

Parallelization and performance tests of the large scale LBM-CA solidification model

Bohumir Jelinek

Postdoctoral Fellow

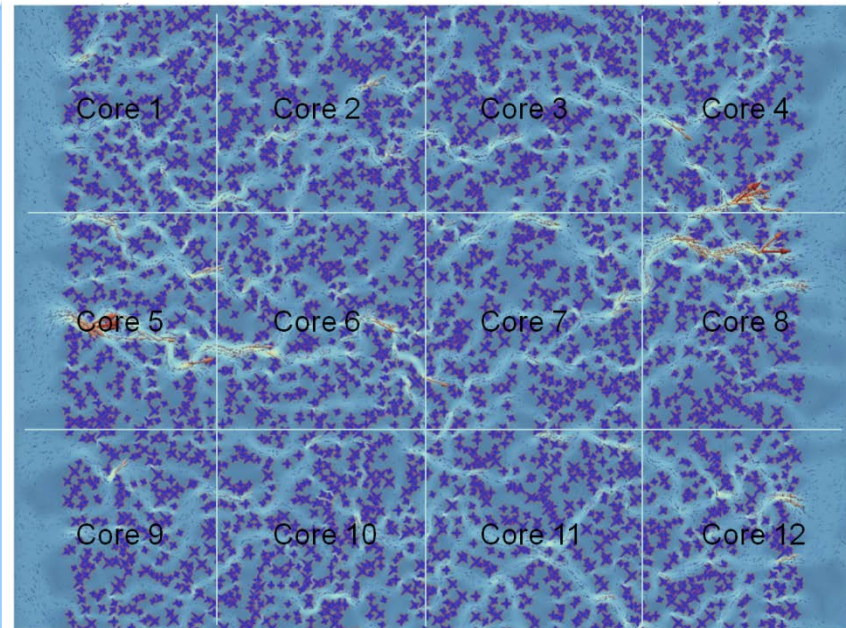
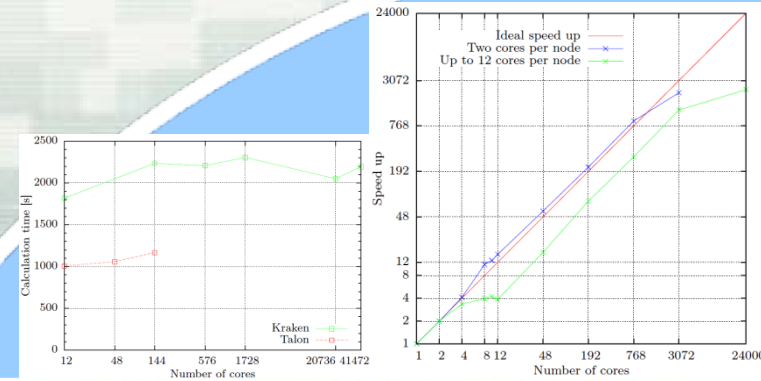
CAVS, Mississippi State University

Columbus, 11/27/2012



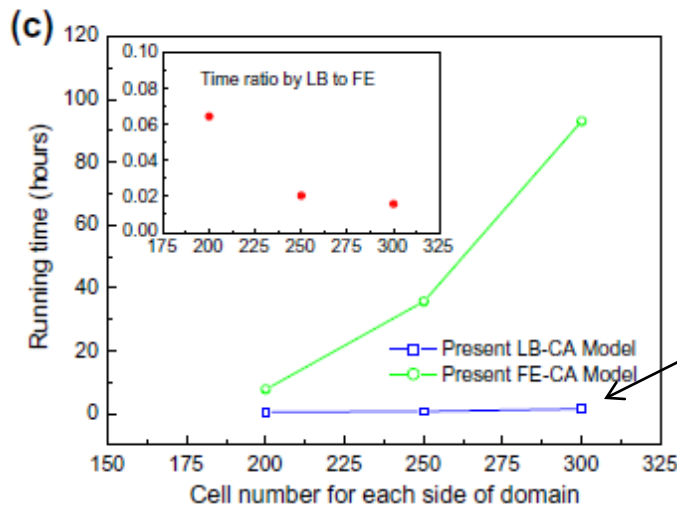
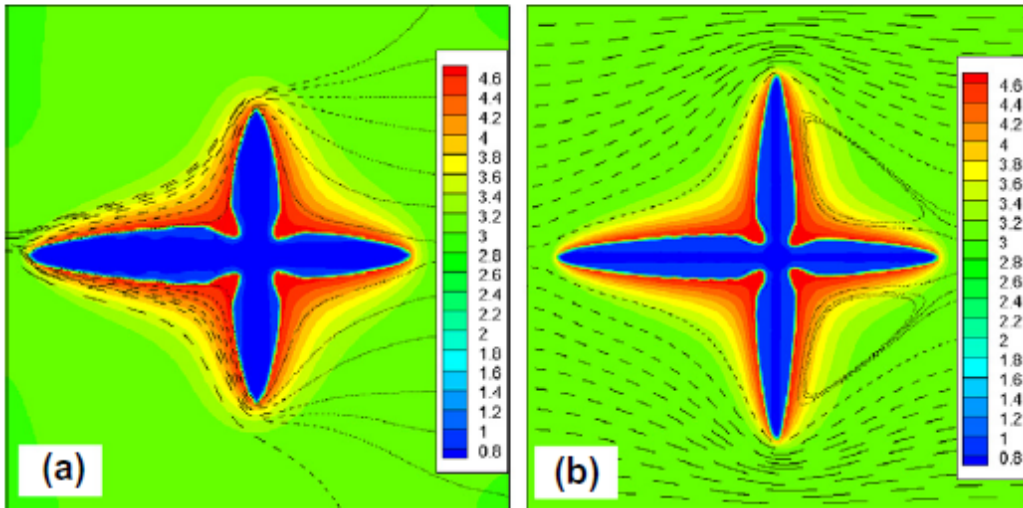
MISSISSIPPI STATE
UNIVERSITY
CAVS

US Army Corps of Engineers
BUILDING STRONG



Why LBM-CA?

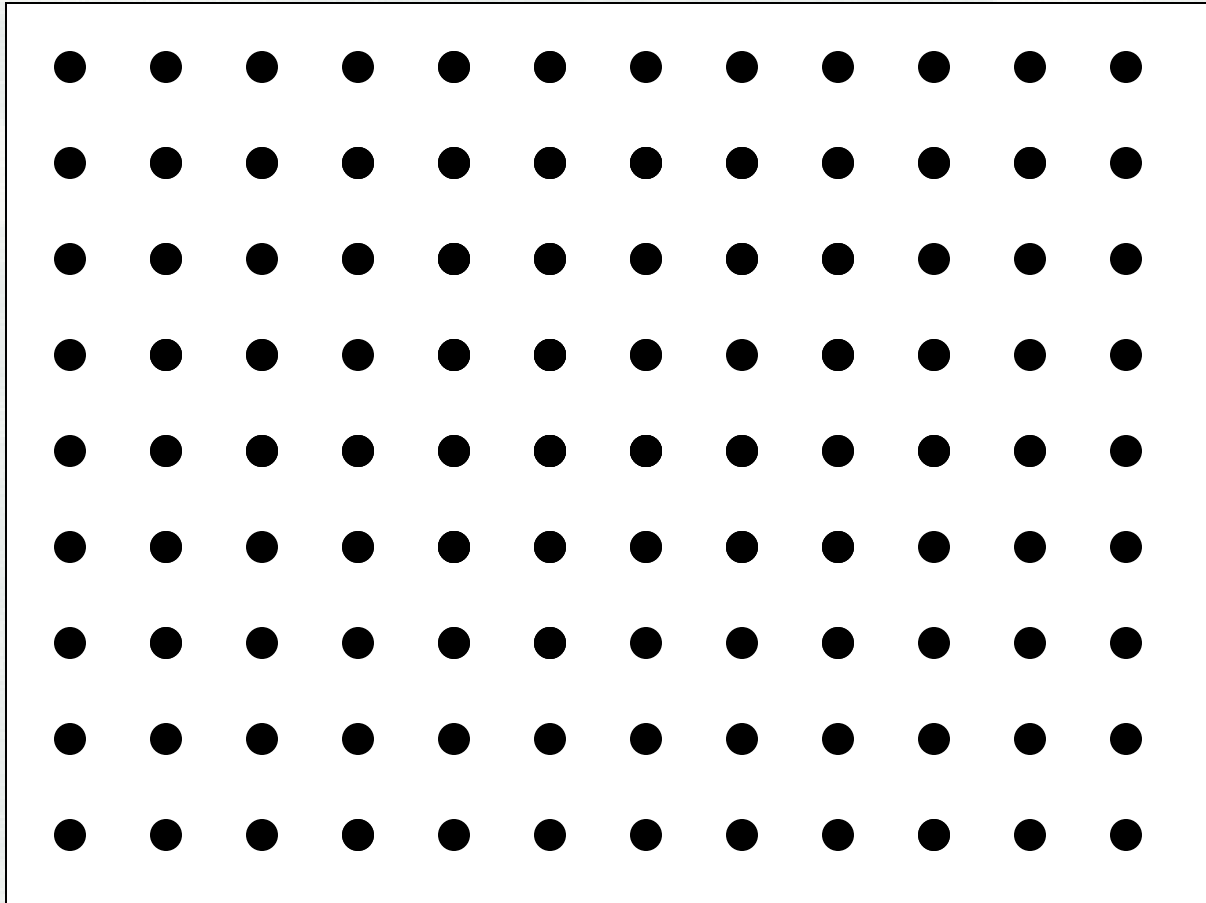
H. Yin et al. / Acta Materialia 59 (2011) 3124–3136



When fluid flow around solidifying dendrites is considered, lattice Boltzmann method is faster than alternatives



LBM parallelization



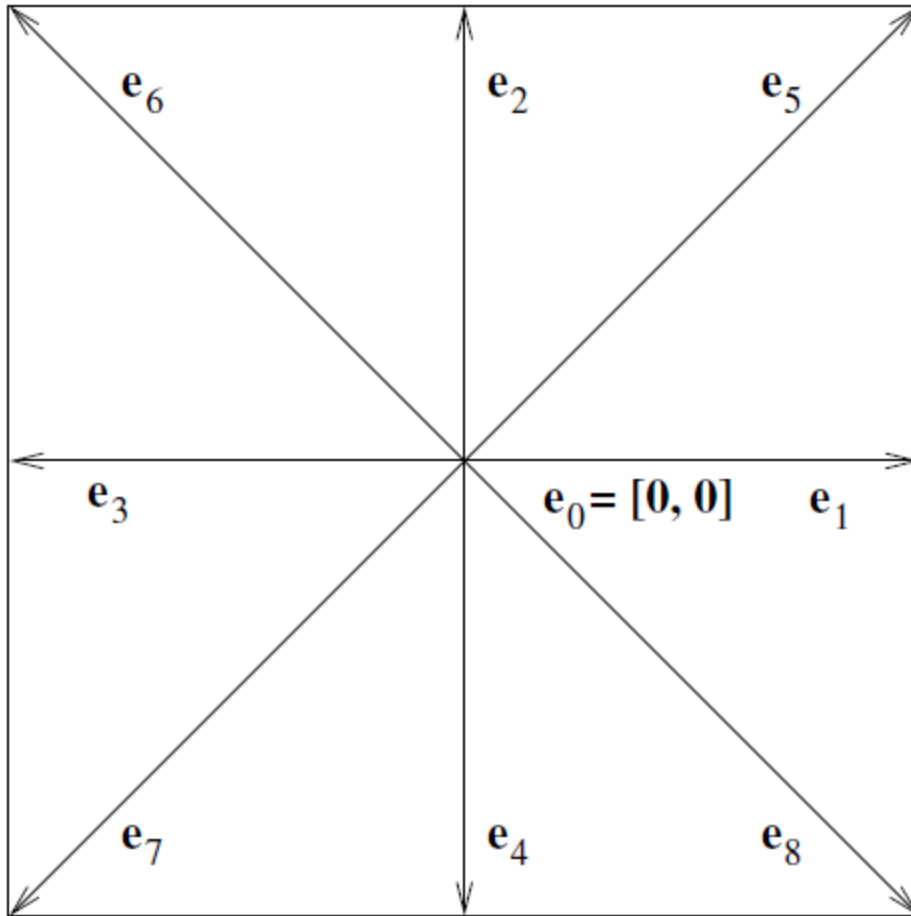
Lattice-Boltzmann method (LBM) calculates values of a quantity of interest at regularly spaced nodes governed by a partial differential equation subject to given boundary conditions.

Acknowledgment: Mohsen Eshraghi provided excellent code guide and parallelization suggestions.



LBM:

$$f_i(\mathbf{r} + \mathbf{e}_i \Delta t, t + \Delta t) = f_i(\mathbf{r}, t) + \frac{1}{\tau} (f_i^{eq}(\mathbf{r}, t) - f_i(\mathbf{r}, t))$$



- Collision and streaming step
- Distribution functions f_i in each of the lattice direction e_i representing portion of the particles moving in that direction

LBM parallelization

CPU 7	CPU 8	CPU 9
CPU 4	CPU 5	CPU 6
CPU 1	CPU 2	CPU 3

Spatial domain
decomposition



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, **E**)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



