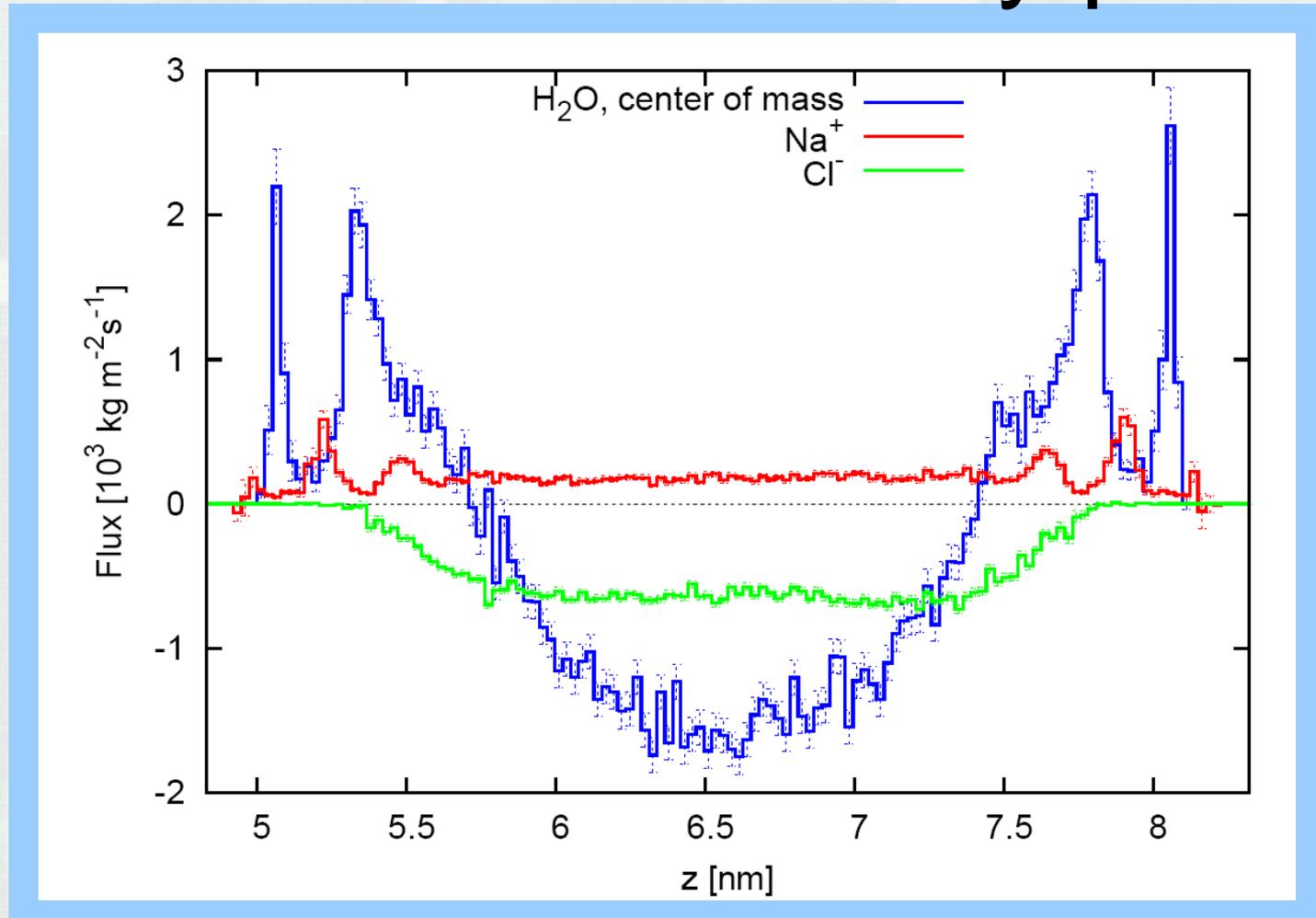
# Selective thermostat



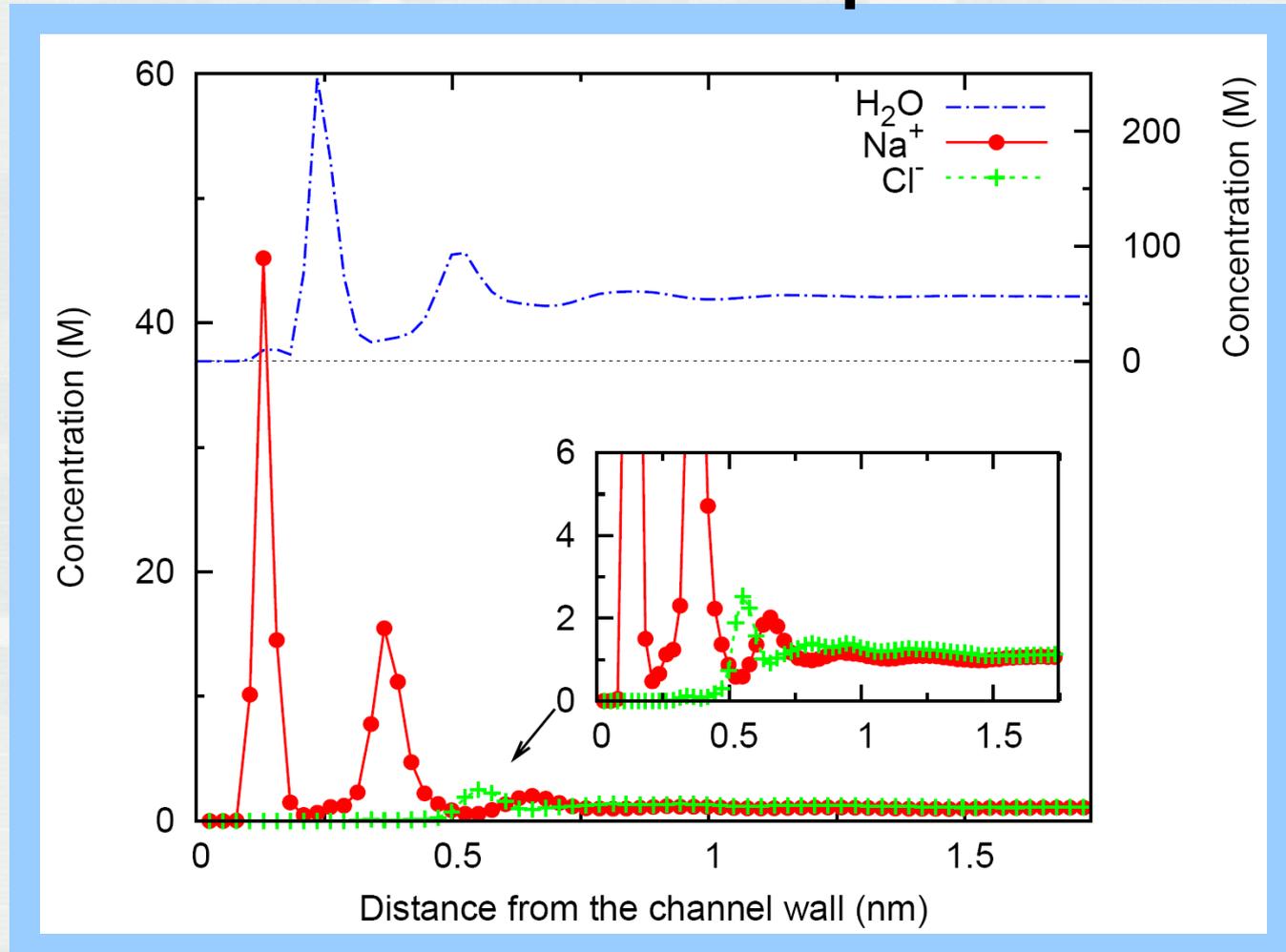
Thermostating of velocity component in the field direction (x) slightly influences velocity profile – we chose to apply selective (yz) thermostat