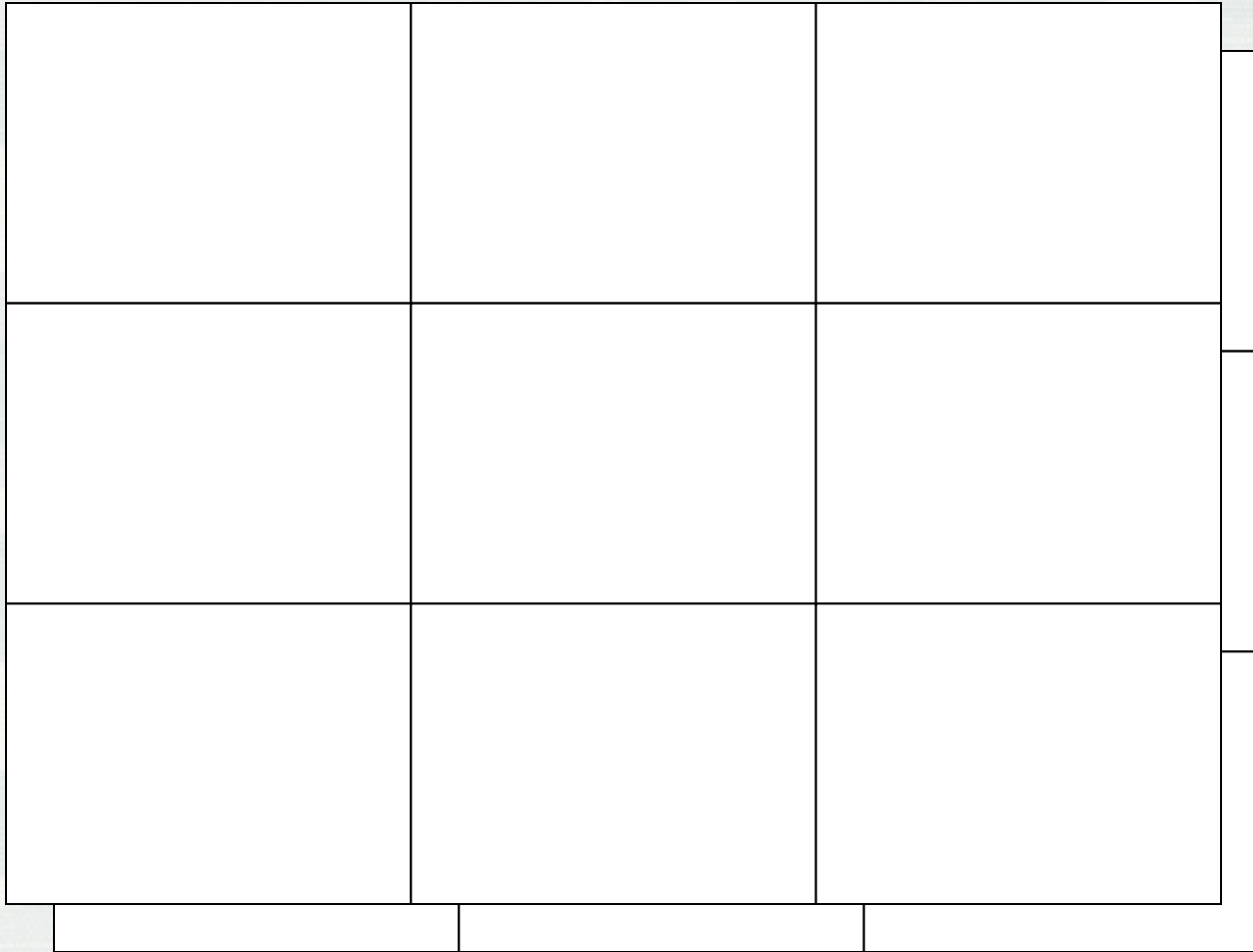
LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



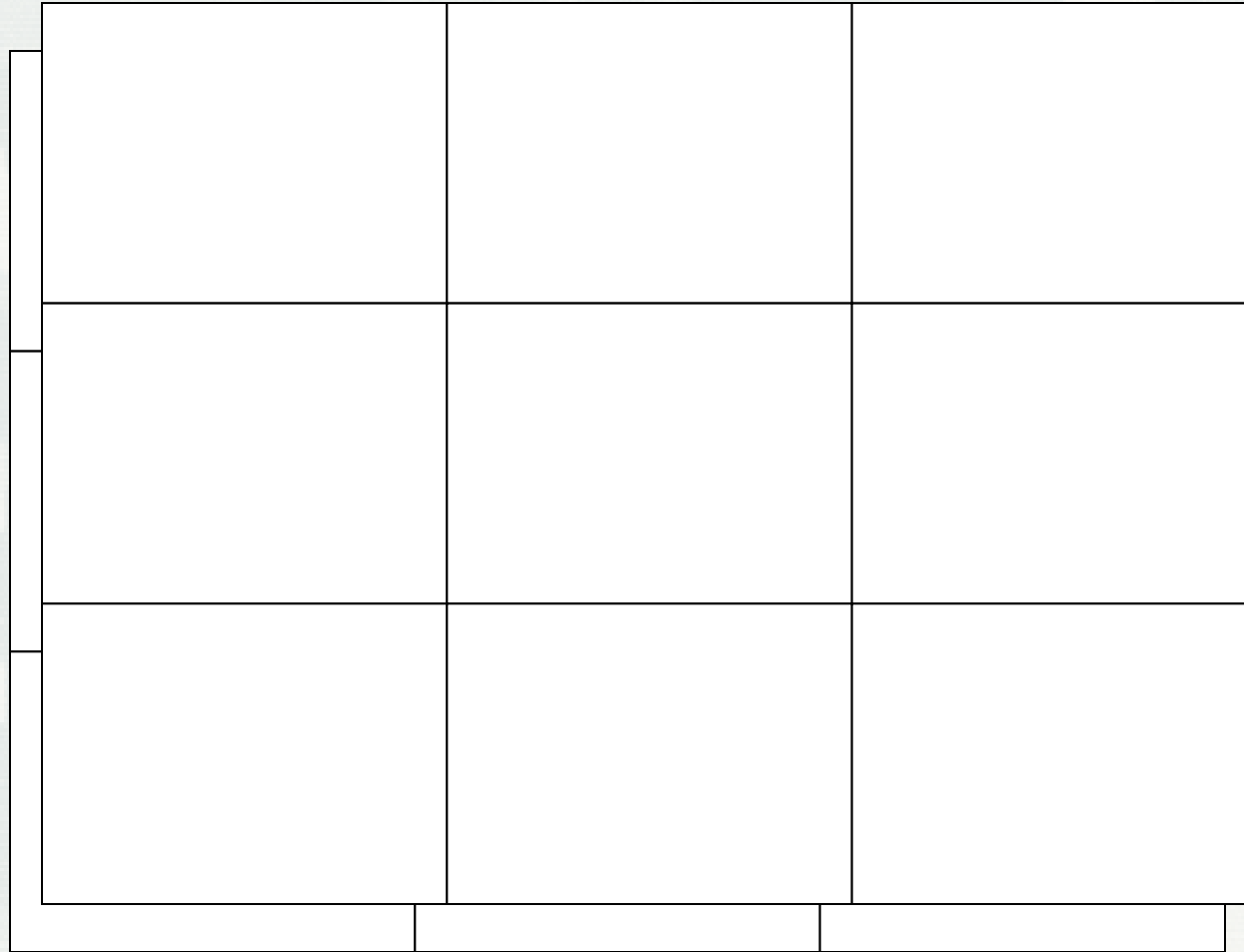
LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, **NE**, SW, SE)



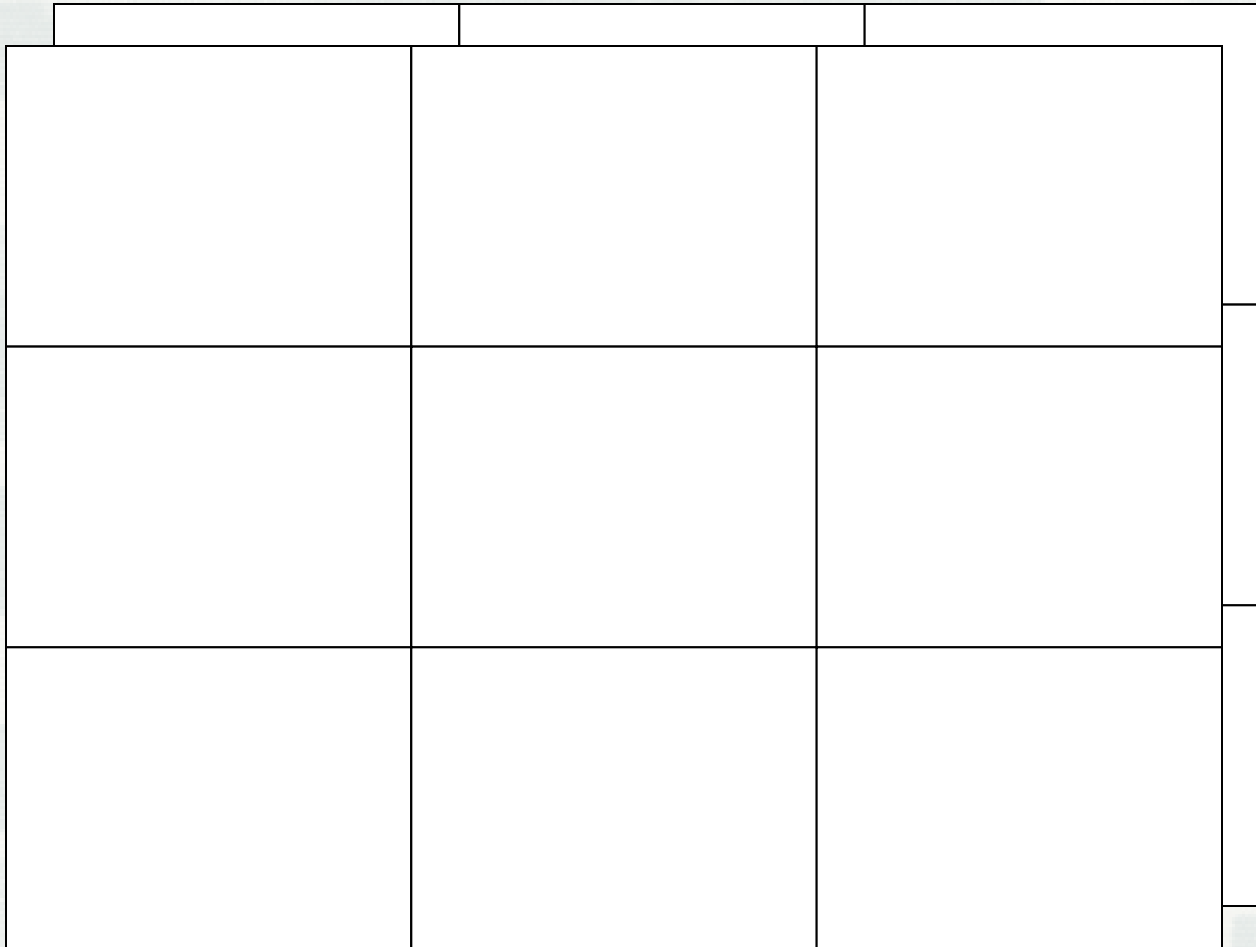
LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



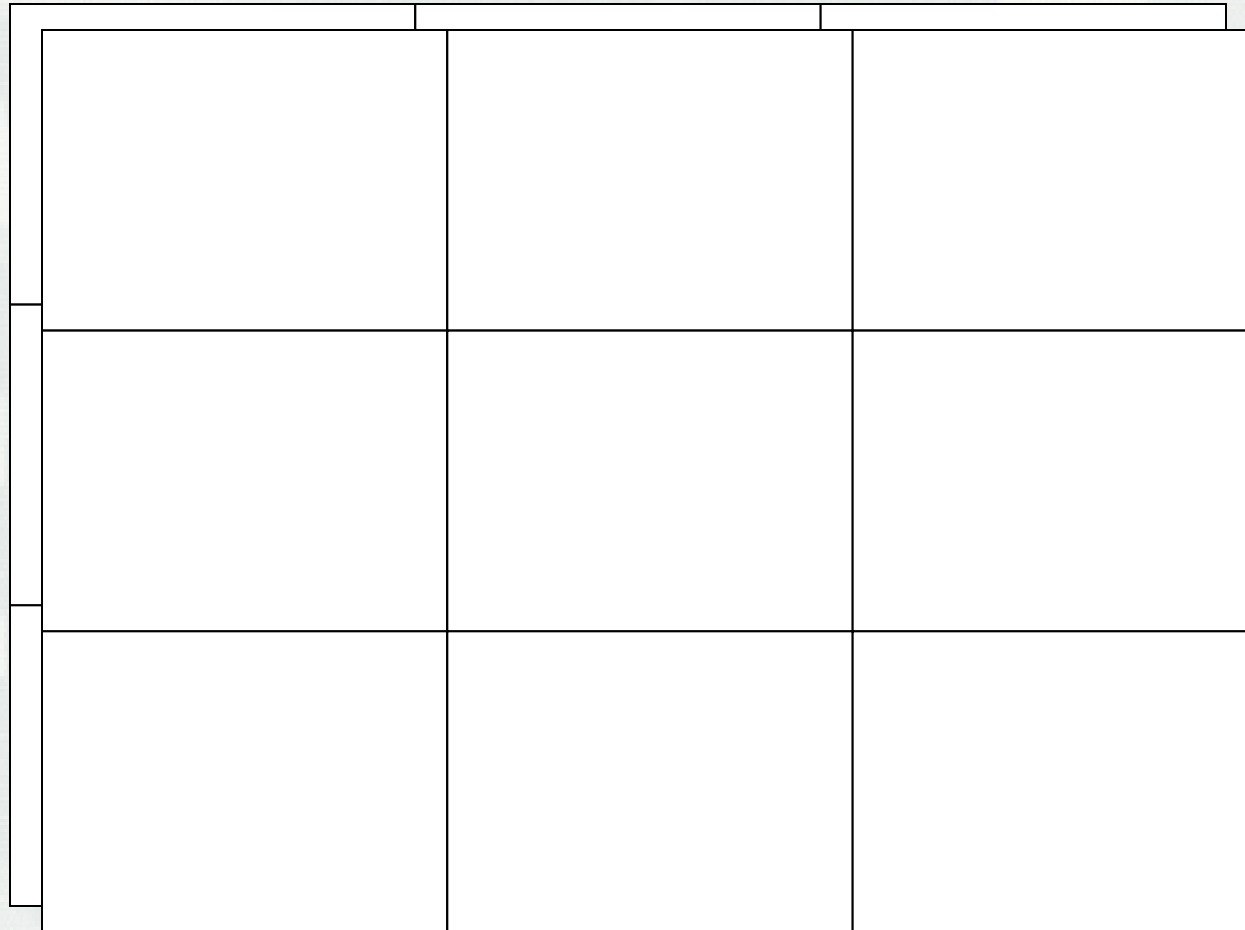
LBM parallelization – streaming

Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, SE)



LBM parallelization – streaming

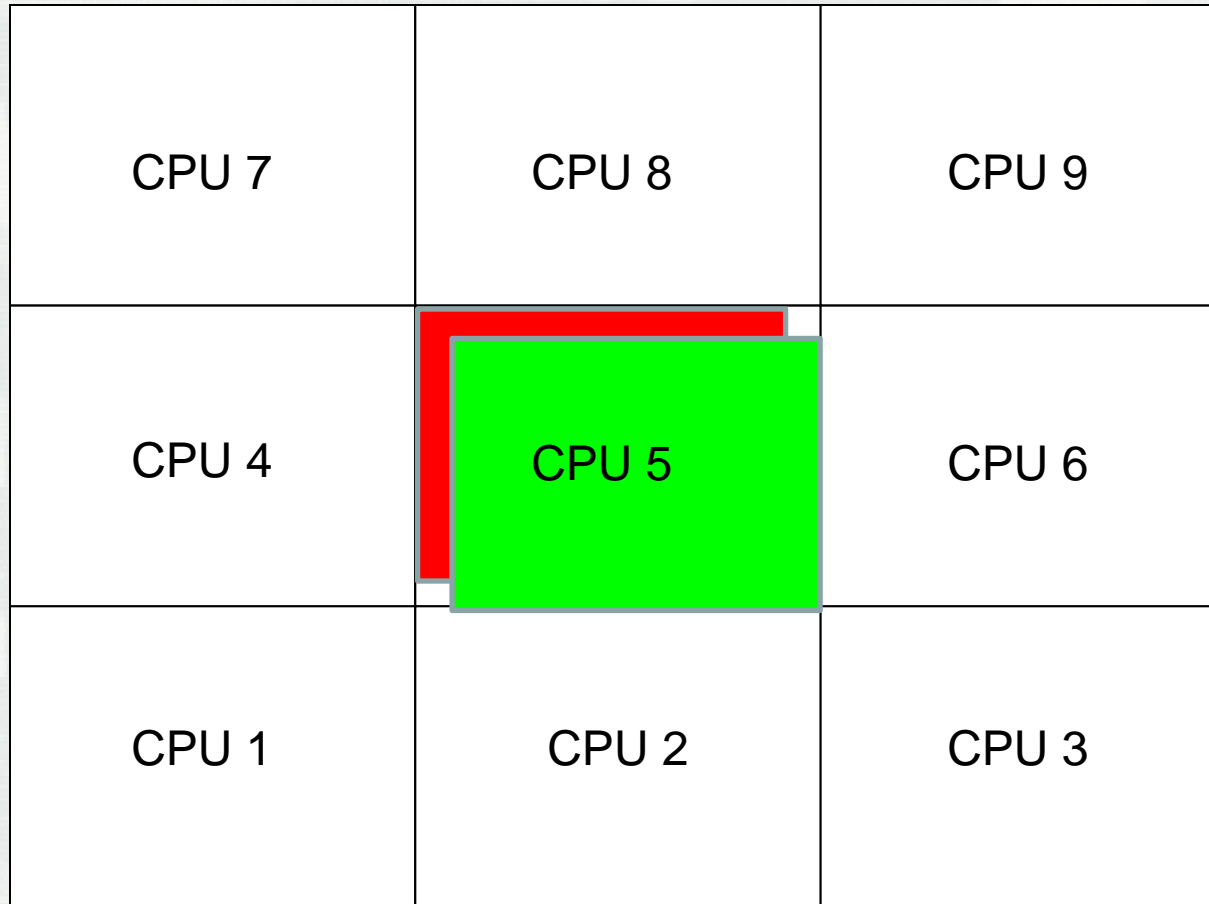


Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, **SE**)



LBM parallelization – streaming

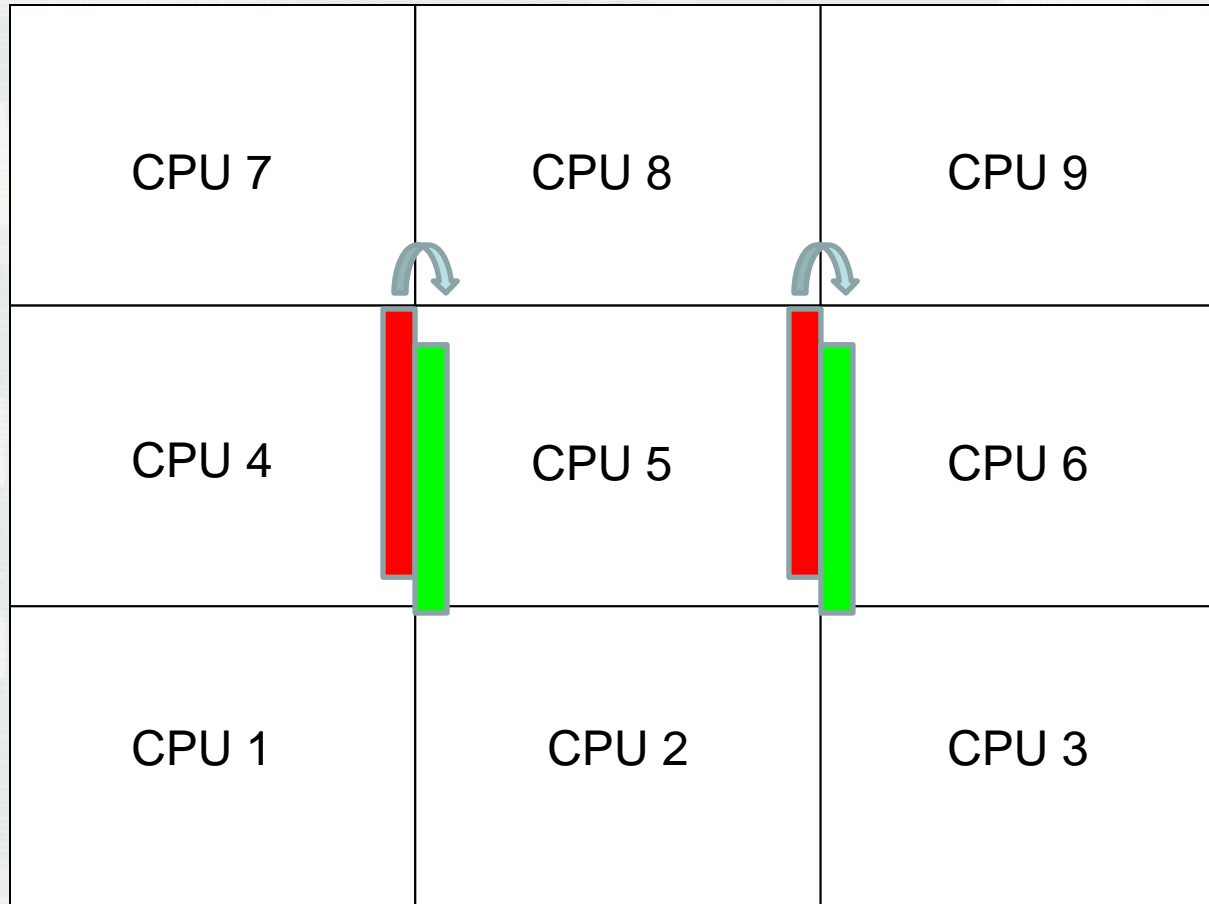


Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, **SE**)



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, **SE**)

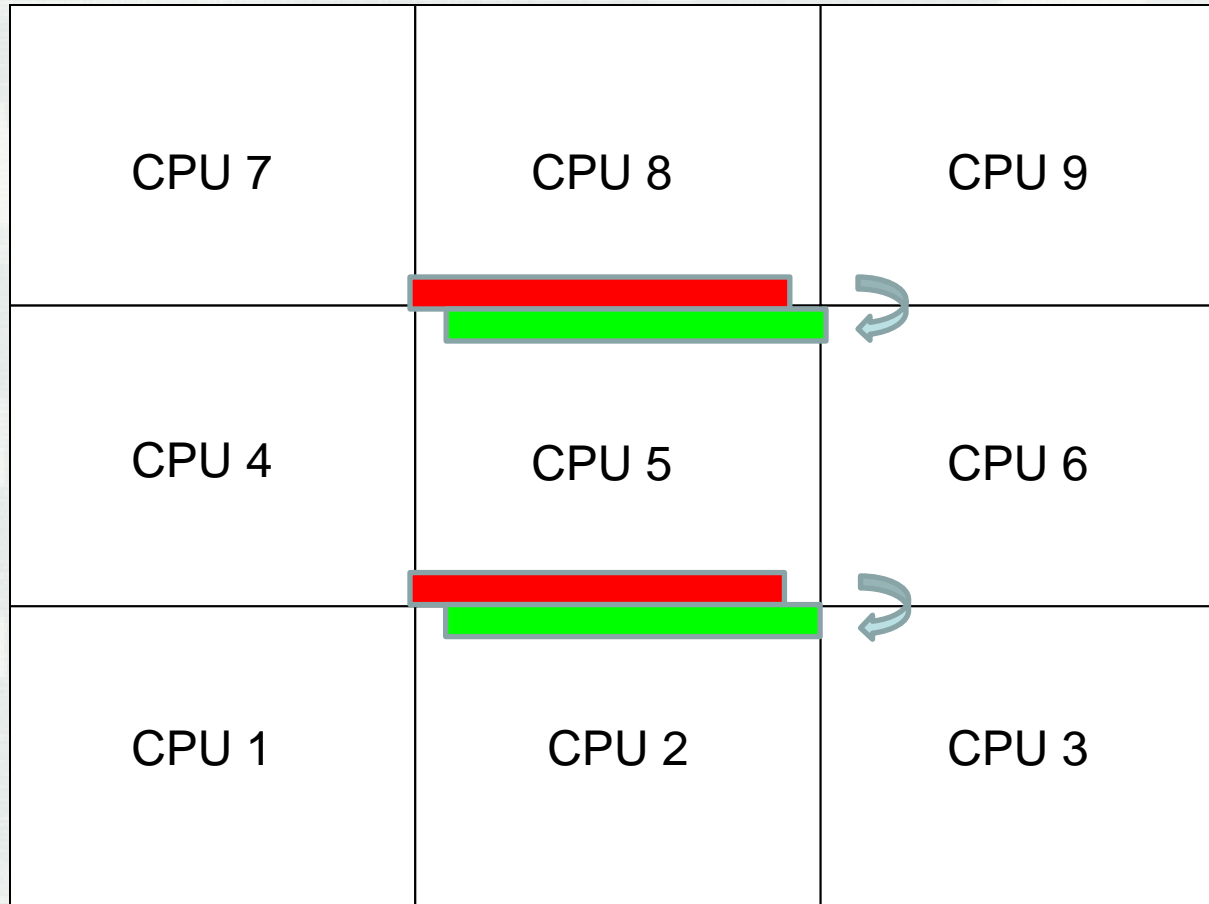
buffer=**send**

MPI_Sendrcv_replace(
buffer, dst=6, src=4)

recv=buffer



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, **SE**)

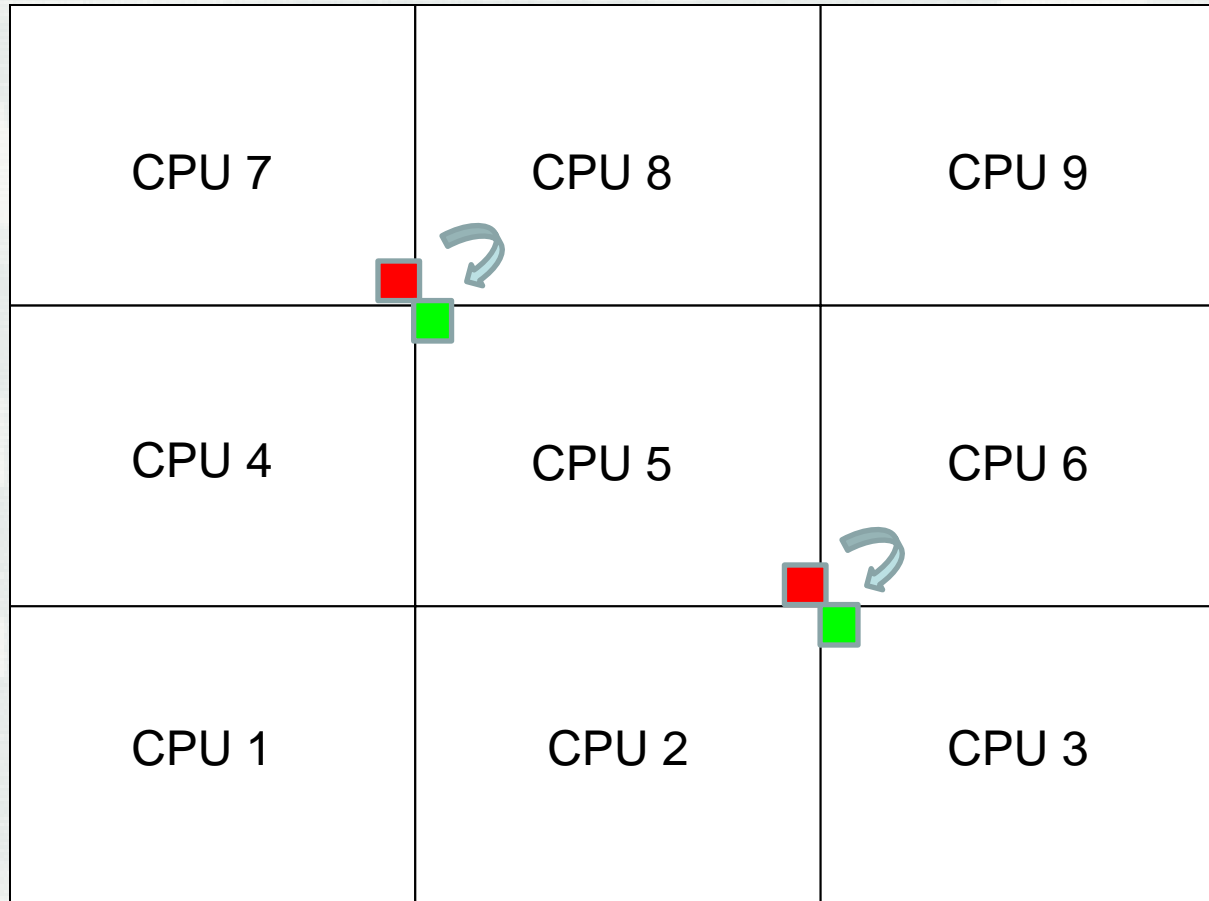
buffer=**send**

MPI_Sendrcv_replace(
buffer, dst=2, src=8)

recv=buffer



LBM parallelization – streaming



Direction

- horizontal (W, E)
- vertical (N, S)
- diagonal (NW, NE, SW, **SE**)

buffer=**send**

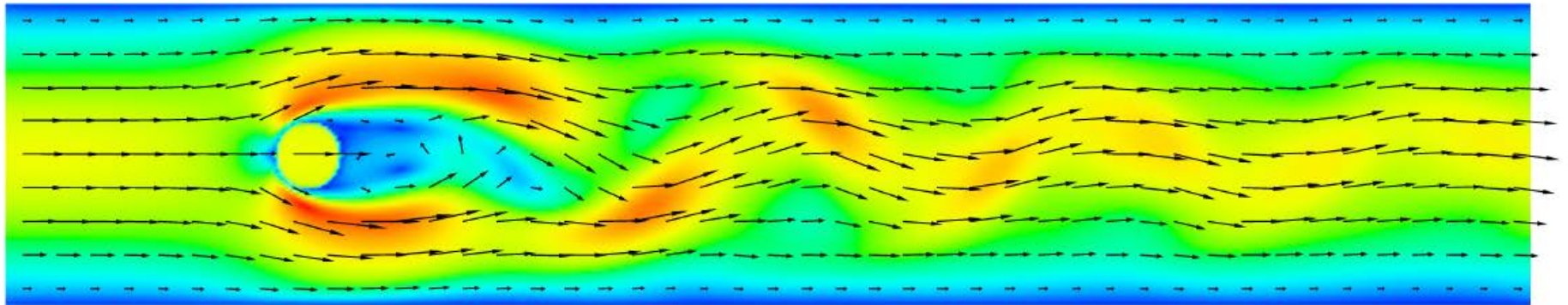
MPI_Sendrcv_replace(
buffer, dst=3, src=7)