# Mass flux areal density profiles

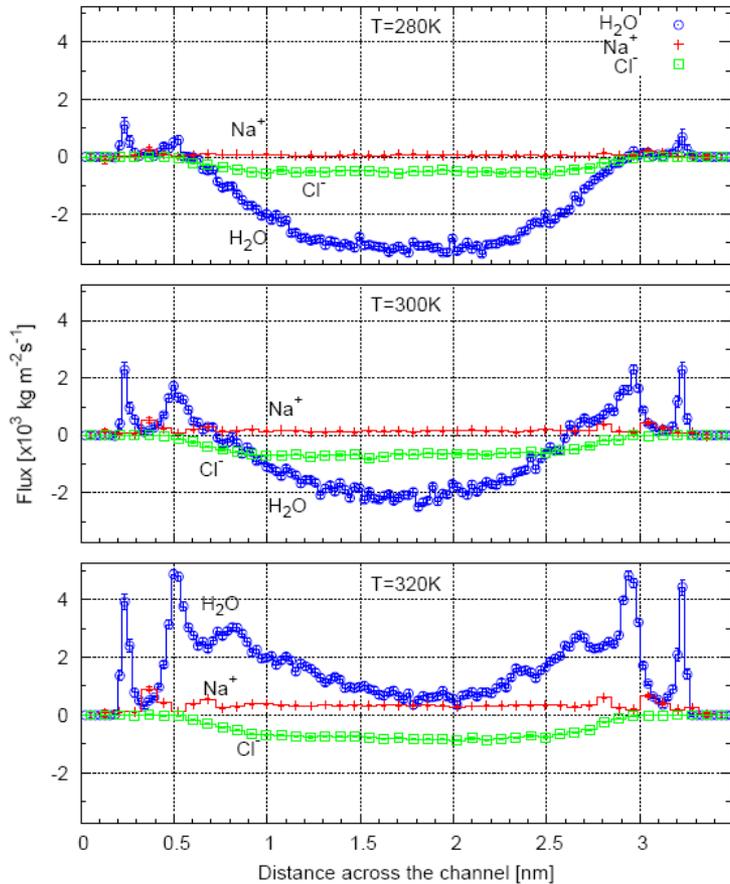


# Concentration profiles

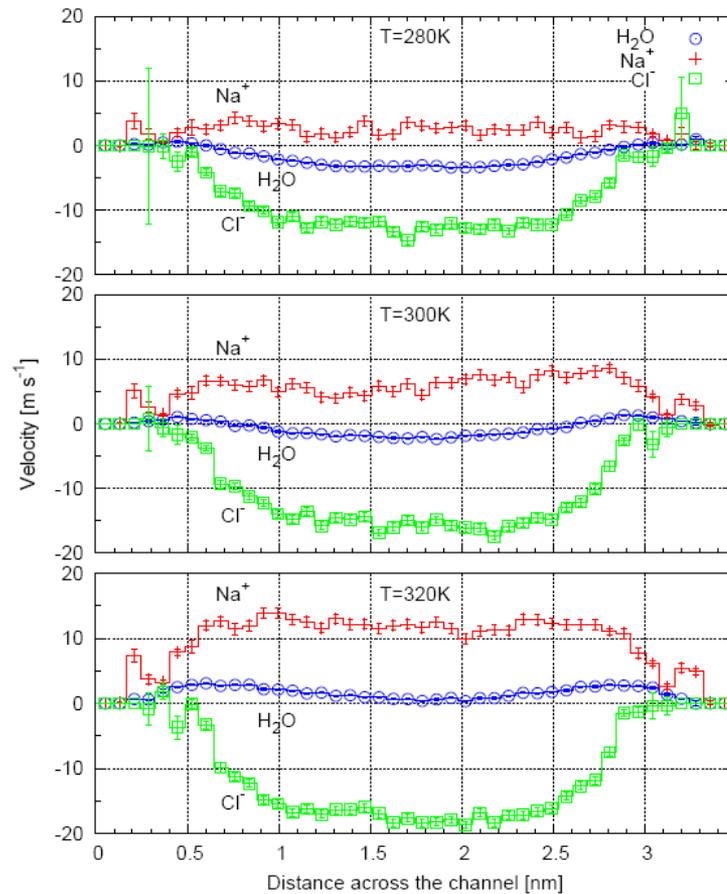


# Temperature dependence

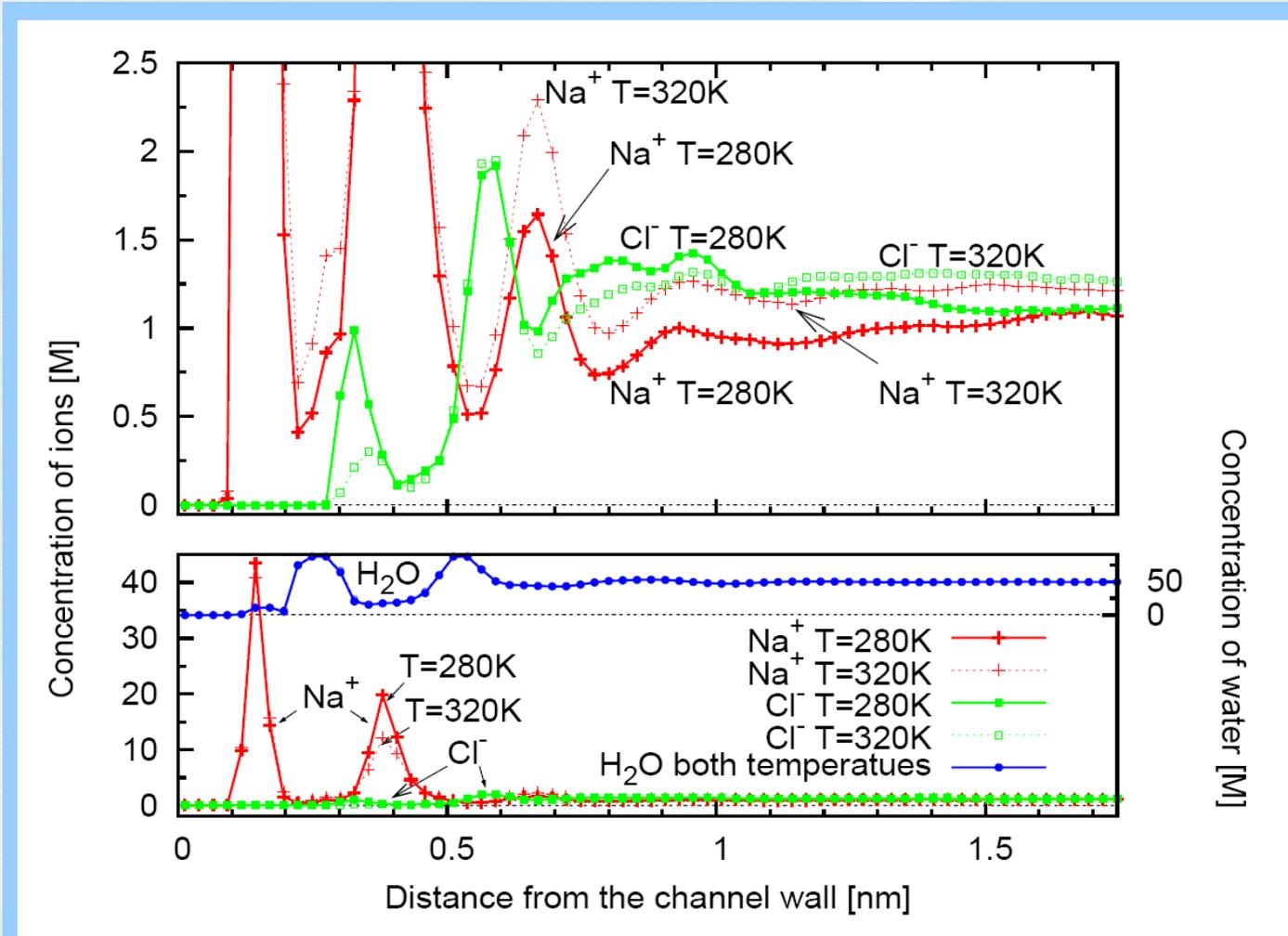
*Flux*



*Velocity*

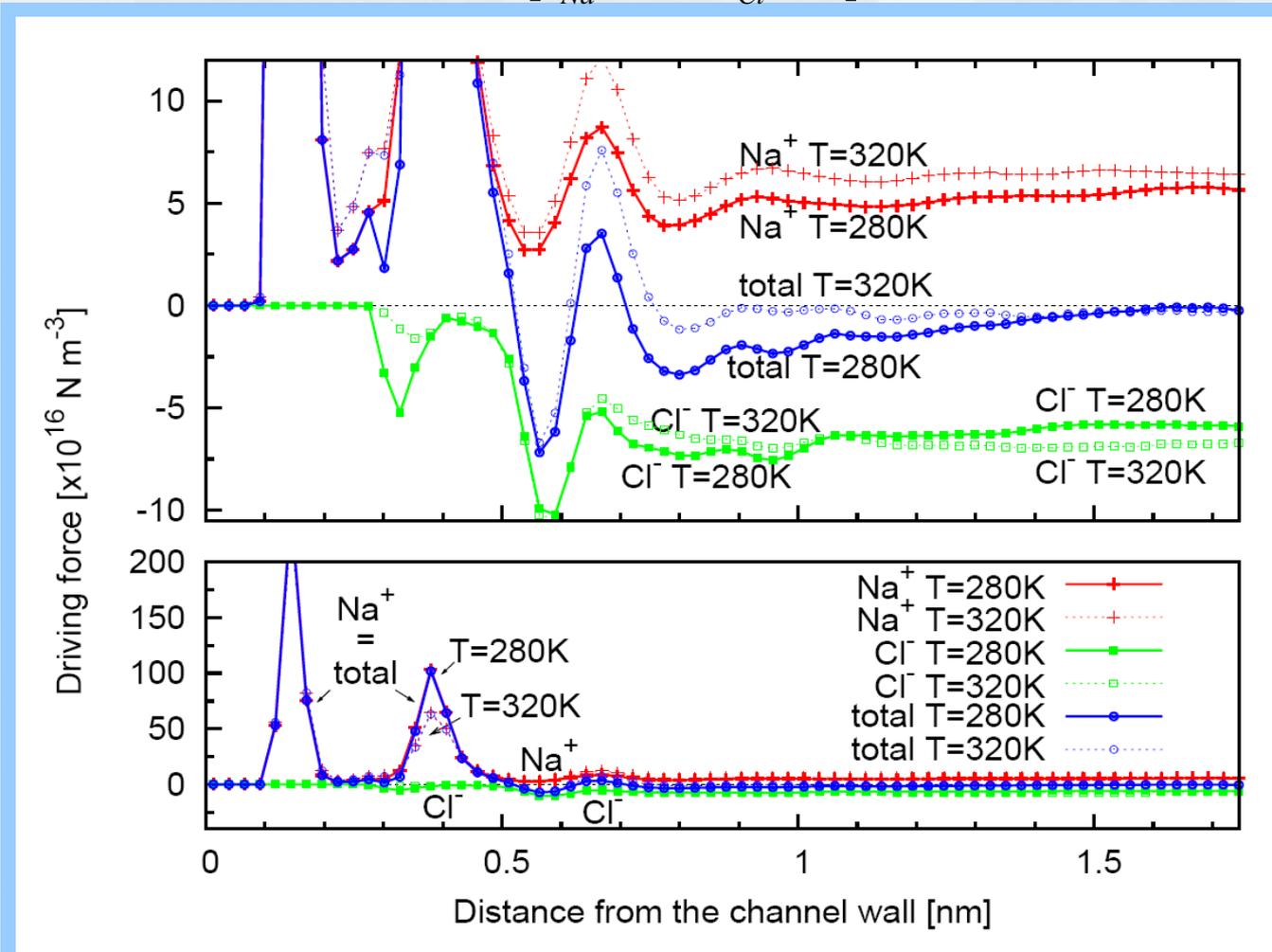


# Temperature effects on concentrations

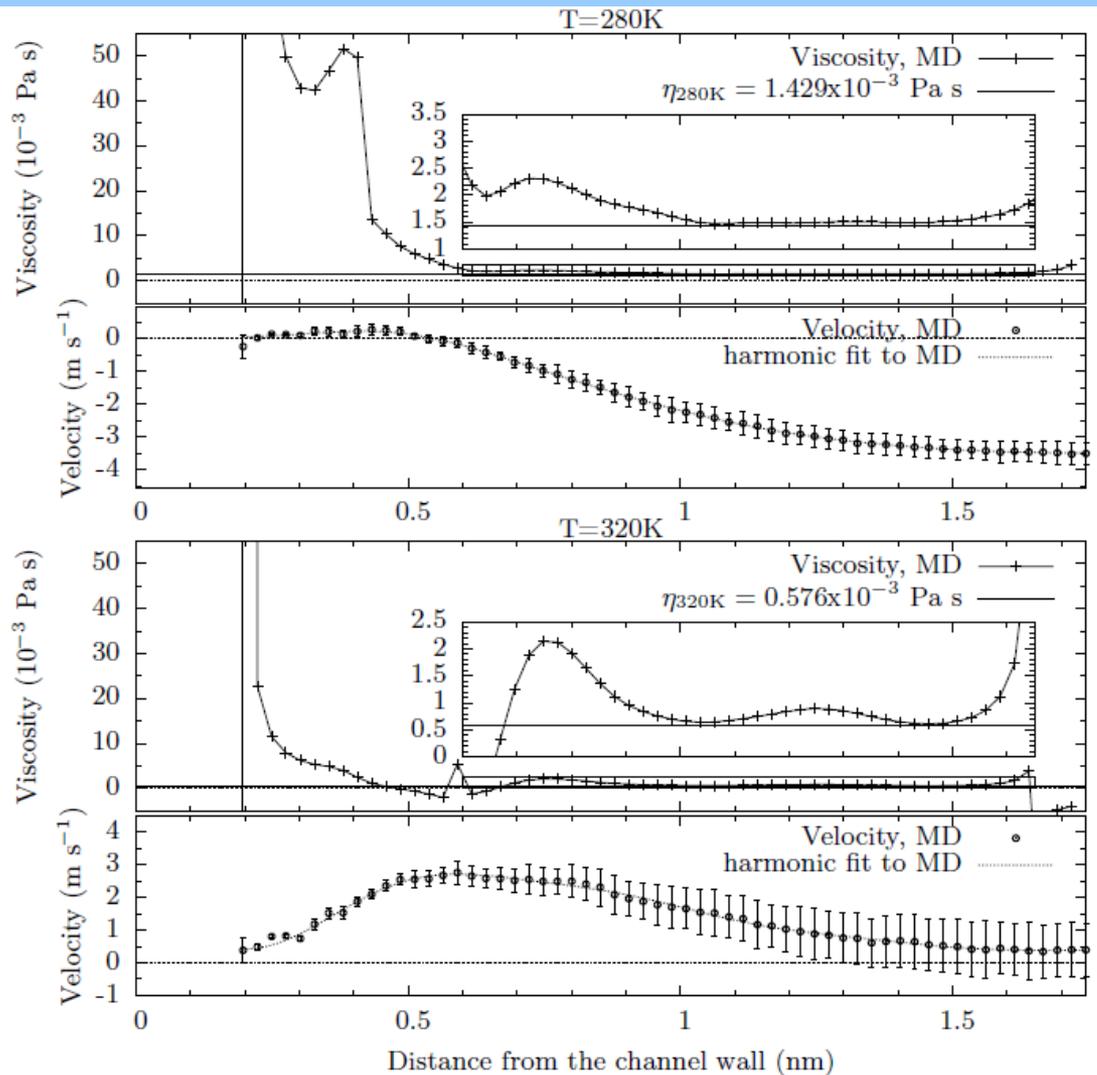


# Temperature effects on driving force

$$\vec{F}_d(z) = e[c_{Na^+}(z) - c_{Cl^-}(z)]\vec{E}_{ext}$$



# Viscosity



Stokes equation:

$$\frac{d}{dz} \left[ \eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

Integrated:

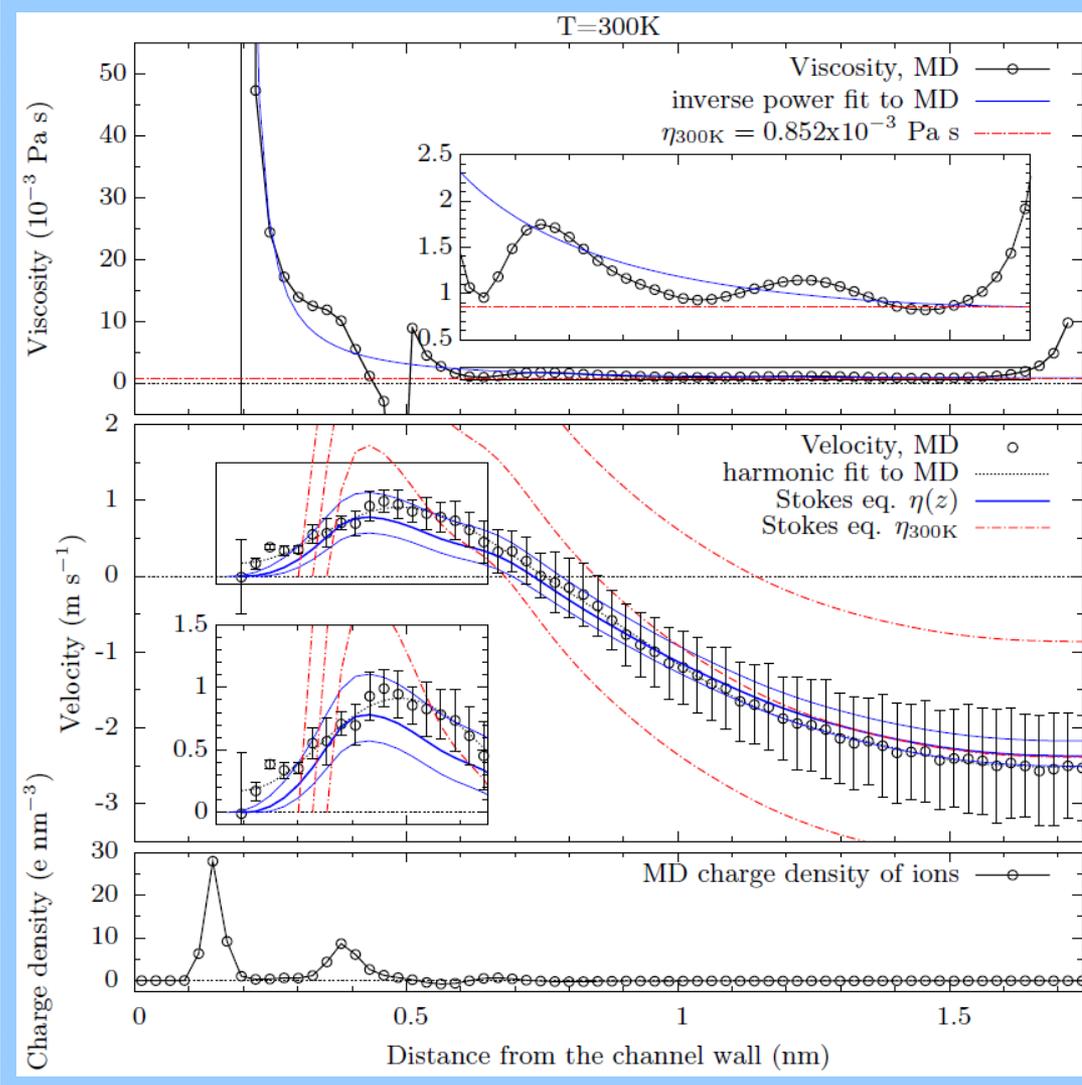
$$\eta(z) \left. \frac{du_x(z)}{dz} \right|_{z=z_0} = \frac{-\int_0^{z_0} F_d(z) dz}{\left. \frac{du_x(z)}{dz} \right|_{z=z_0}}$$

Velocity approximation:

$$u_{x fit}(z) = \sum_{n=0}^7 a_n \cos \left( n\pi \frac{z}{h} \right)$$



# Velocity predicted from charge density



Stokes equation:

$$\frac{d}{dz} \left[ \eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

Black:  
Molecular Dynamics

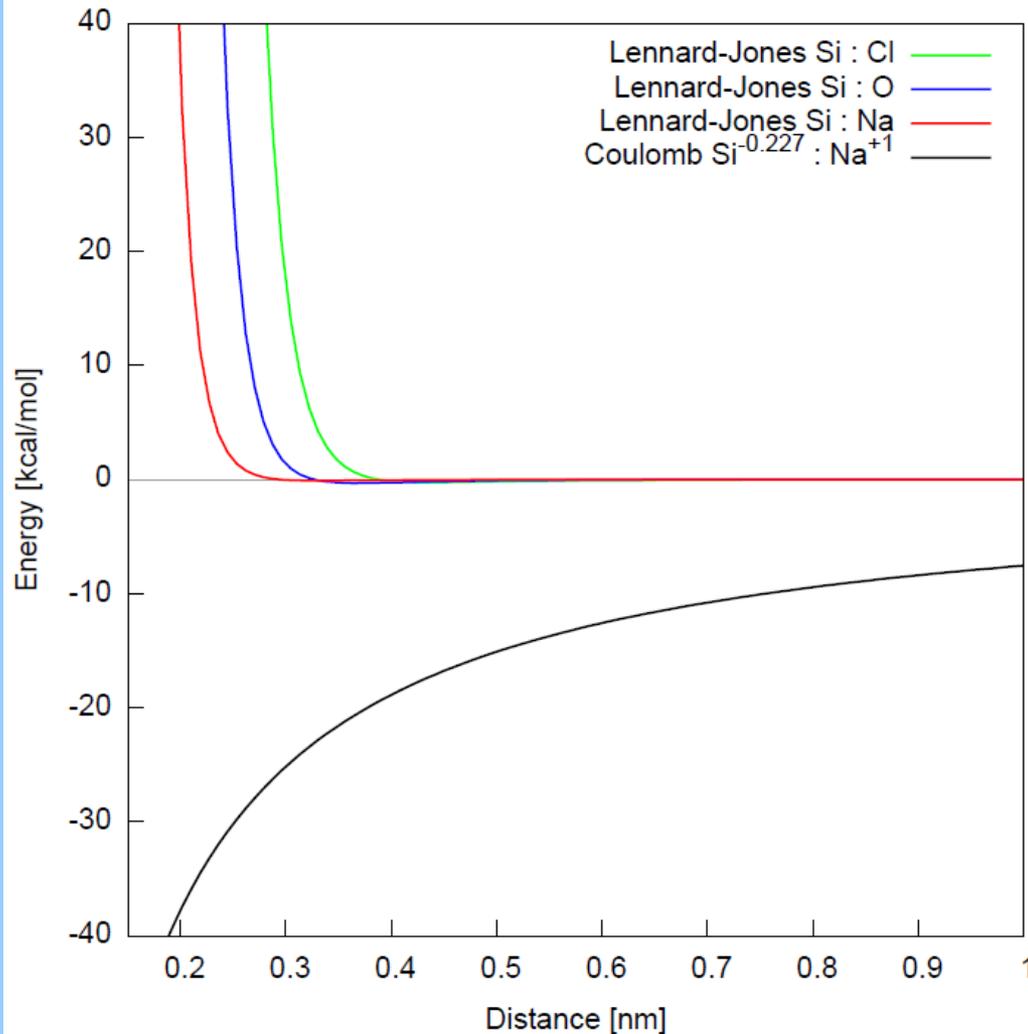
Red:  
constant viscosity

Blue:  
inverse power viscosity

$$\eta(z) = \left[ 1 - \left( \frac{z}{h} \right)^2 \right]^{-p} \eta_{\text{exp}}$$



# Lennard-Jones and Coulomb interaction



RGB

Lennard-Jones

$$V_{LJ}(r) = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right]$$

i-j	O-O	O-Si	O-Na	O-Cl	Si-Si	Si-Na	Si-Cl	Na-Na	Na-Cl	Cl-Cl
$\sigma_{ij}$	3.17	3.27	2.86	3.75	3.39	2.95	3.88	2.58	3.38	4.45
$\epsilon_{ij}$	155	301	47.9	129	584	92.9	249	14.8	39.6	106

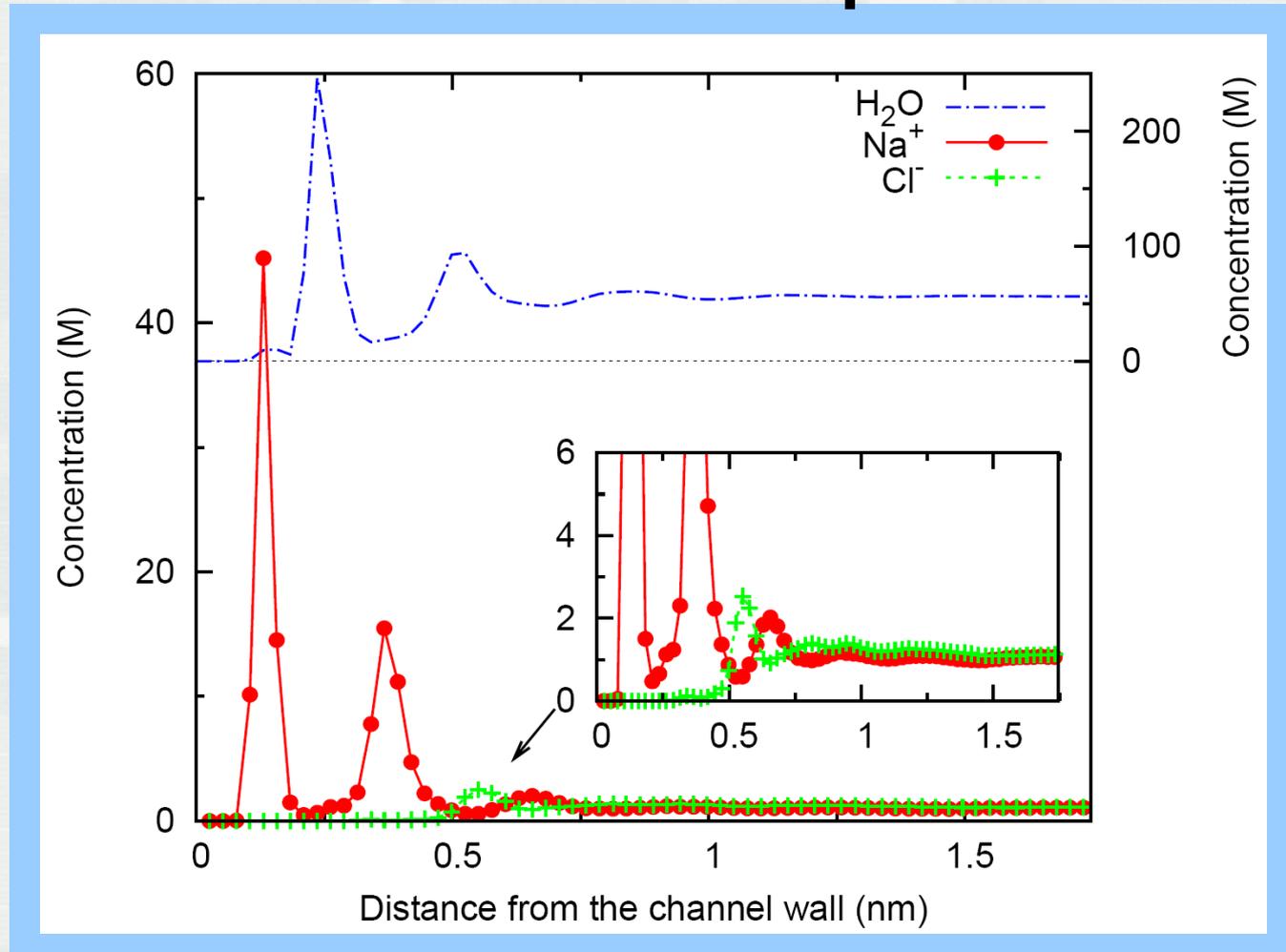
Black

Electrostatic (Coulomb)

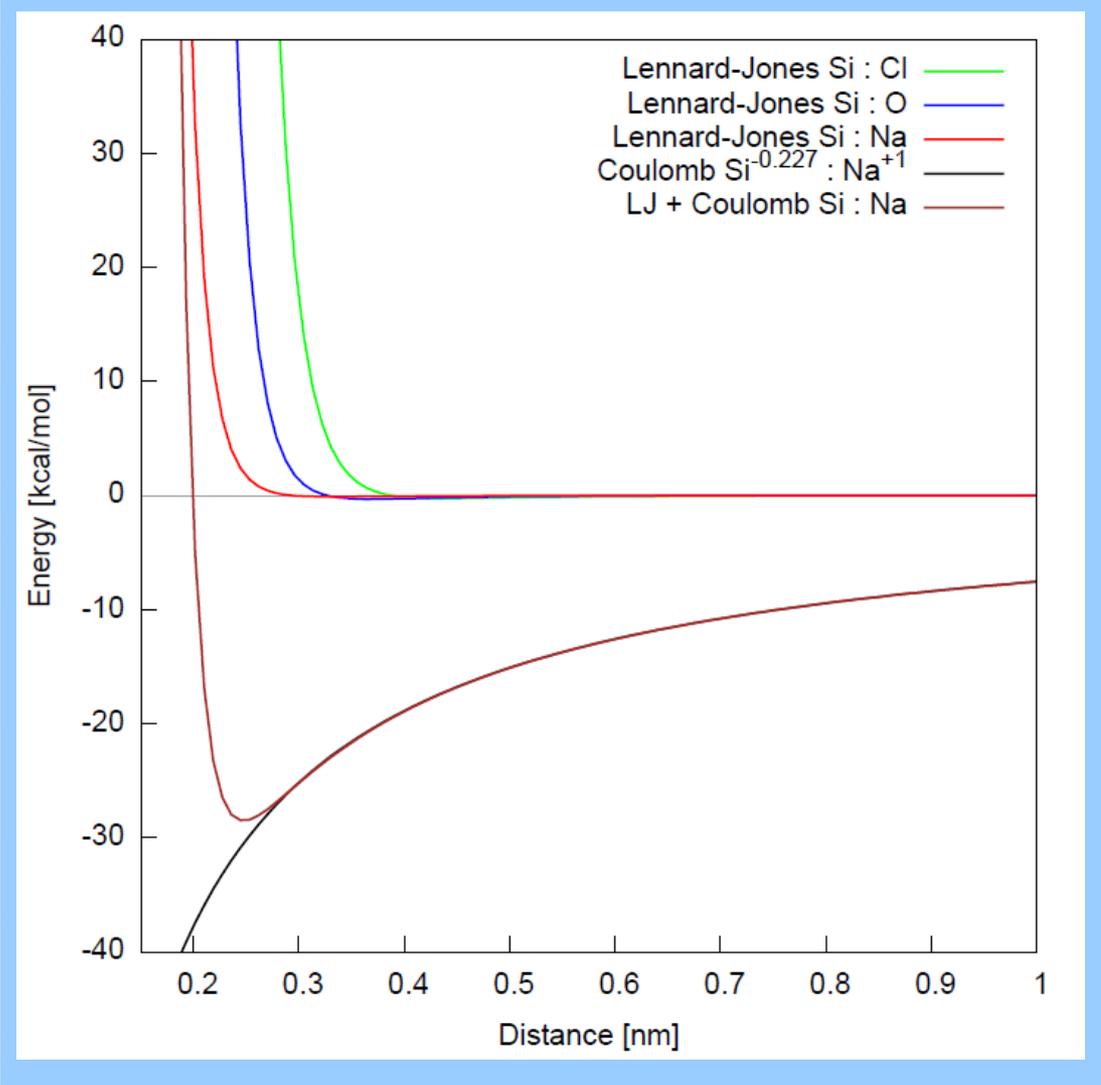
$$V_C(r) = \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r}$$