recv=buffer



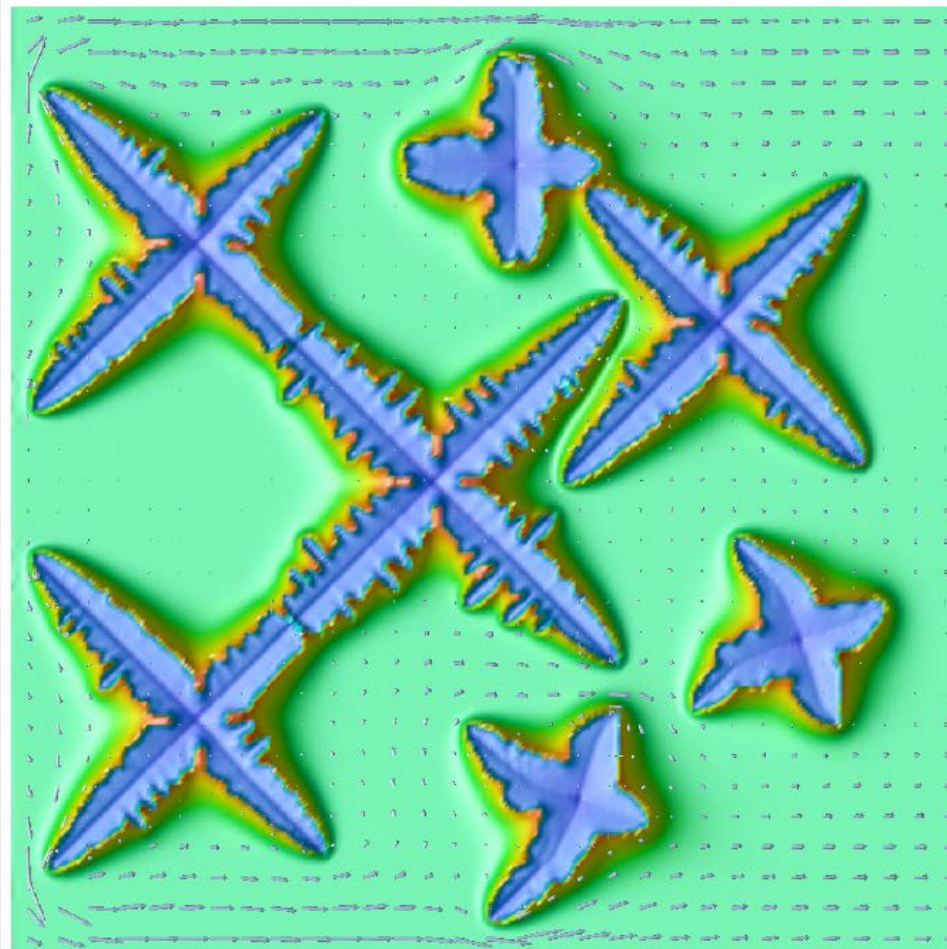
LBM parallelization – streaming

Street flow – example LBM problem:
velocity of flow



LBM parallelization

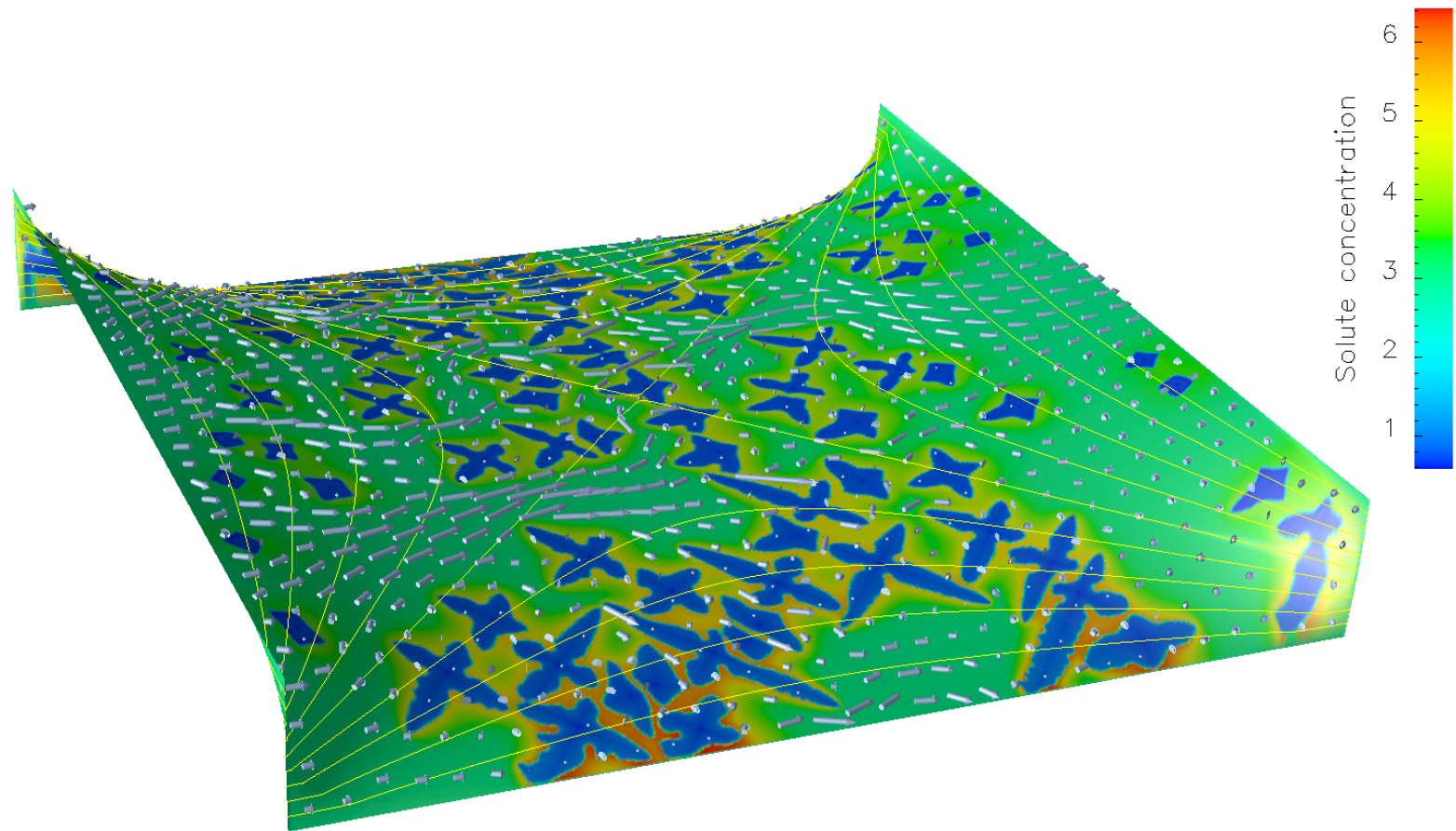
Dendrite growth in AlCu alloy upon cooling:
temperature, velocity of flow, and solute concentration



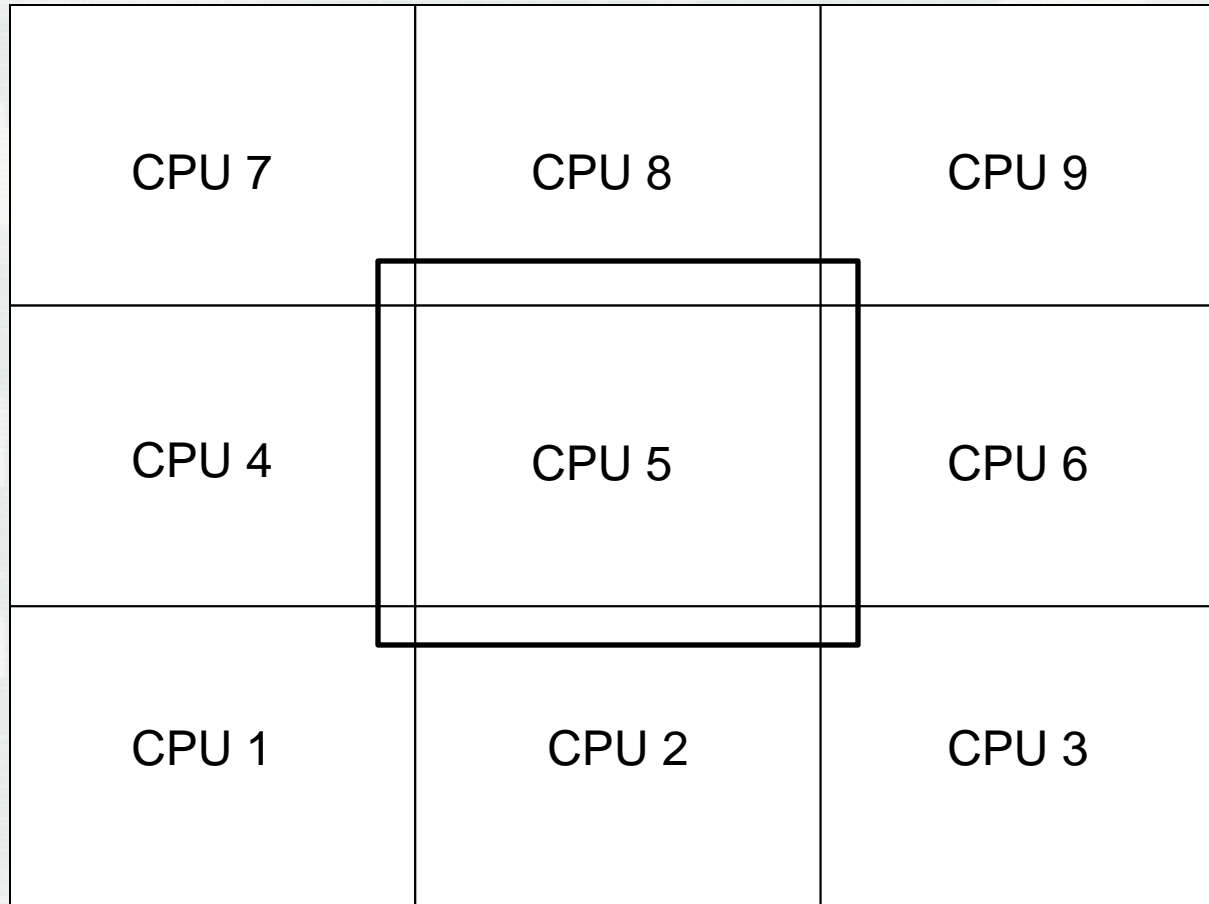
LBM-CA solidification model – C_1 , v , T

Flow of solute between solidifying dendrites in variable temperature field.

Cooled at front and back boundaries, heated from left (inlet) and right (outlet) boundaries.



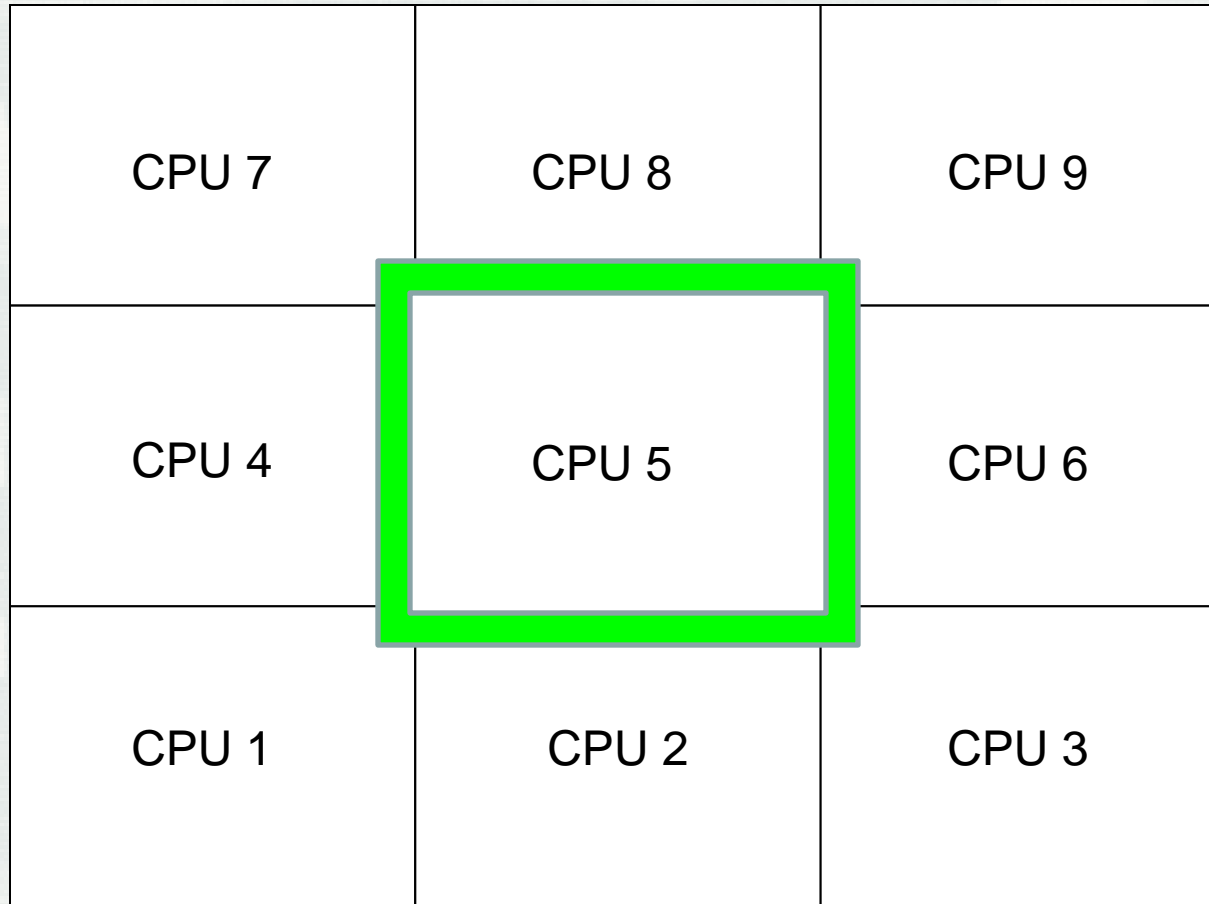
LBM parallelization



For dendrite growth, information from neighboring nodes is needed to update local node value



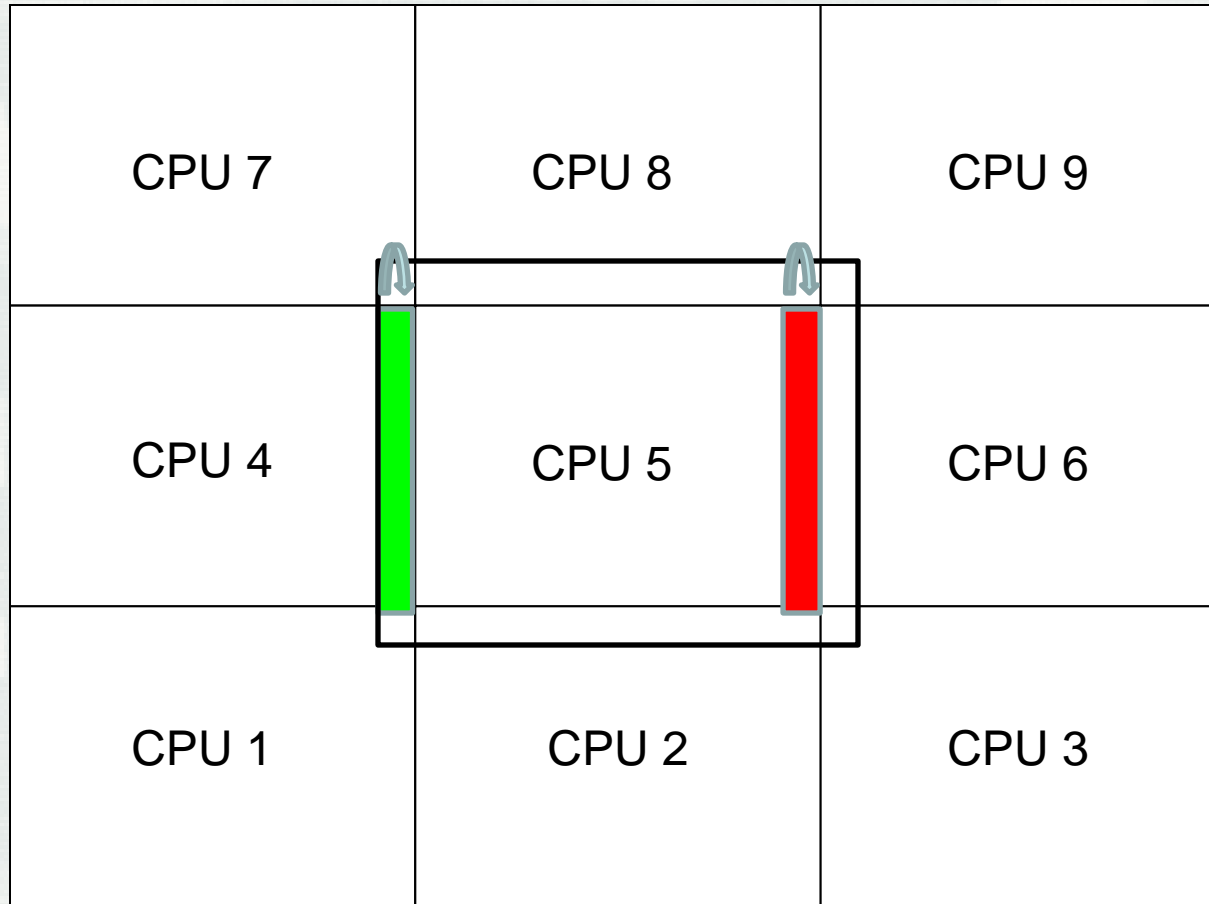
LBM parallelization – ghost nodes



Populate **ghost nodes**
after each local update



LBM parallelization – ghost nodes

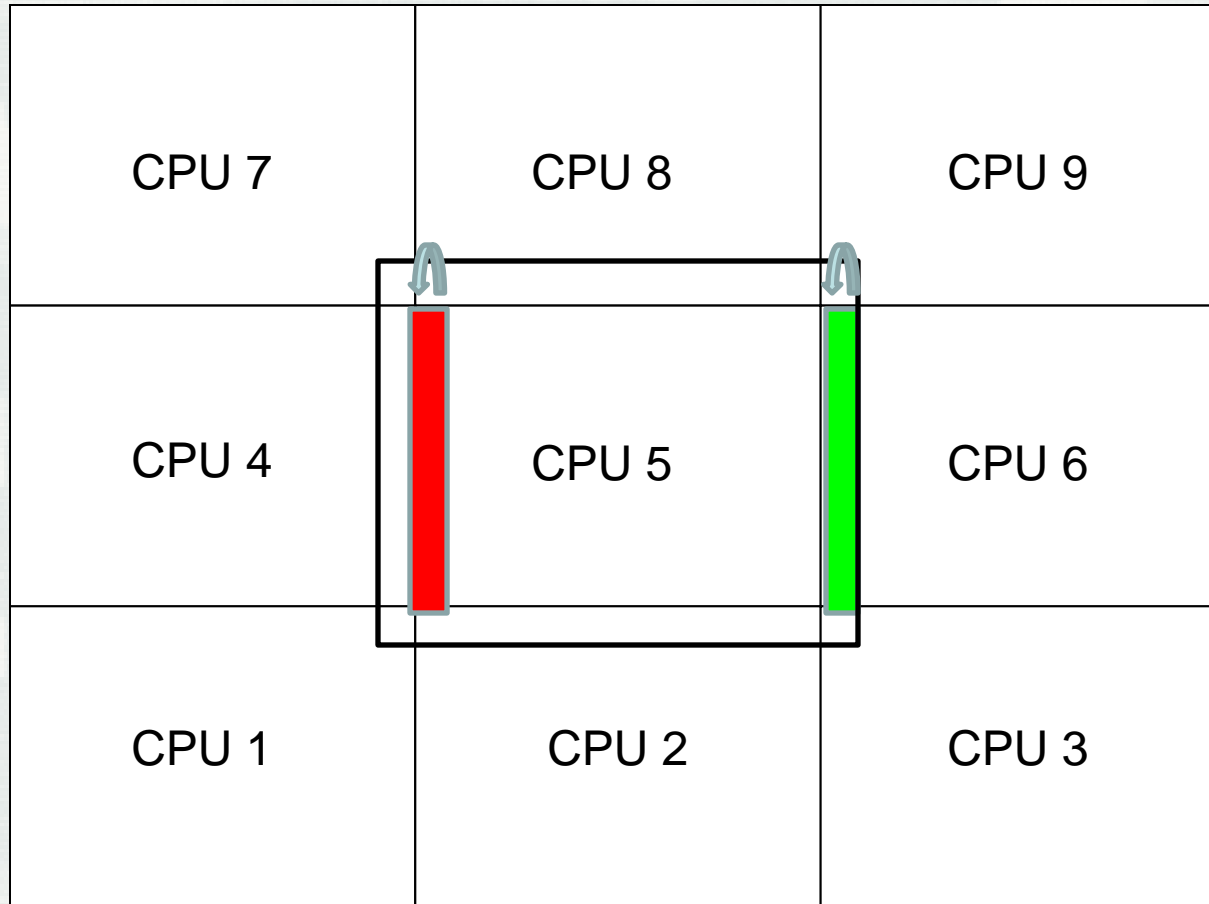


Populate **ghost nodes**
after each local update
east

```
MPI_Sendrcv(  
  send, rcv,  
  dst=6, src=4)
```



LBM parallelization – ghost nodes

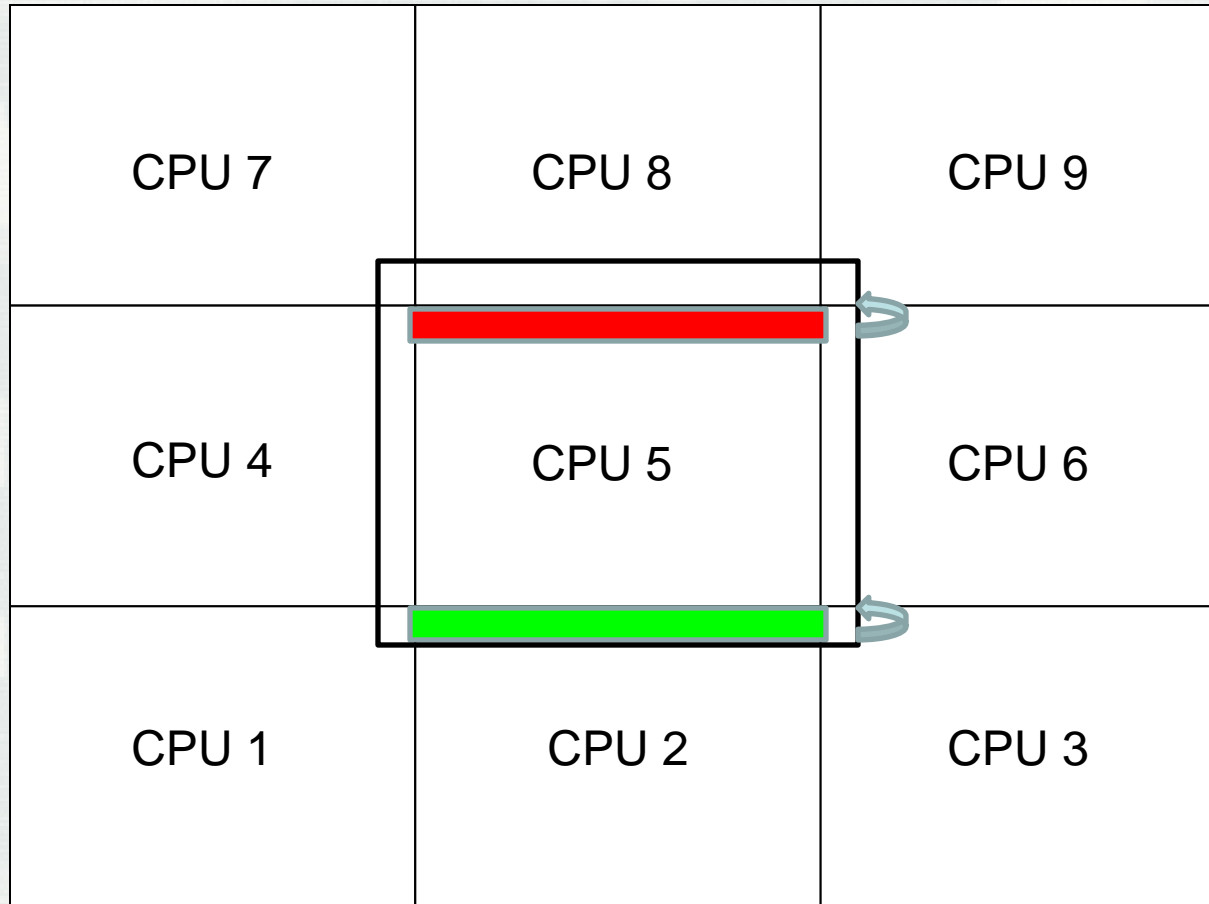


Populate **ghost nodes**
after each local update
west

MPI_Sendrcv(
send, **rcv**,
dst=4, src=6)



LBM parallelization – ghost nodes

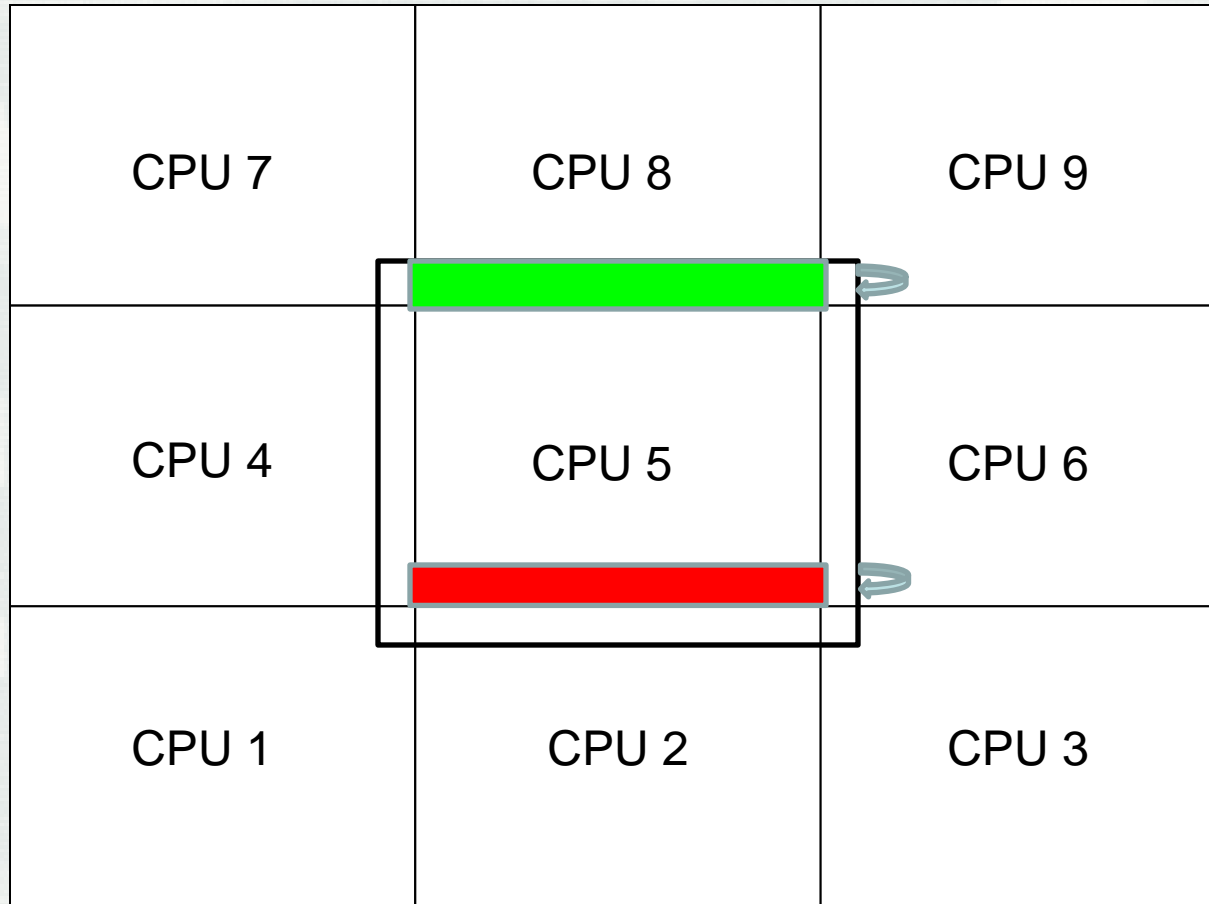


Populate **ghost nodes**
after each local update
north

MPI_Sendrcv(
send, **recv**,
dst=8, src=2)