# Concentration profiles



# Lennard-Jones and Coulomb interaction



RGB

Lennard-Jones

$$V_{LJ}(r) = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right]$$

i-j	O-O	O-Si	O-Na	O-Cl	Si-Si	Si-Na	Si-Cl	Na-Na	Na-Cl	Cl-Cl
$\sigma_{ij}$	3.17	3.27	2.86	3.75	3.39	2.95	3.88	2.58	3.38	4.45
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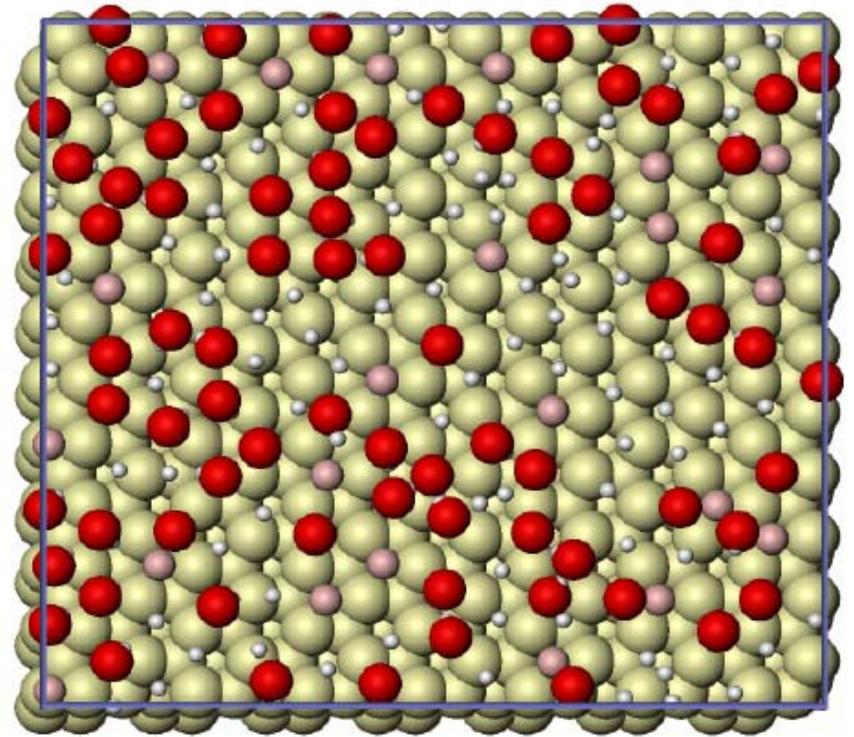
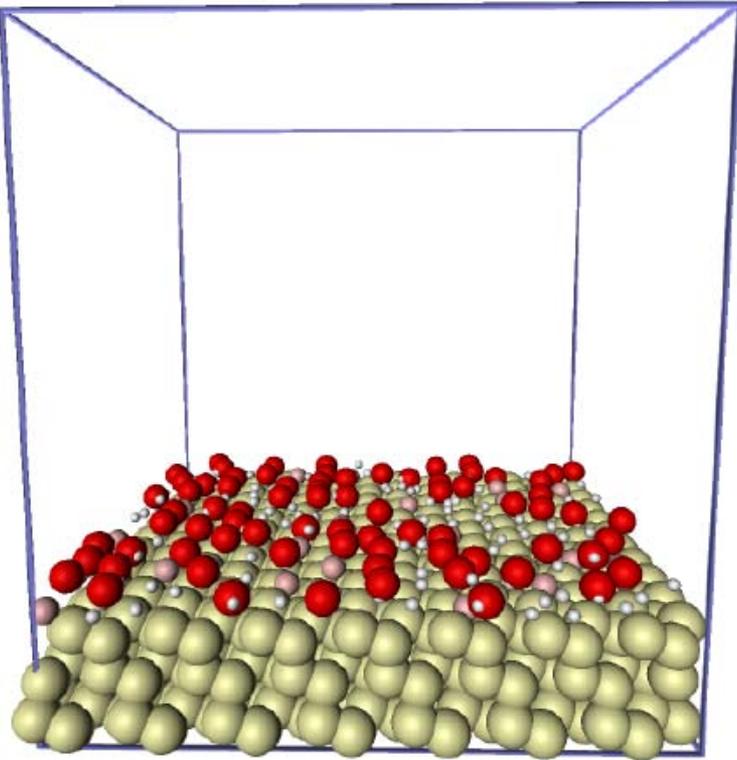
Black

Electrostatic (Coulomb)

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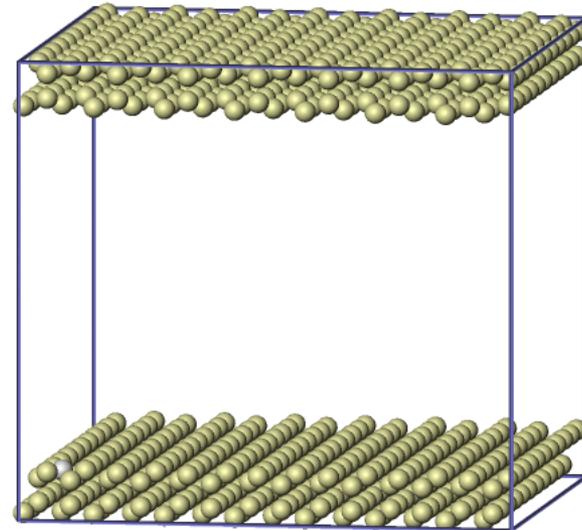
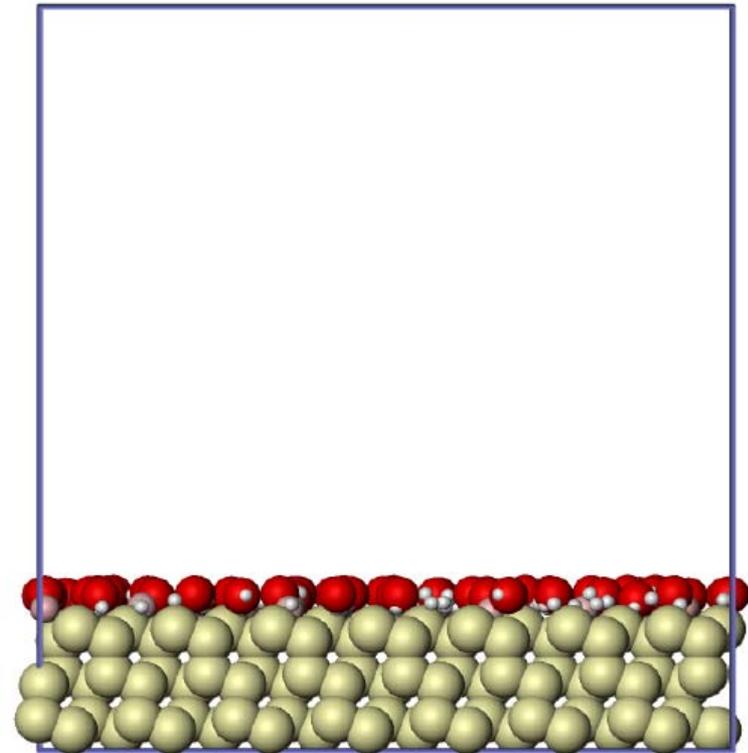


# Adsorption sites



The nearest-to-wall peak of high  $\text{Na}^+$  concentration corresponds to the favorable adsorption sites on the silicon surface

# Potential energy profile

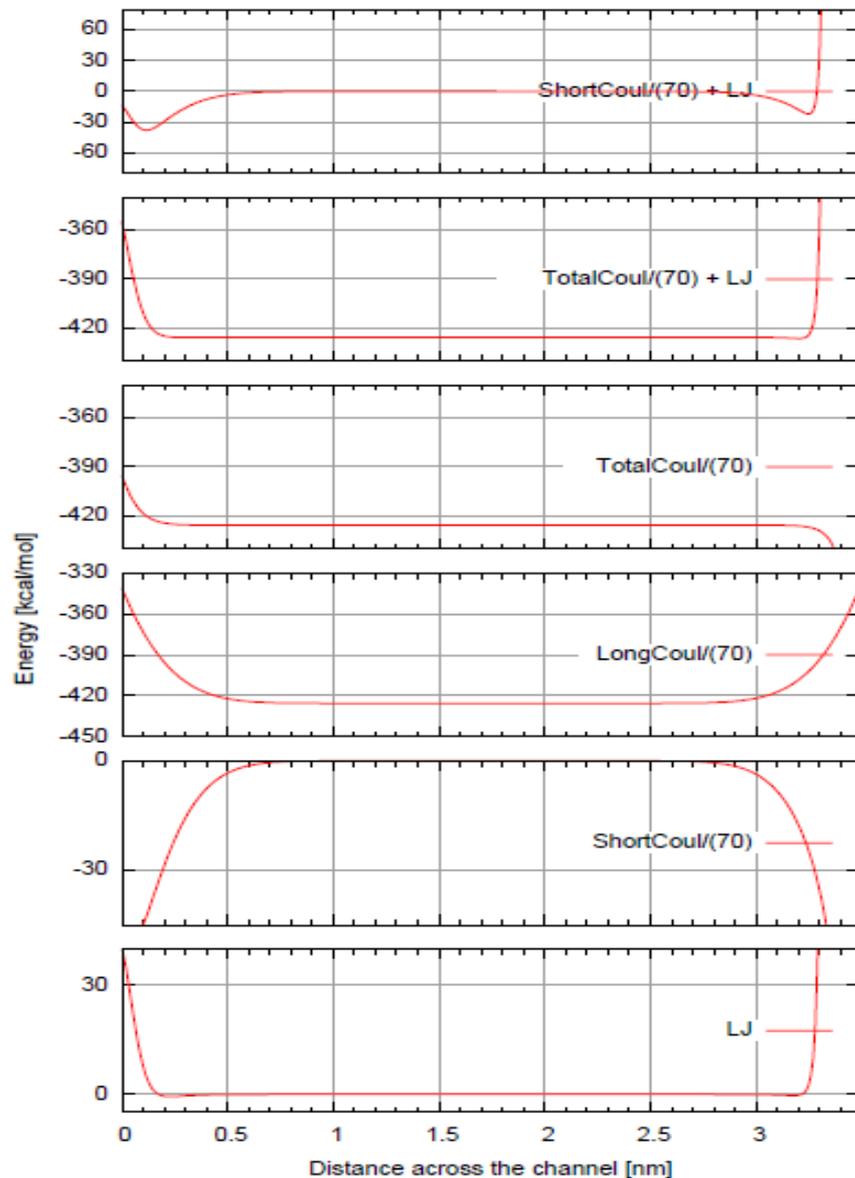
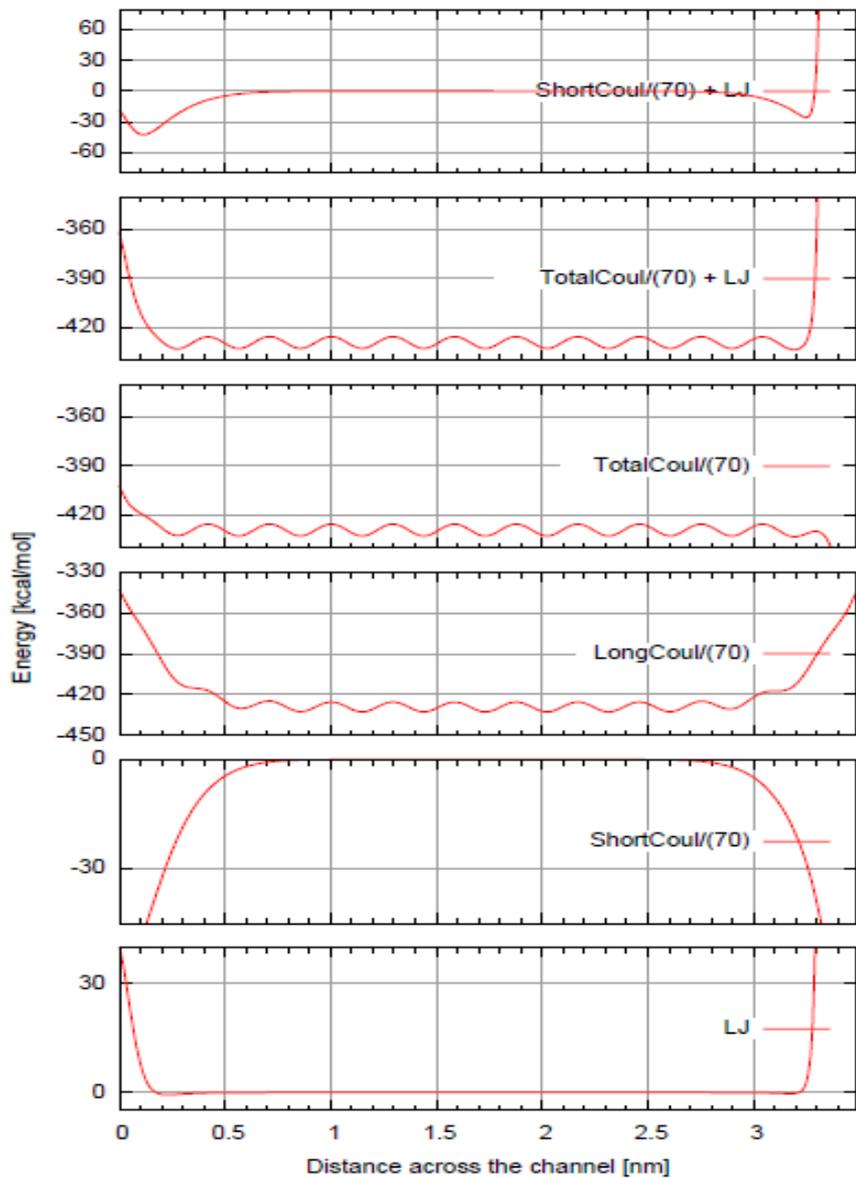