LBM parallelization – ghost nodes

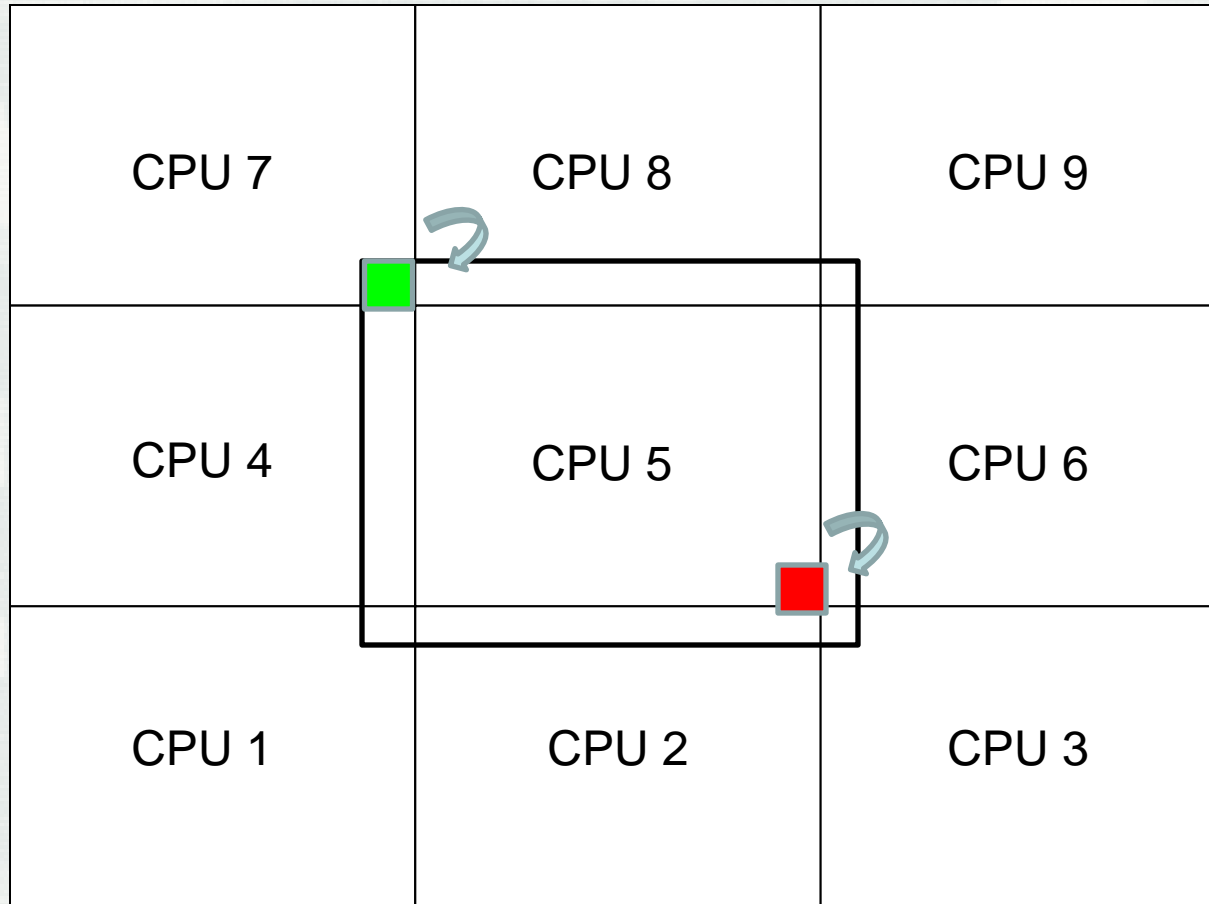


Populate **ghost nodes**
after each local update
south

MPI_Sendrcv(
send, **rcv**,
dst=2, src=8)



LBM parallelization – ghost nodes

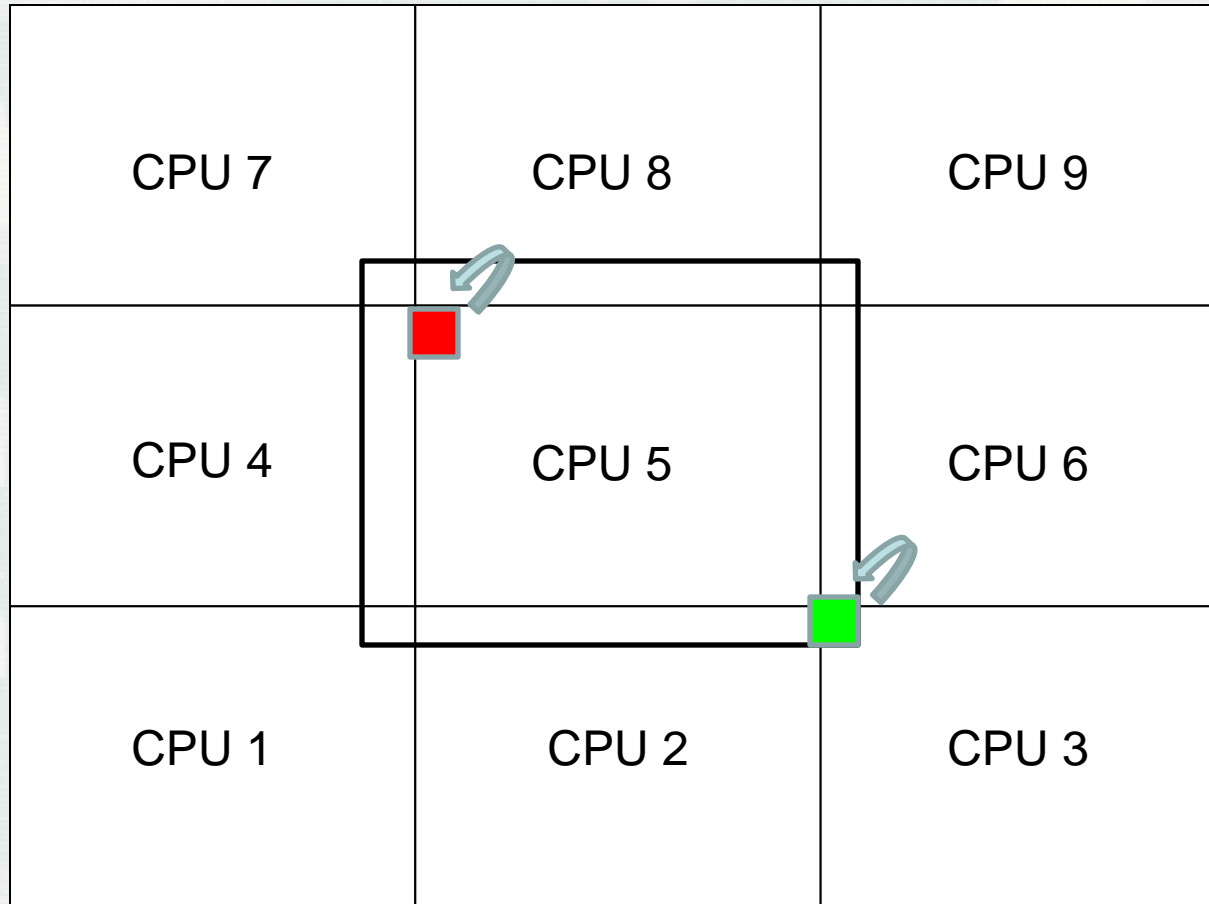


Populate **ghost nodes**
after each local update
south-east

MPI_Sendrcv(
send, **recv**,
dst=3, src=7)



LBM parallelization – ghost nodes

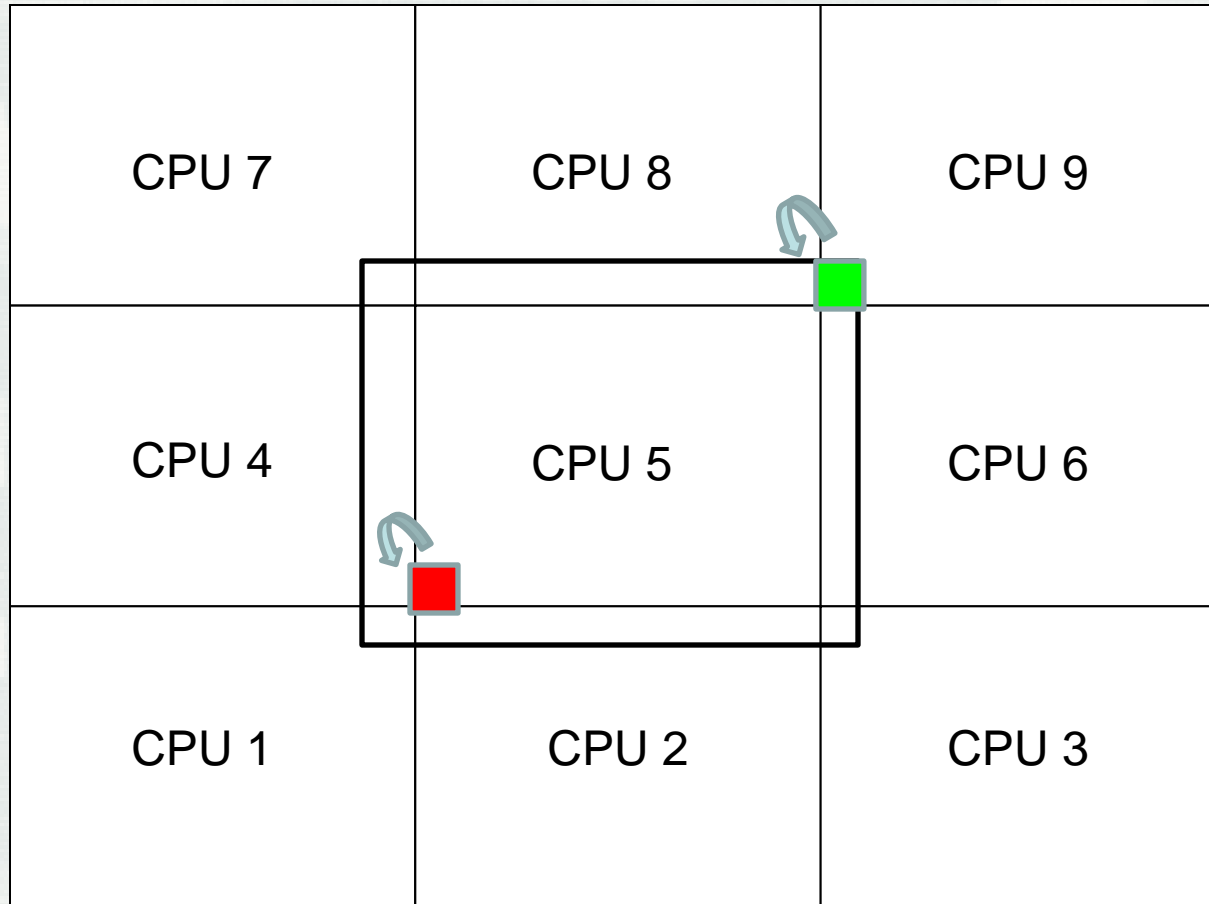


Populate **ghost nodes**
after each local update
north-west

MPI_Sendrcv(
send, **recv**,
dst=7, src=3)



LBM parallelization – ghost nodes

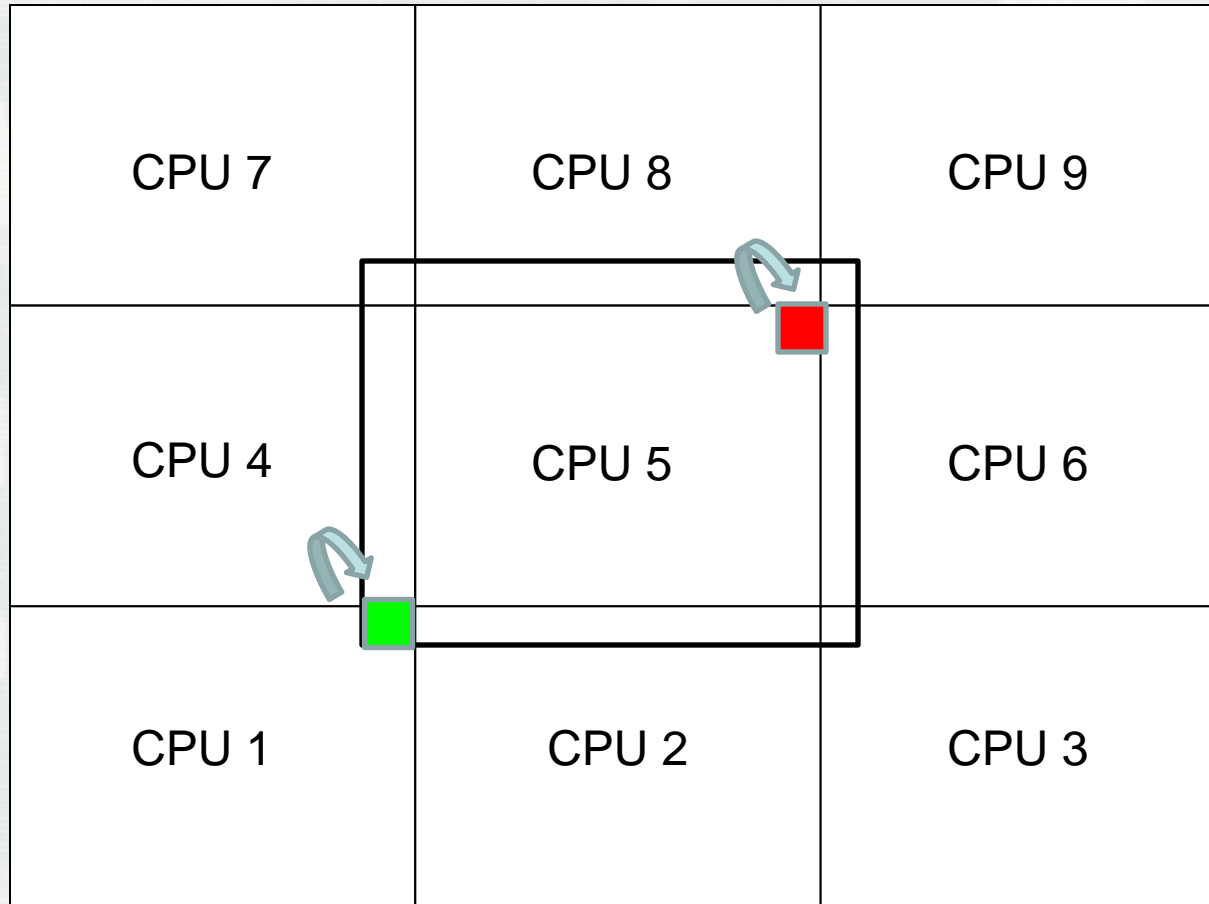


Populate **ghost nodes**
after each local update
south-west

MPI_Sendrcv(
send, **rcv**,
dst=1, src=9)