Potential energy profile of an ions was measured along the line perpendicular to the surface

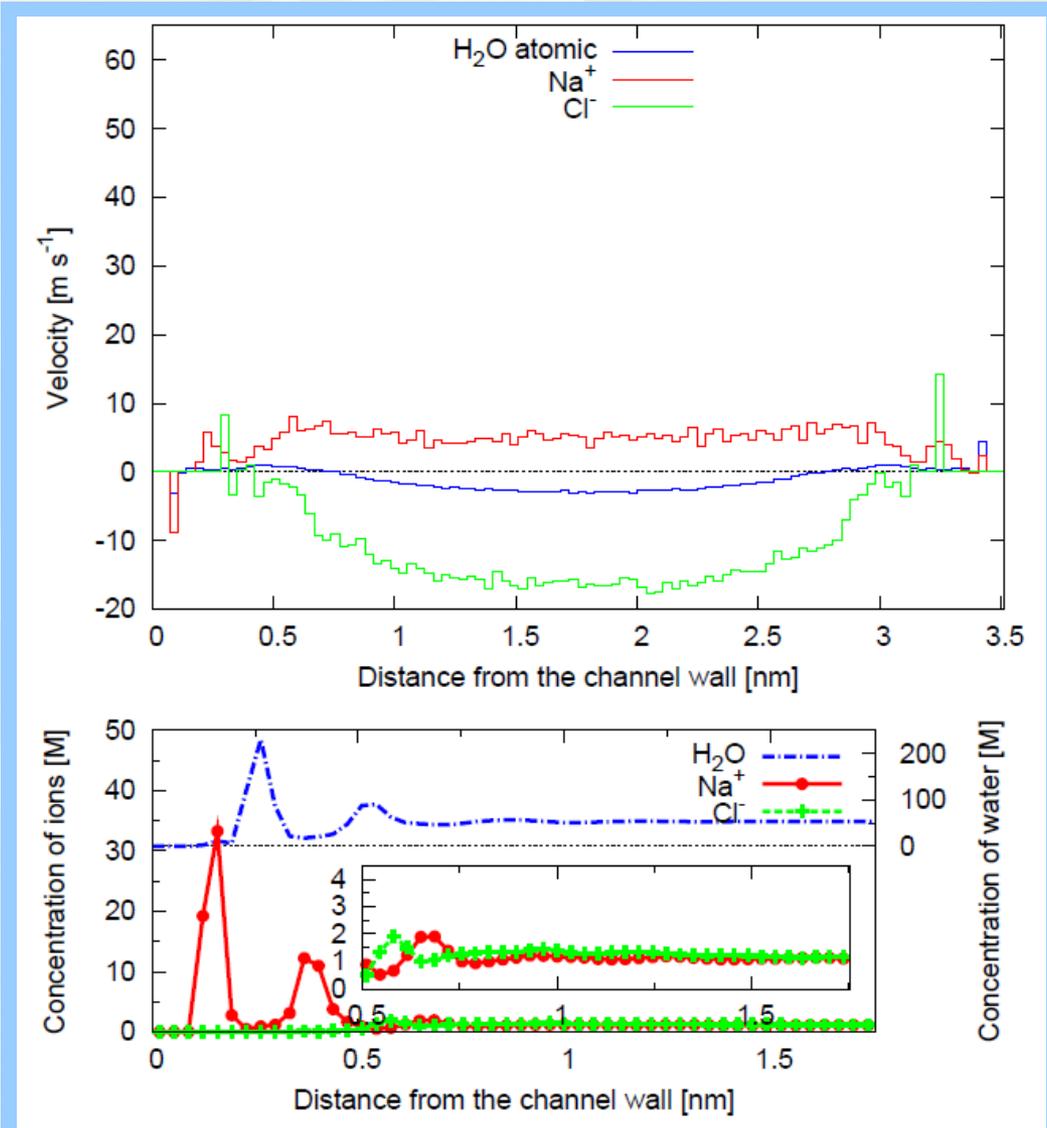
The line passed through different adsorption sites