LBM parallelization – ghost nodes



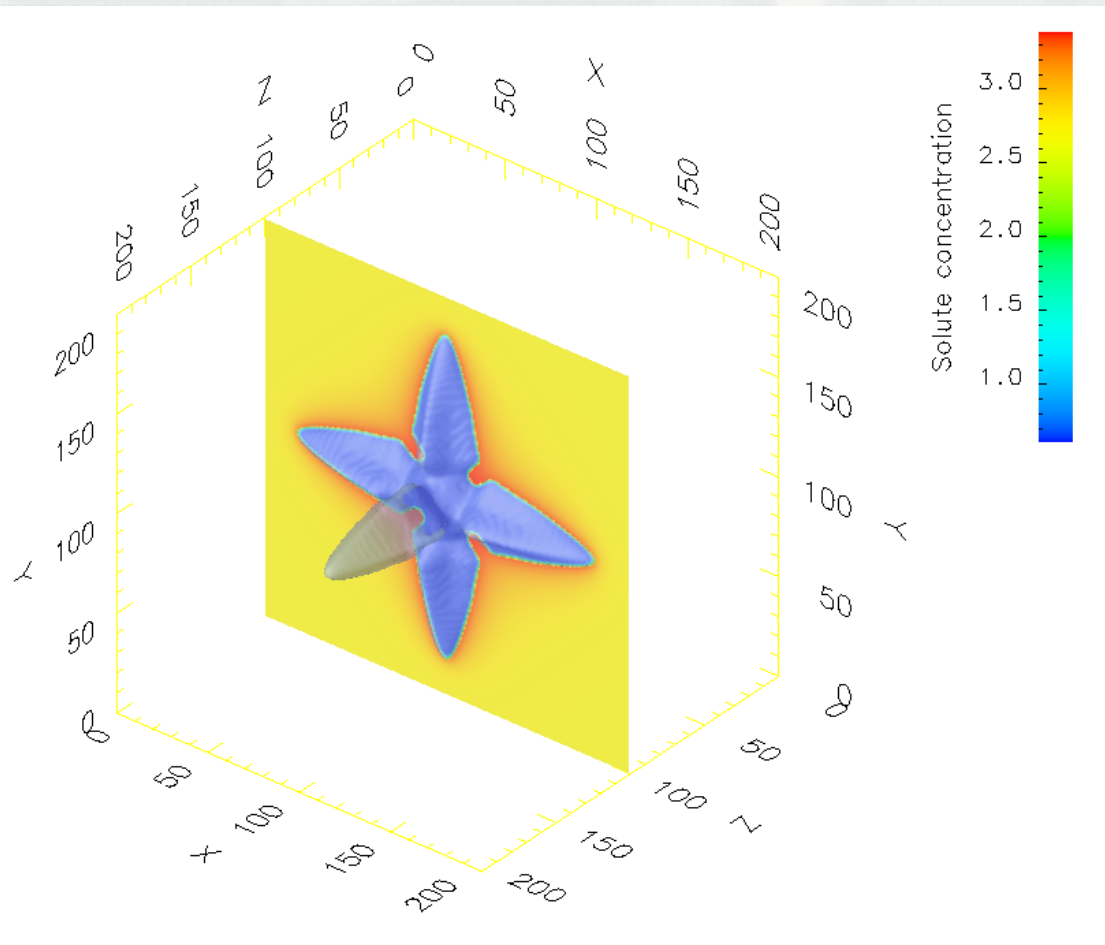
Populate **ghost nodes**
after each local update
north-east

```
MPI_Sendrcv(  
  send, recv,  
  dst=9, src=1)
```



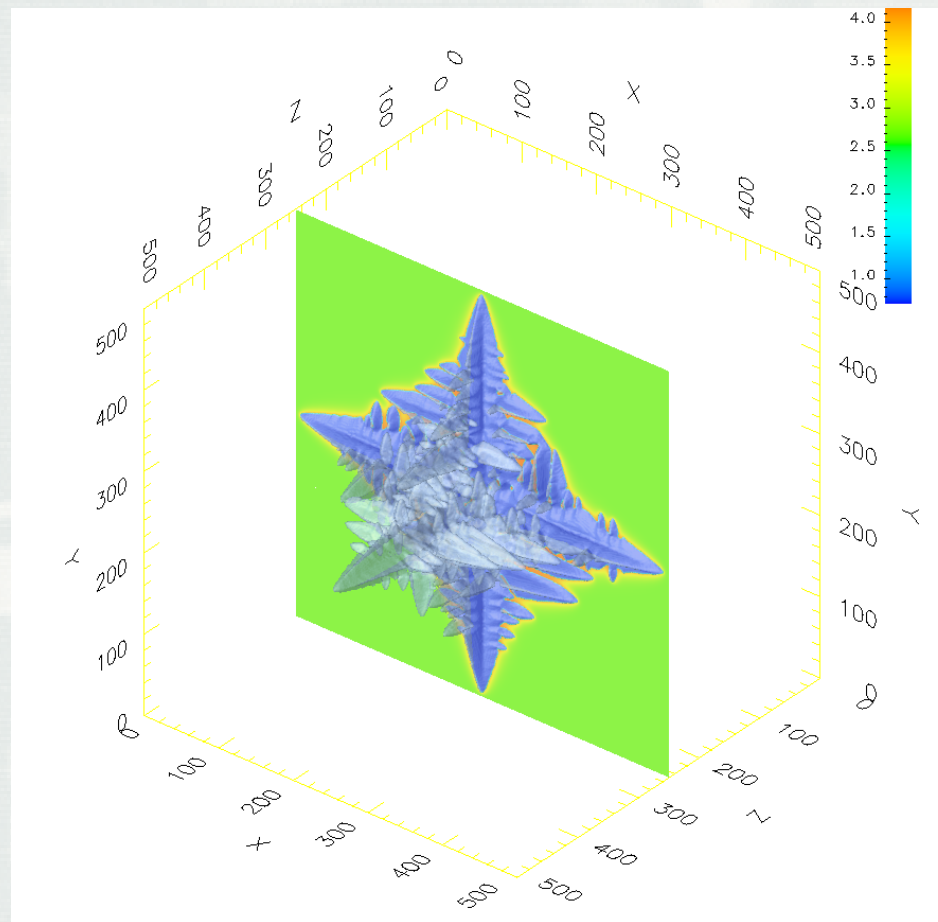
LBM parallelization

3D Dendrite growth in AlCu alloy upon cooling:
temperature, fluid flow, and solute concentration



LBM parallelization

3D Dendrite growth in AlCu alloy upon cooling:
temperature, fluid flow, and solute concentration



simulation by Mohsen Eshraghi

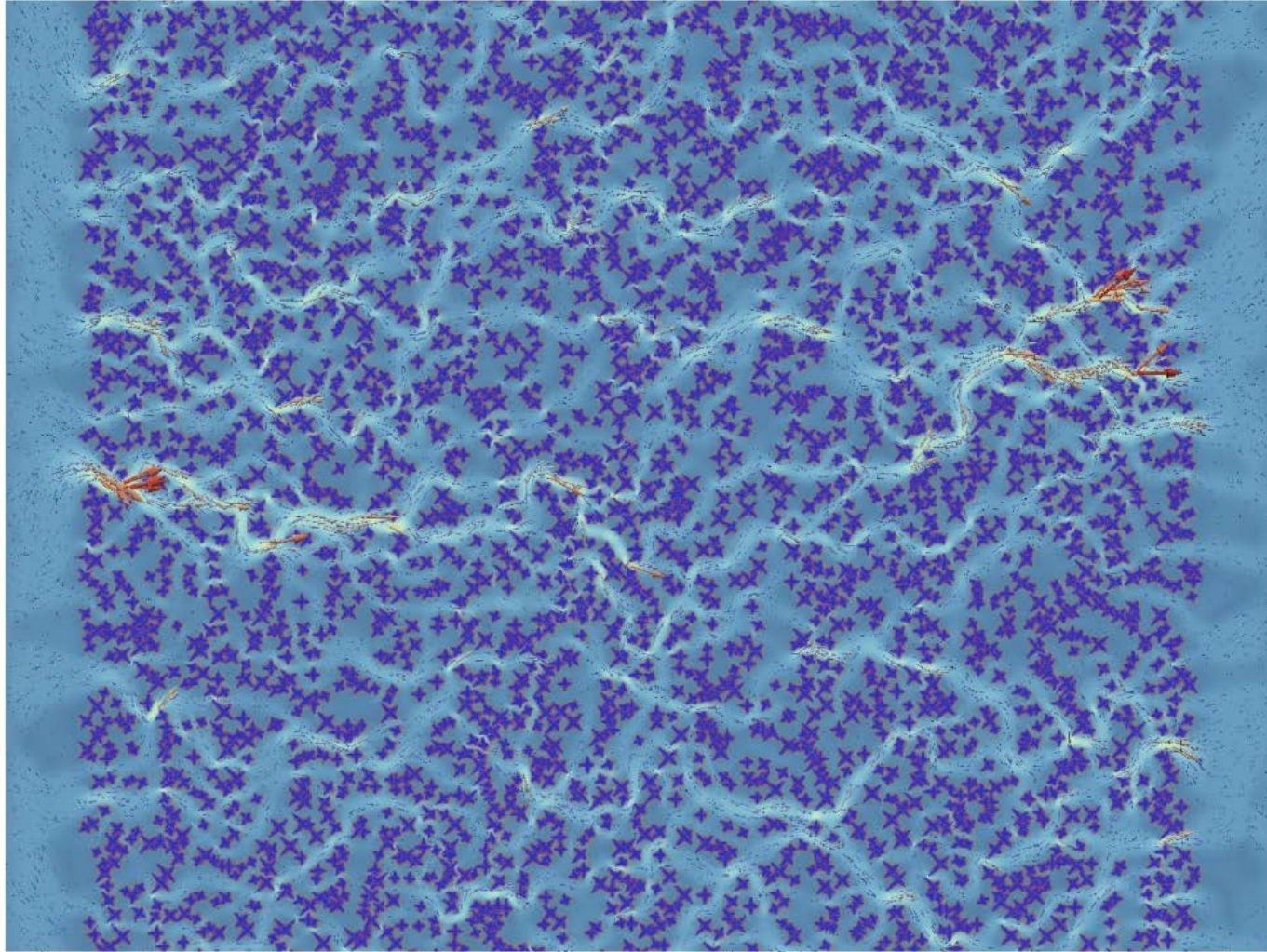


Generating an initial configuration for parallel scaling tests

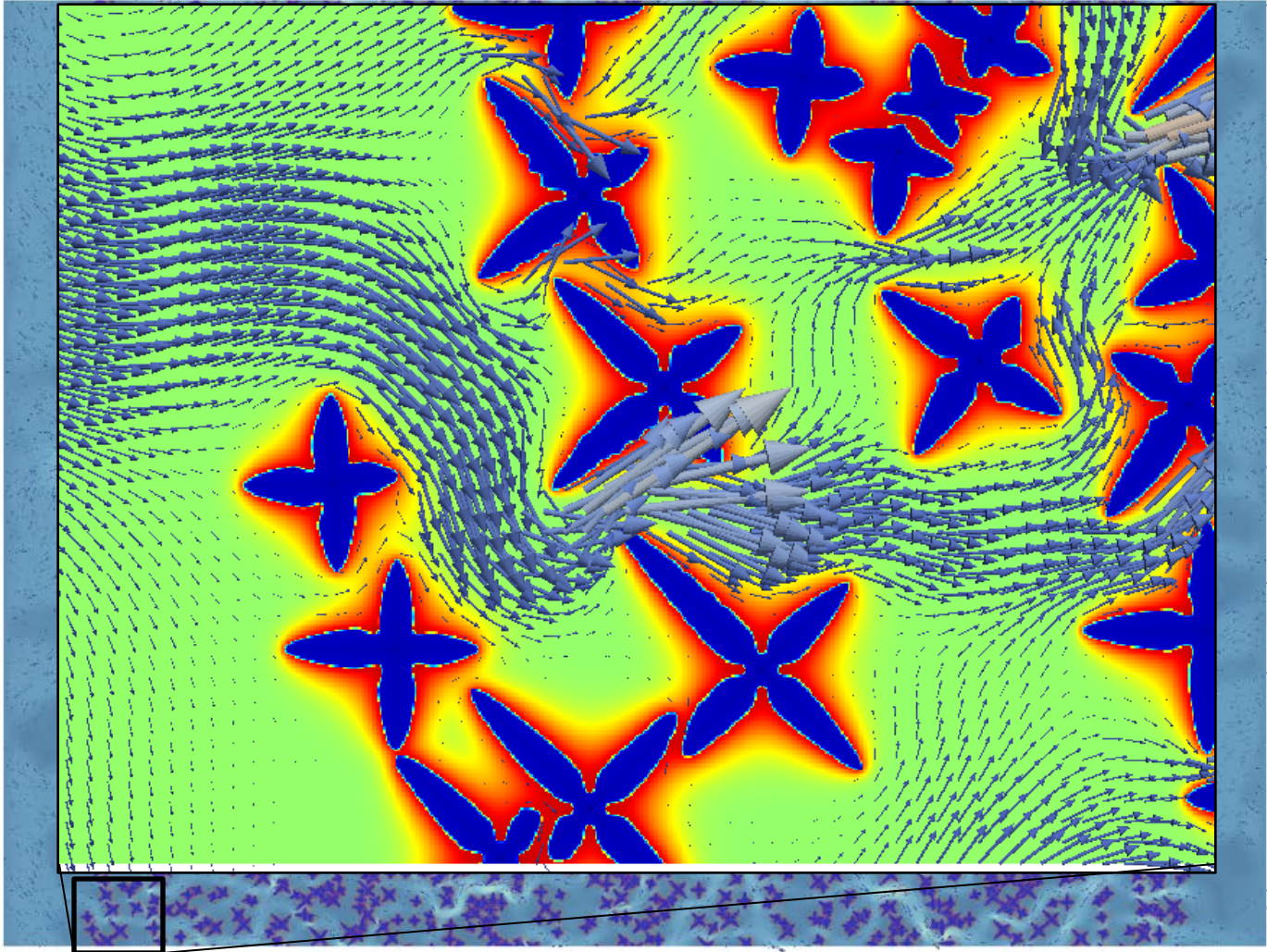
Simulation domain:

- rectangular lattice, 8000x6000 grid points
- dimensions: 2.4 mm x 1.8 mm (0.3 μm /lattice distance)
- 3264 random dendrite nucleation sites
- constant cooling rate 100K/s across the whole domain
- forced melt flow through inlet (left) and outlet (right) boundaries
- almost 16 GB of memory = single node of Kraken
- 400k time steps
- took about 10 hours on 192 cores on Talon @ MSU