# PPPM

# Ewald sum



# Effects of ionic concentrations



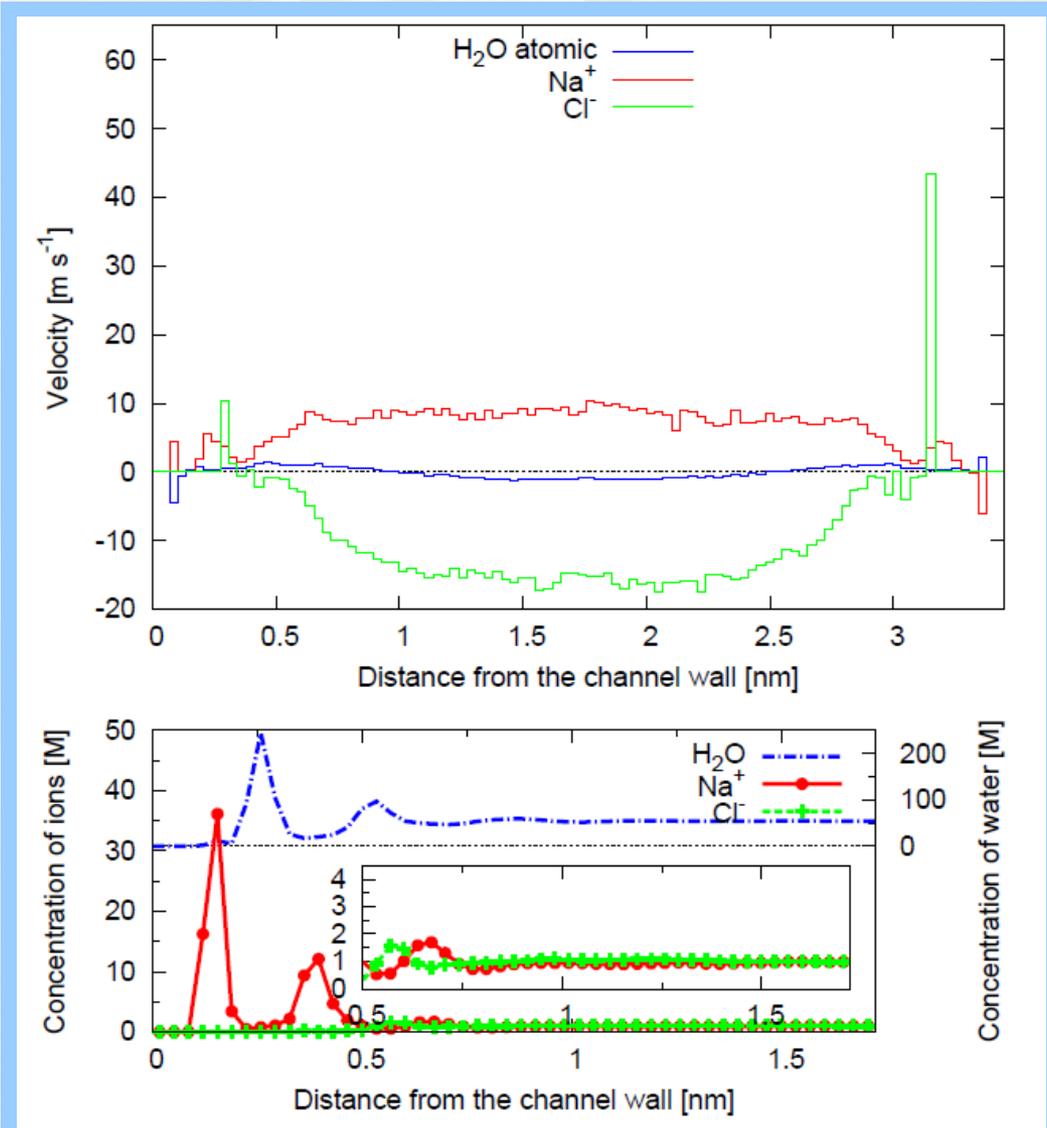
Surface charge:  
-70 e

Na<sup>+</sup>:  
108

Cl<sup>-</sup>:  
38



# Effects of ionic concentrations



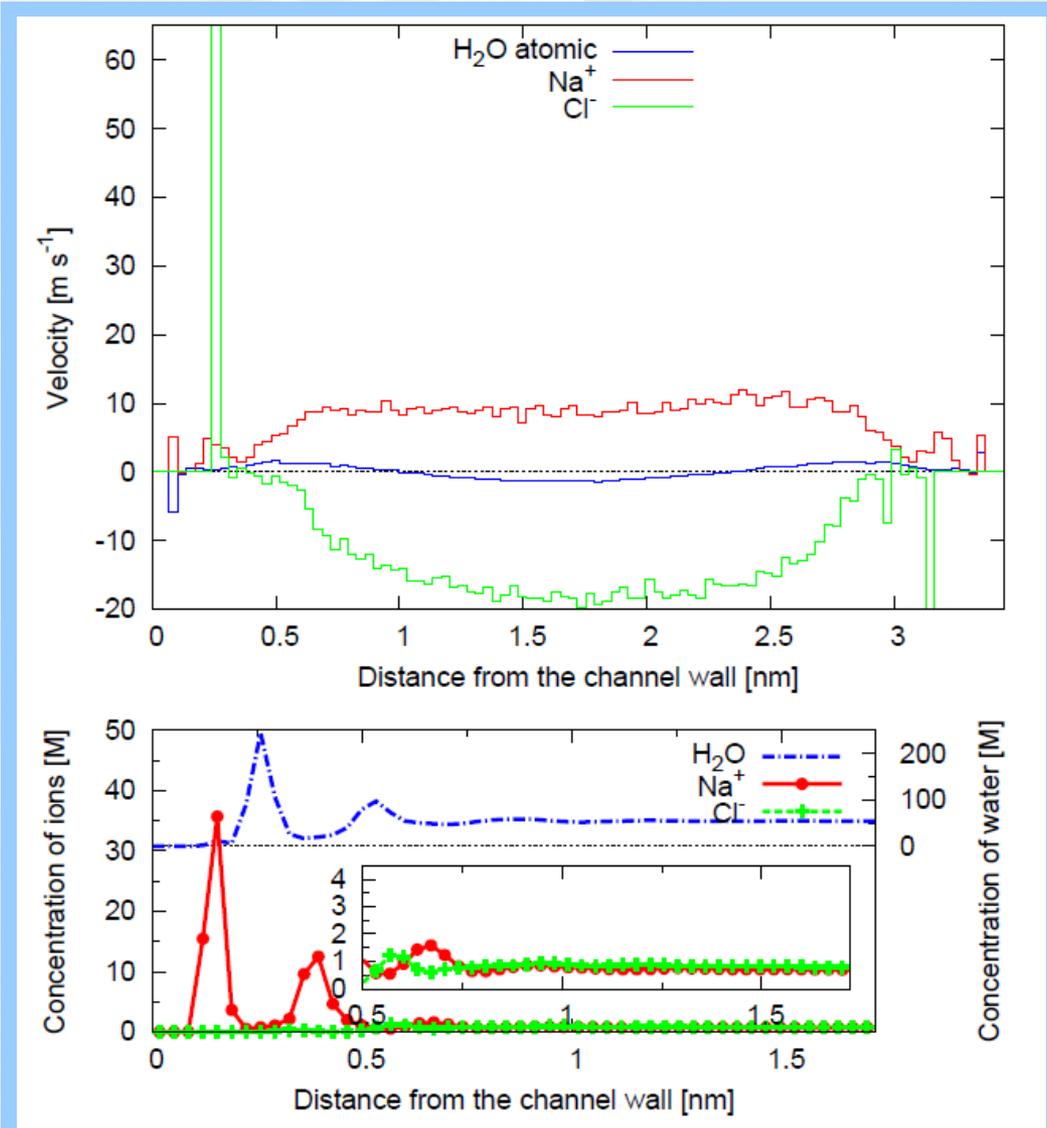
Surface charge:  
-70 e

Na<sup>+</sup>:  
100

Cl<sup>-</sup>:  
30



# Effects of ionic concentrations



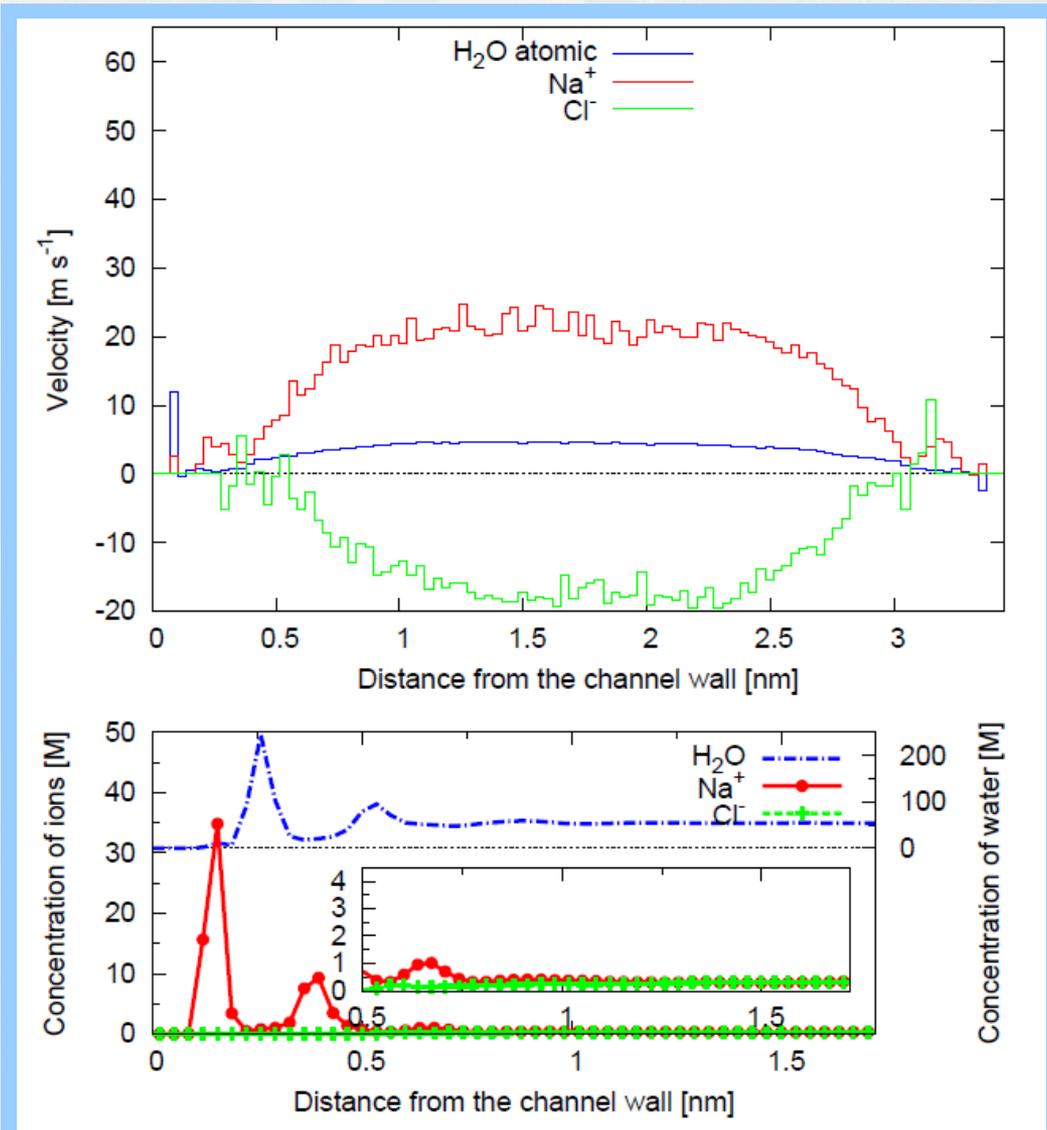
Surface charge:  
-70 e

Na<sup>+</sup>:  
93

Cl<sup>-</sup>:  
23



# Effects of ionic concentrations



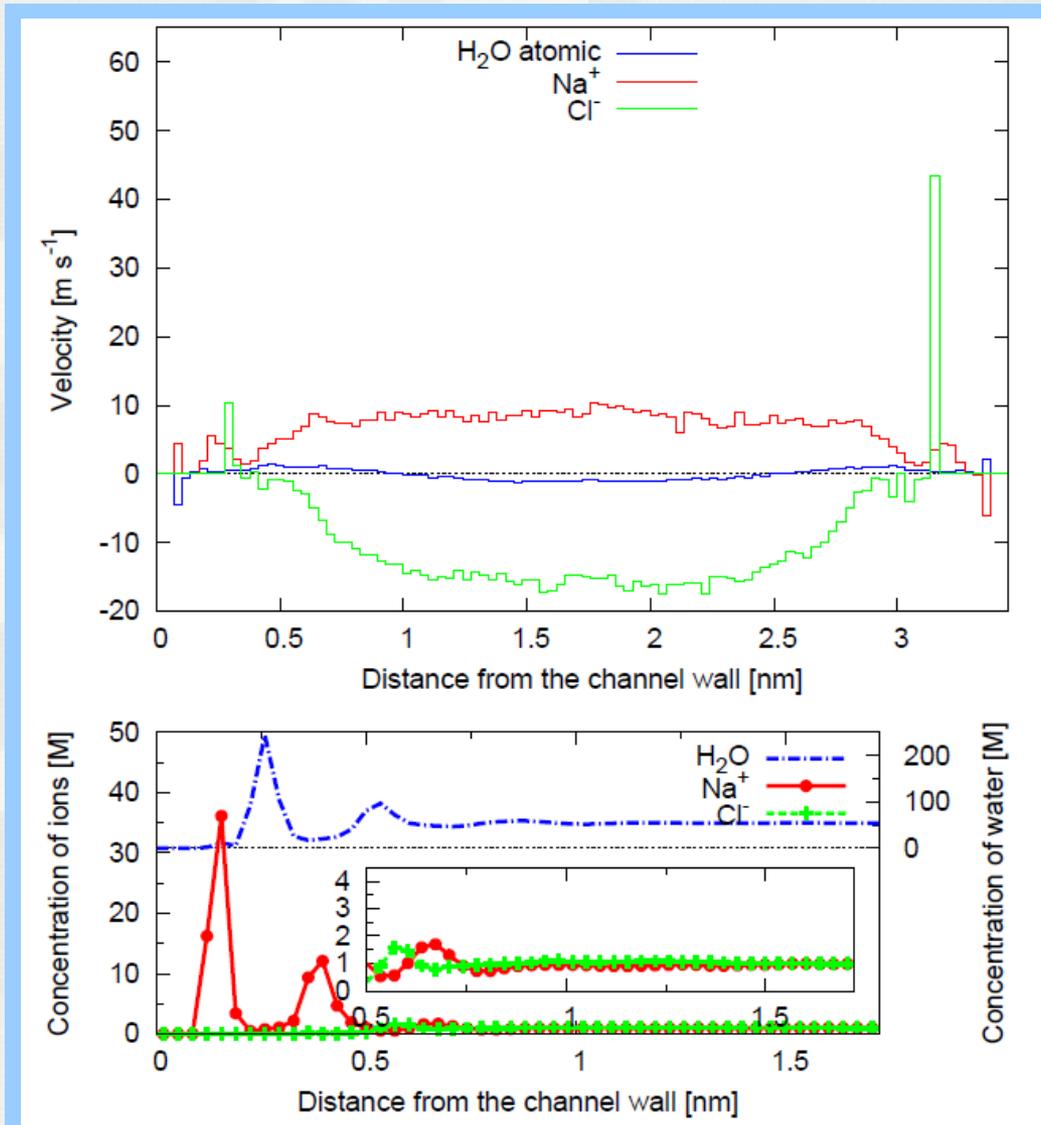
Surface charge:  
-70 e

Na<sup>+</sup>:  
78

Cl<sup>-</sup>:  
8



# Effects of surface charge density



Surface charge:

-70 e

Na<sup>+</sup>:

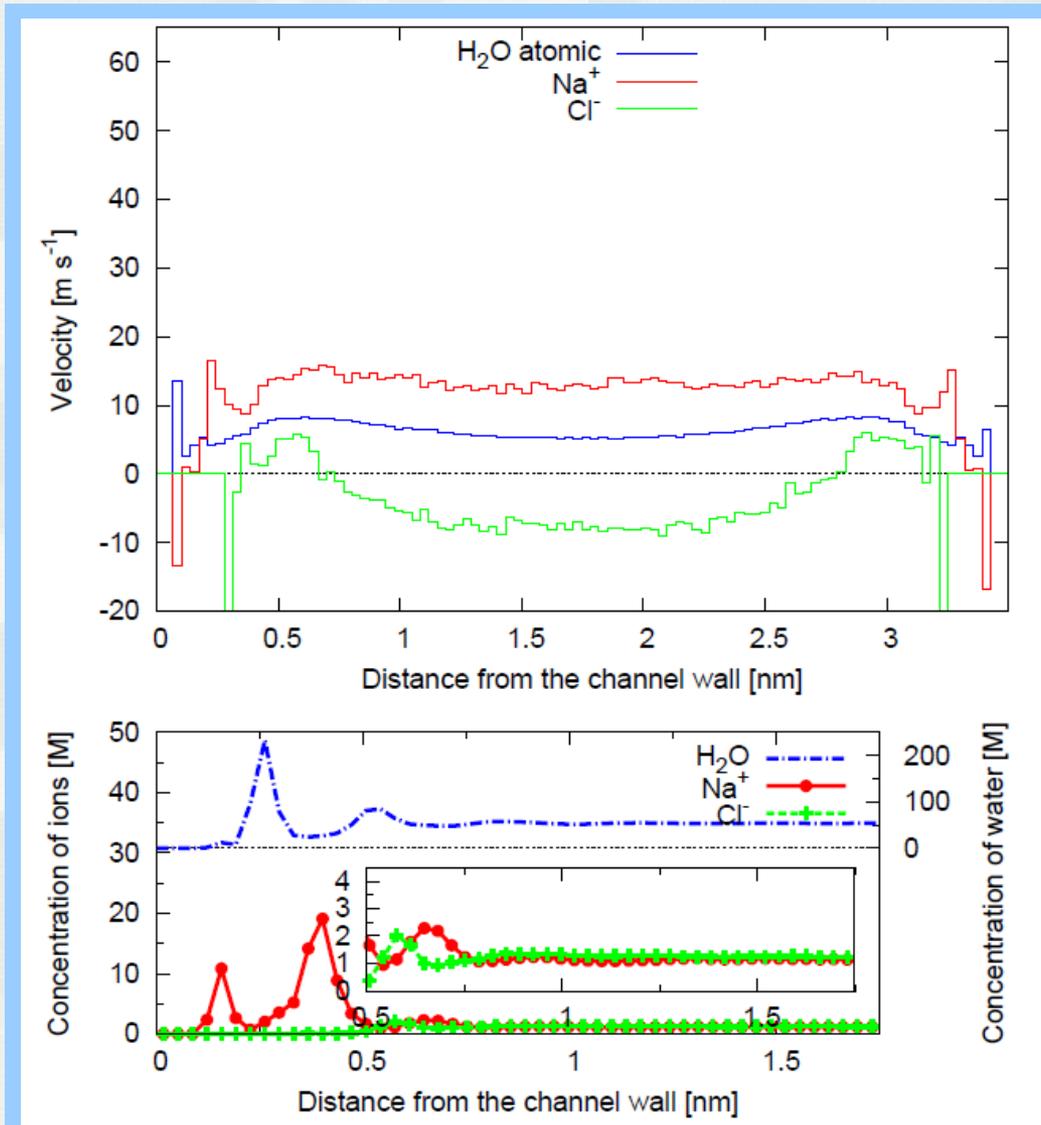
100

Cl<sup>-</sup>:

30



# Effects of surface charge density



Surface charge:

-60 e

Na<sup>+</sup>:

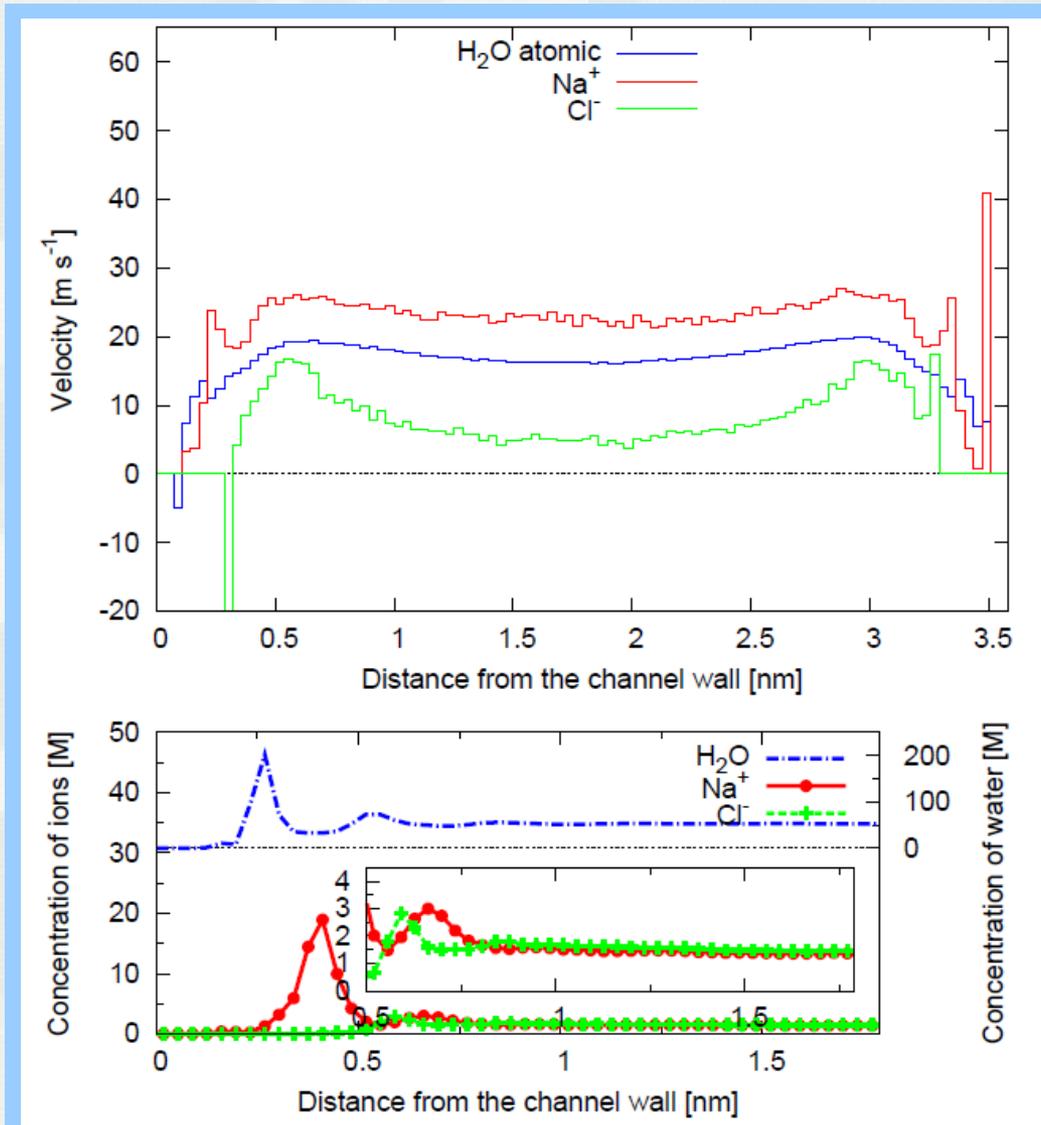
100

Cl<sup>-</sup>:

40



# Effects of surface charge density



Surface charge:

-50 e

Na<sup>+</sup>:

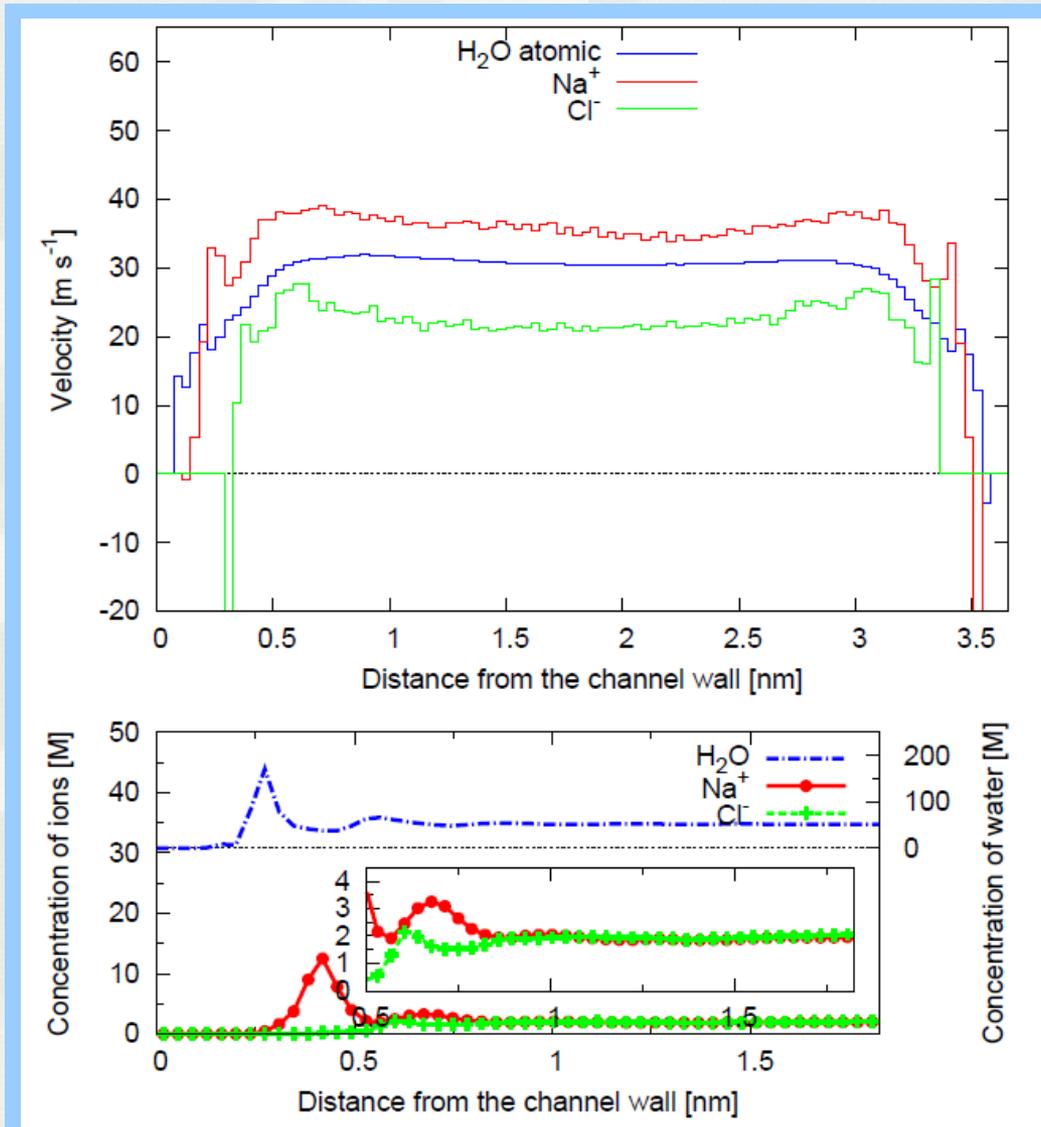
100

Cl<sup>-</sup>:

50



# Effects of surface charge density



Surface charge:

-40 e

Na<sup>+</sup>:

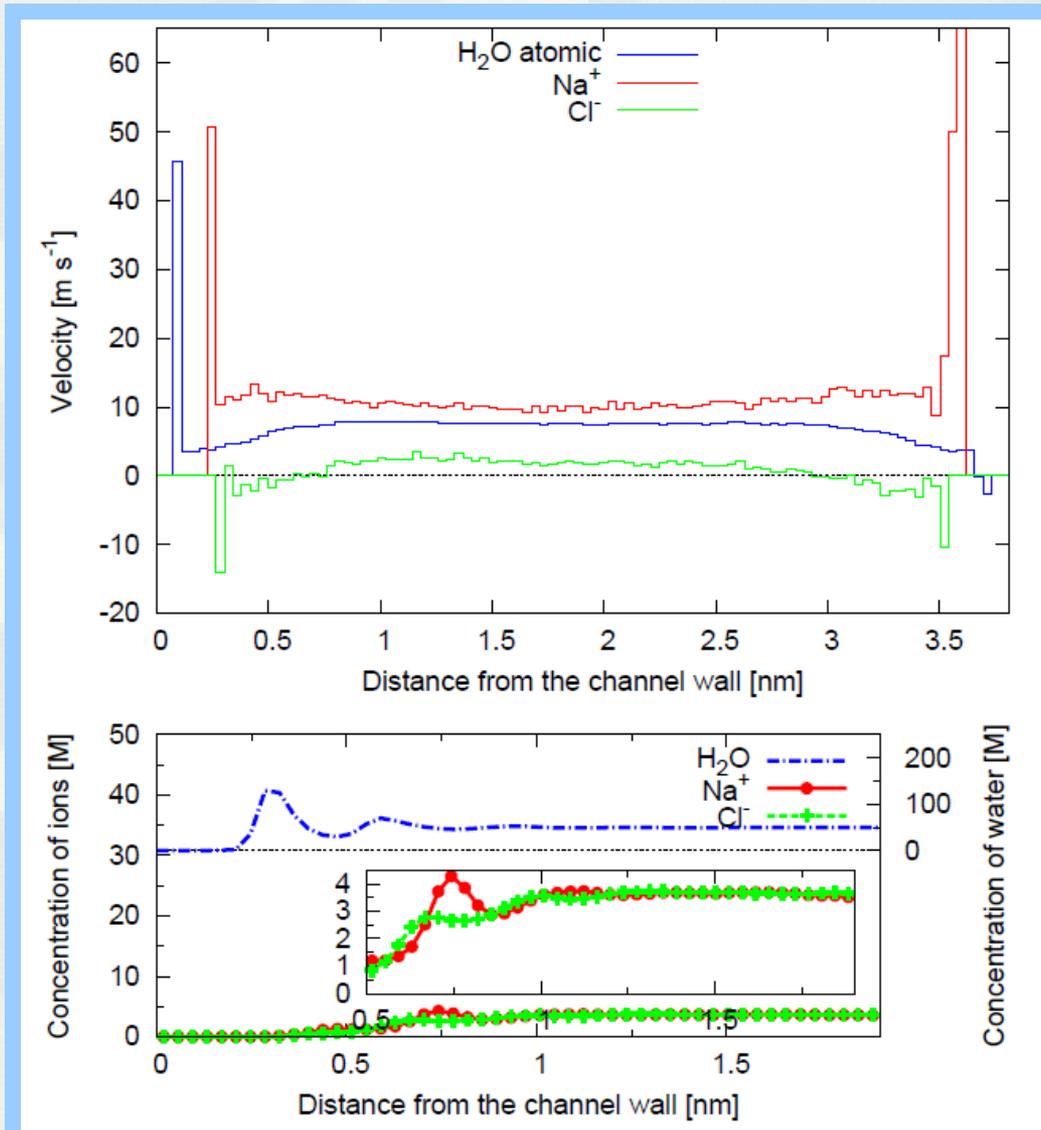
100

Cl<sup>-</sup>:

60



# Low surface charge density flow



Surface charge:

-4 e

Na<sup>+</sup>:

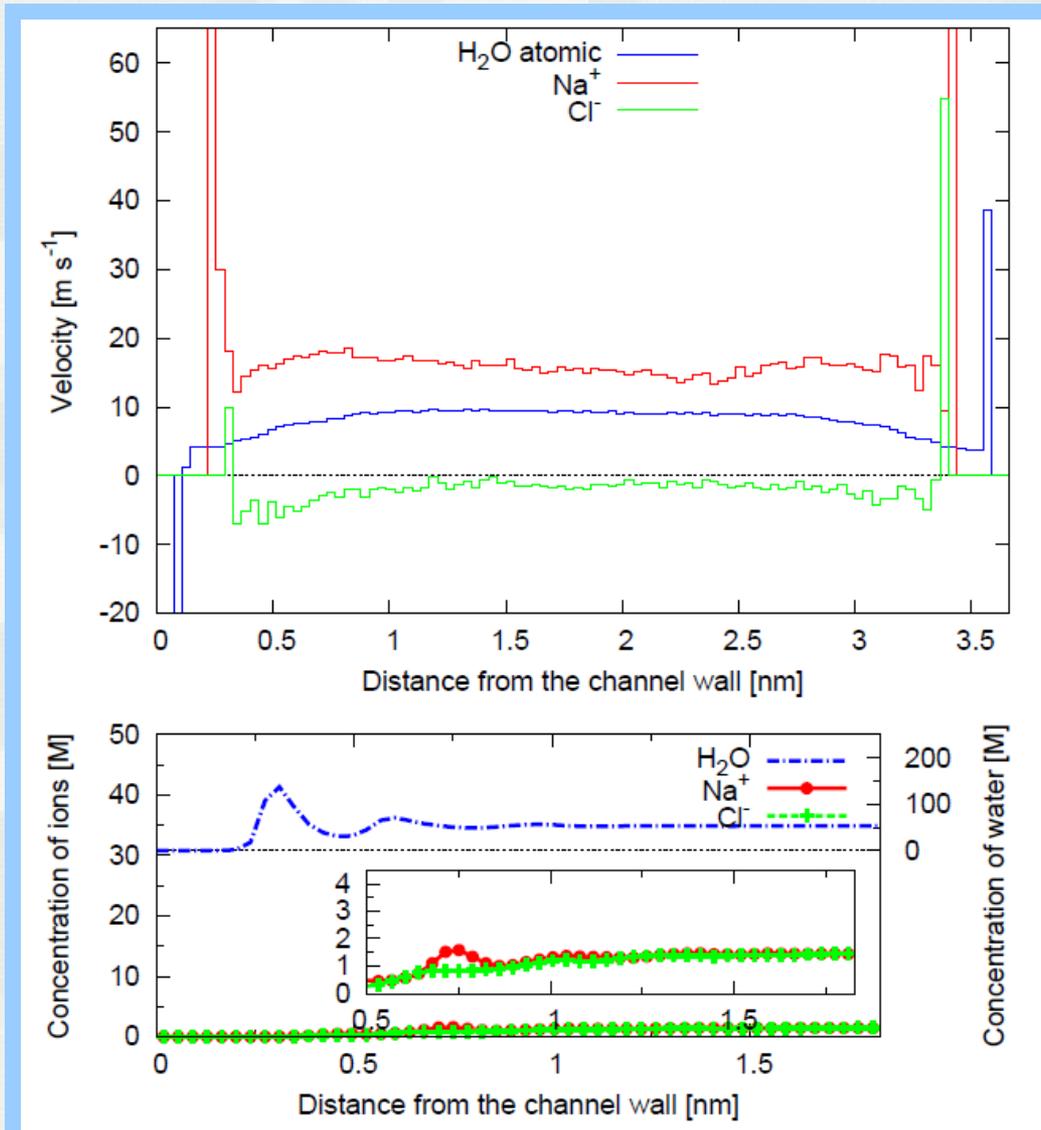
108

Cl<sup>-</sup>:

104



# Low surface charge density flow



Surface charge:

-4 e

Na<sup>+</sup>:

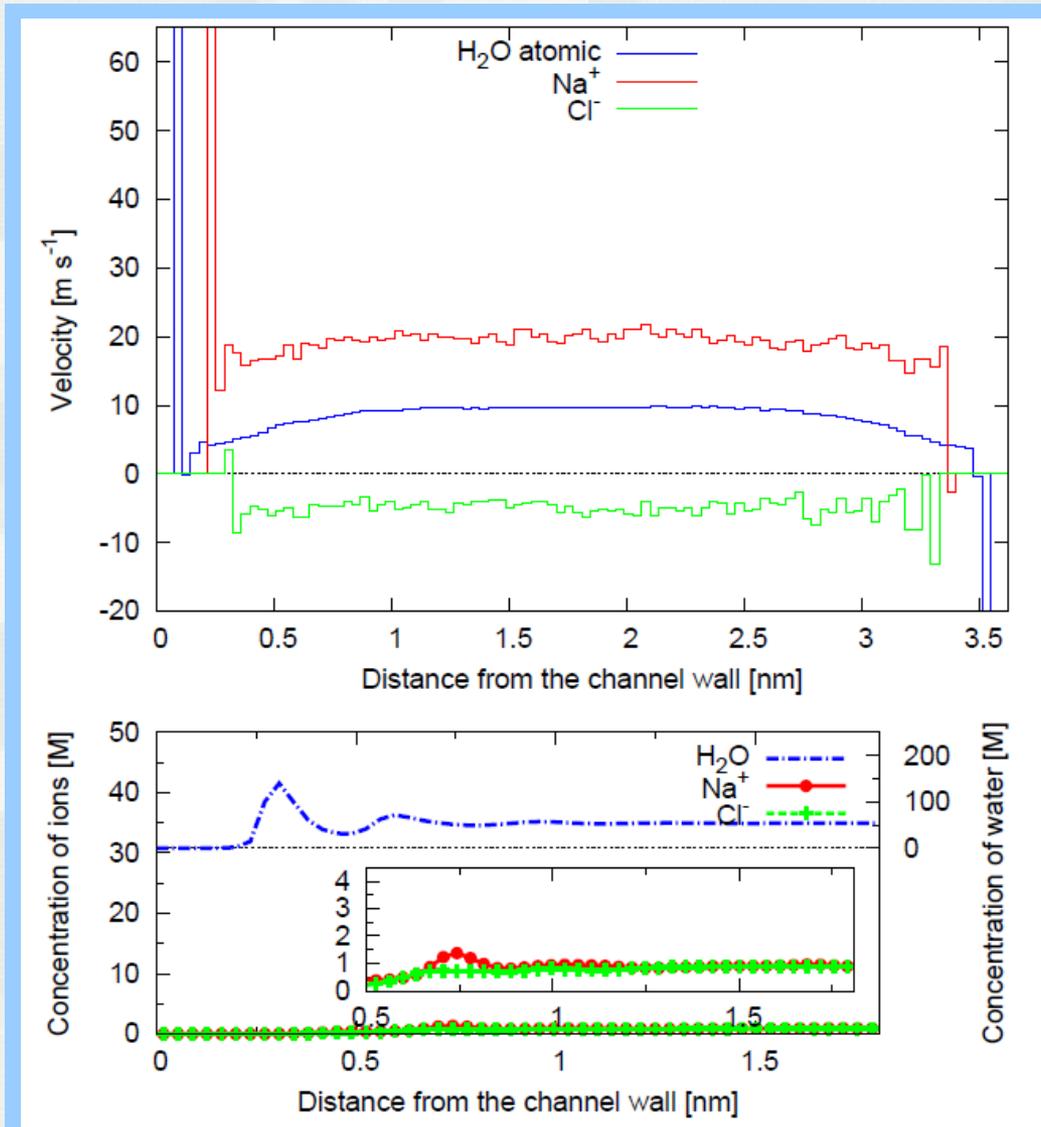
44

Cl<sup>-</sup>:

40



# Low surface charge density flow



Surface charge:

-4 e

Na<sup>+</sup>:

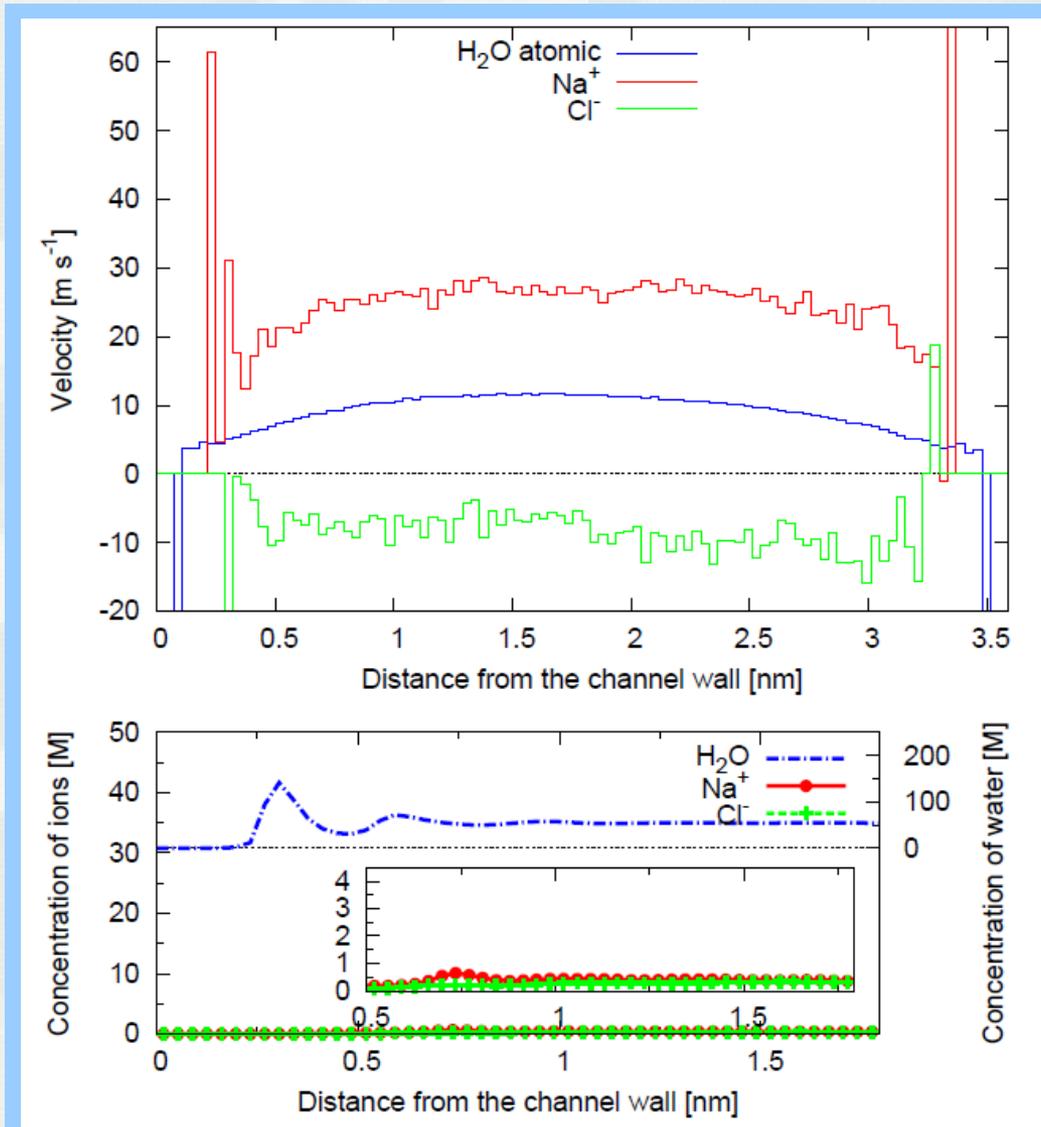
28

Cl<sup>-</sup>:

24



# Low surface charge density flow



Surface charge:

-4 e

Na<sup>+</sup>:

12

Cl<sup>-</sup>:

8



# Conclusions

- Studied temperature, viscosity, and charge density effects on a nanochannel electroosmotic flow by MD simulations
- Obtained velocity, mass flux, ionic concentration, and viscosity profiles
- Justified temperature dependence of water flow direction by thermal release of adsorbed  $\text{Na}^+$  ions and spatial variation of viscosity
- Demonstrated an improved prediction of velocity profile from charge density using non-constant viscosity
- Revealed the dependence of the flow on surface charge density and ionic concentrations