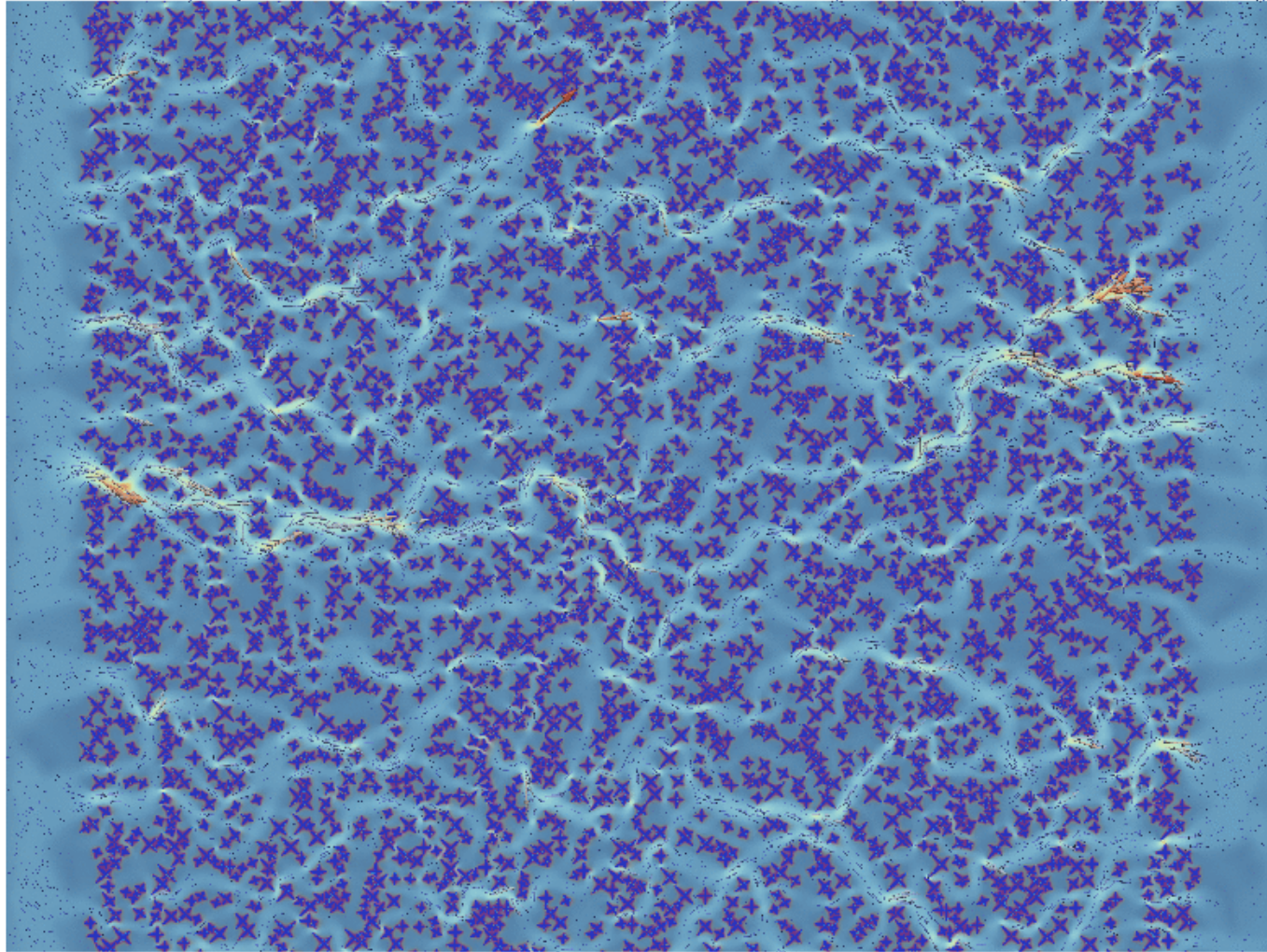
Initial configuration



Magnified portion of initial configuration



Growing dendrites to initial configuration



Generating an initial configuration for parallel scaling tests

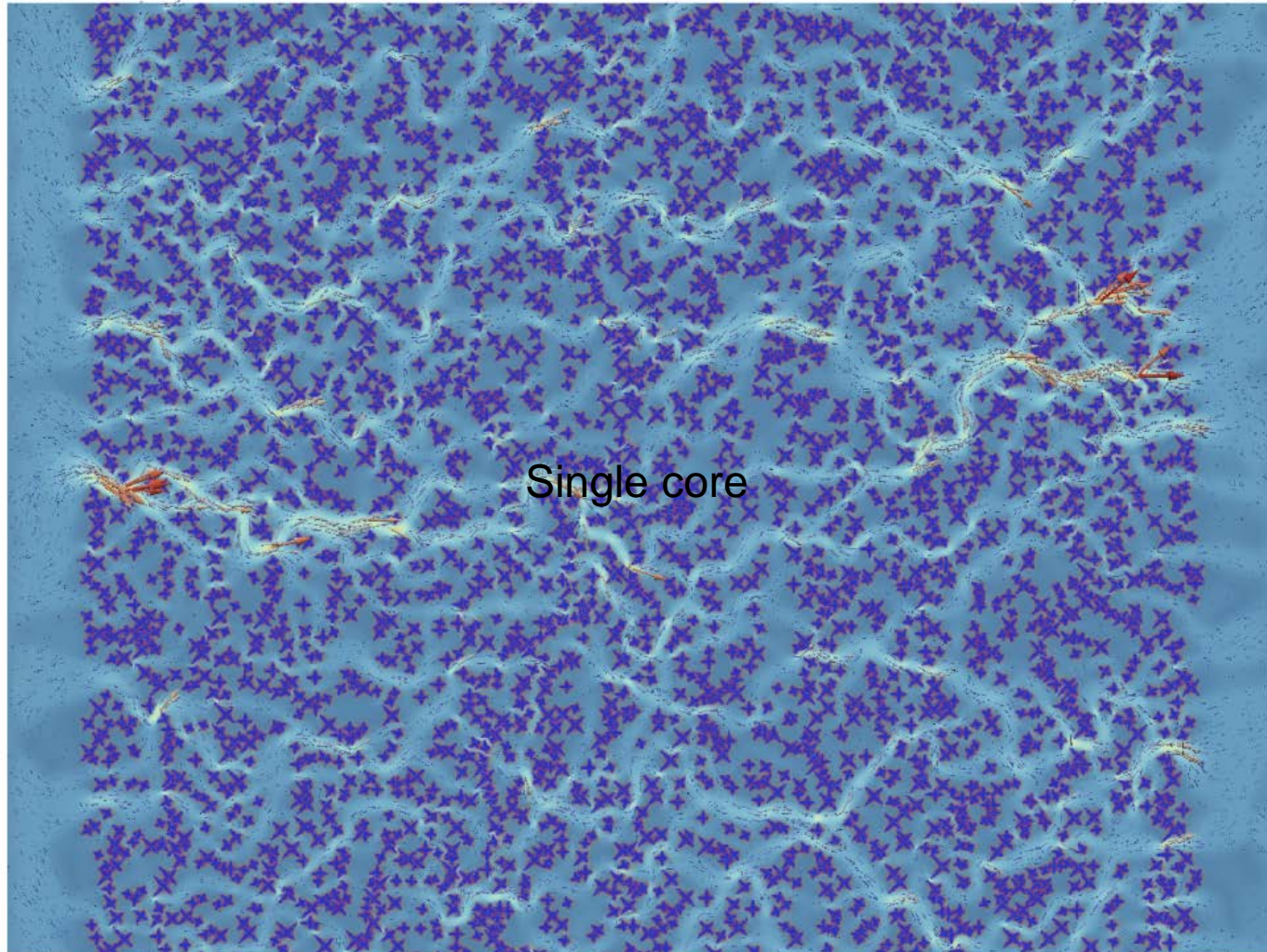
Simulation domain:

- rectangular lattice, 8000x6000 grid points
- dimensions: 2.4 mm x 1.8 mm (0.3 μm /lattice distance)
- 3264 random dendrite nucleation sites
- constant cooling rate 100K/s across the whole domain
- forced melt flow through inlet (left) and outlet (right) boundaries
- almost 16 GB of memory = single node of Kraken
- 400k time steps
- took about 10 hours on 192 cores on Talon @ MSU

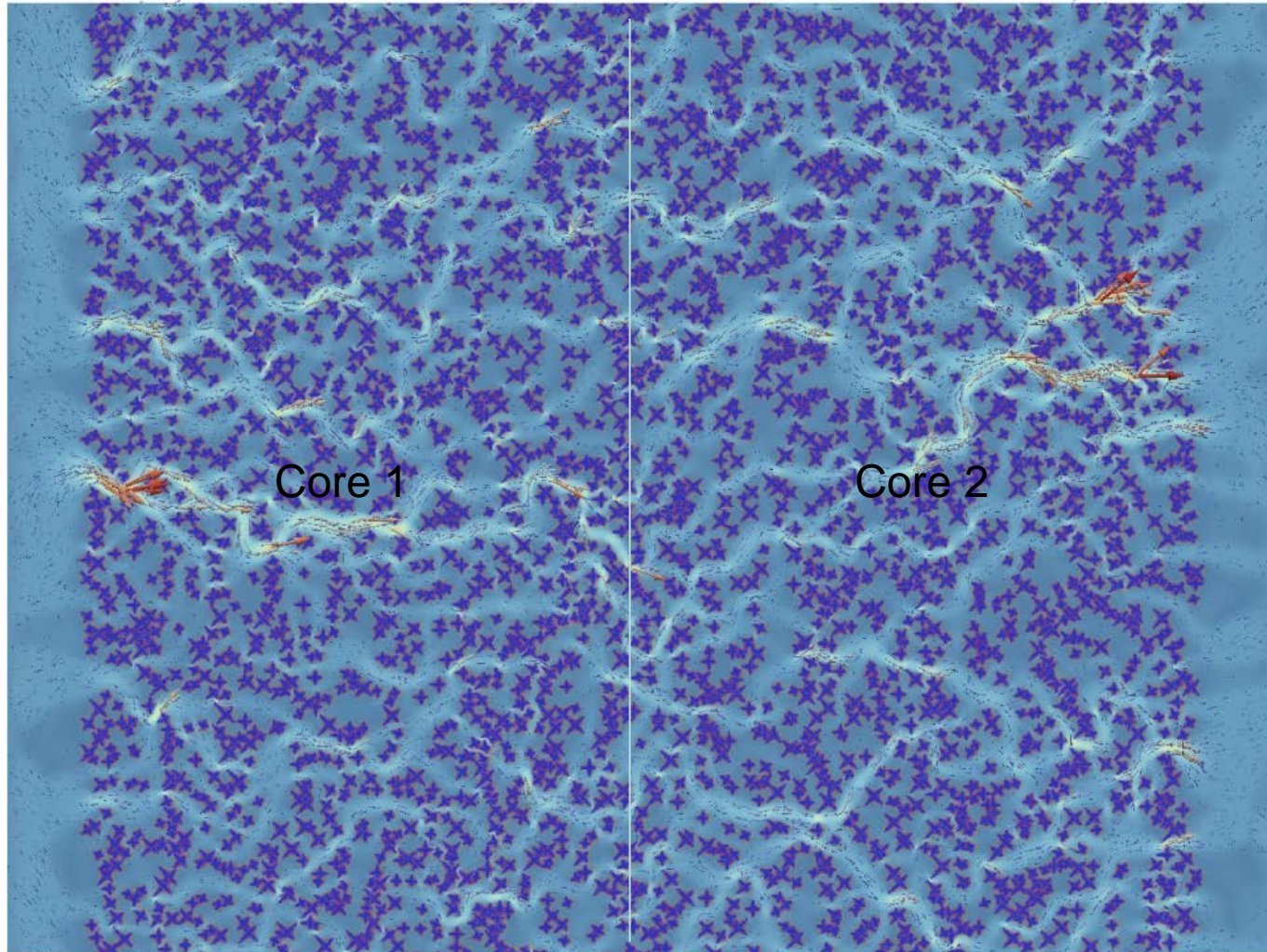
Speed up

- Speed up (strong scaling) represents how much faster a task is solved utilizing multiple cores
- Speed up tests were performed by restarting simulation from the step when the dendrites were fairly grown in the incubation domain
- Incubation domain is “split” equally between varying number of cores, then executed for 587 time steps with a flow forced at the inlet (left) and outlet (right), and with a specified cooling flow rate at all boundaries

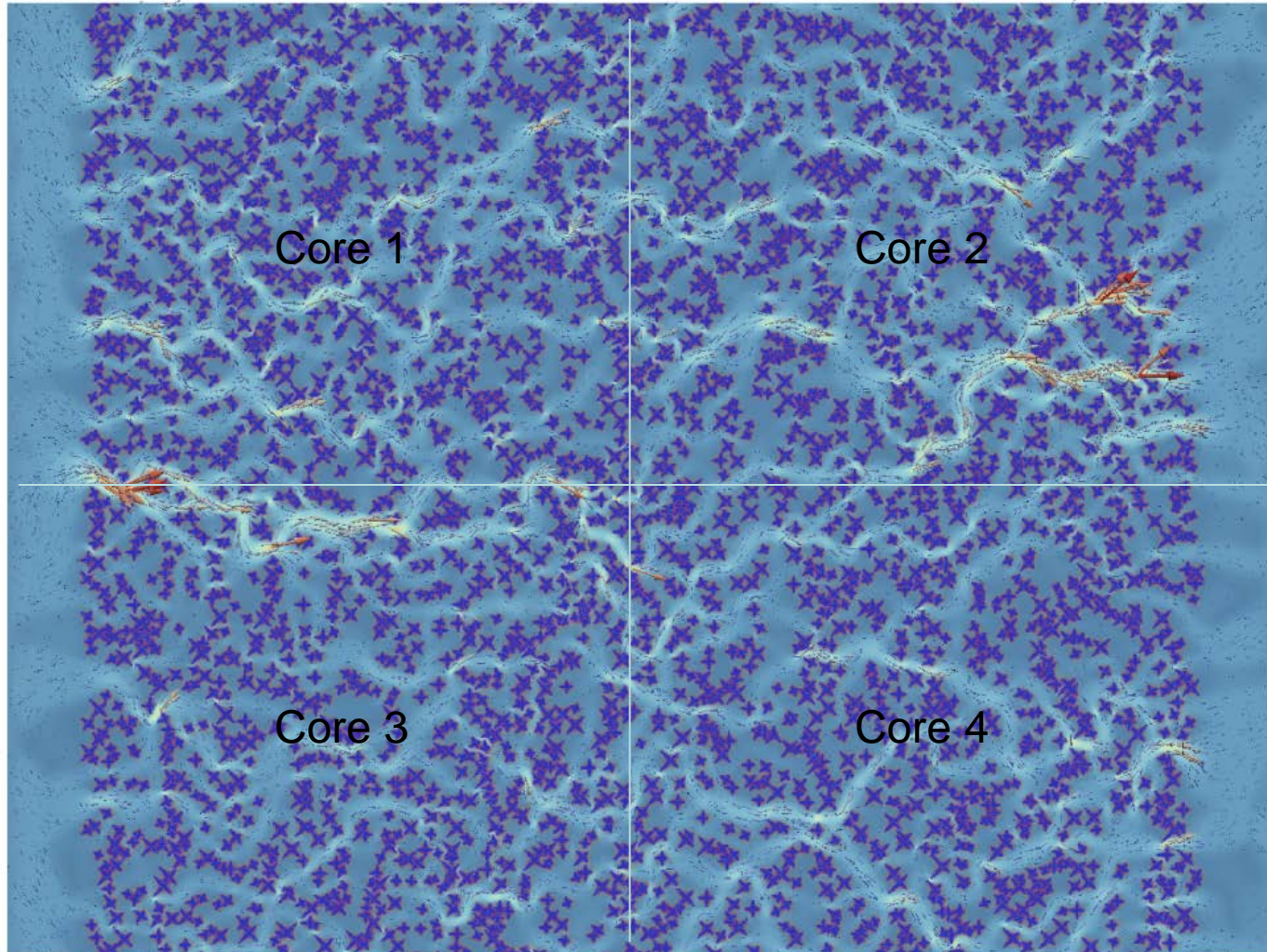
Speed up - constant task, 1 core



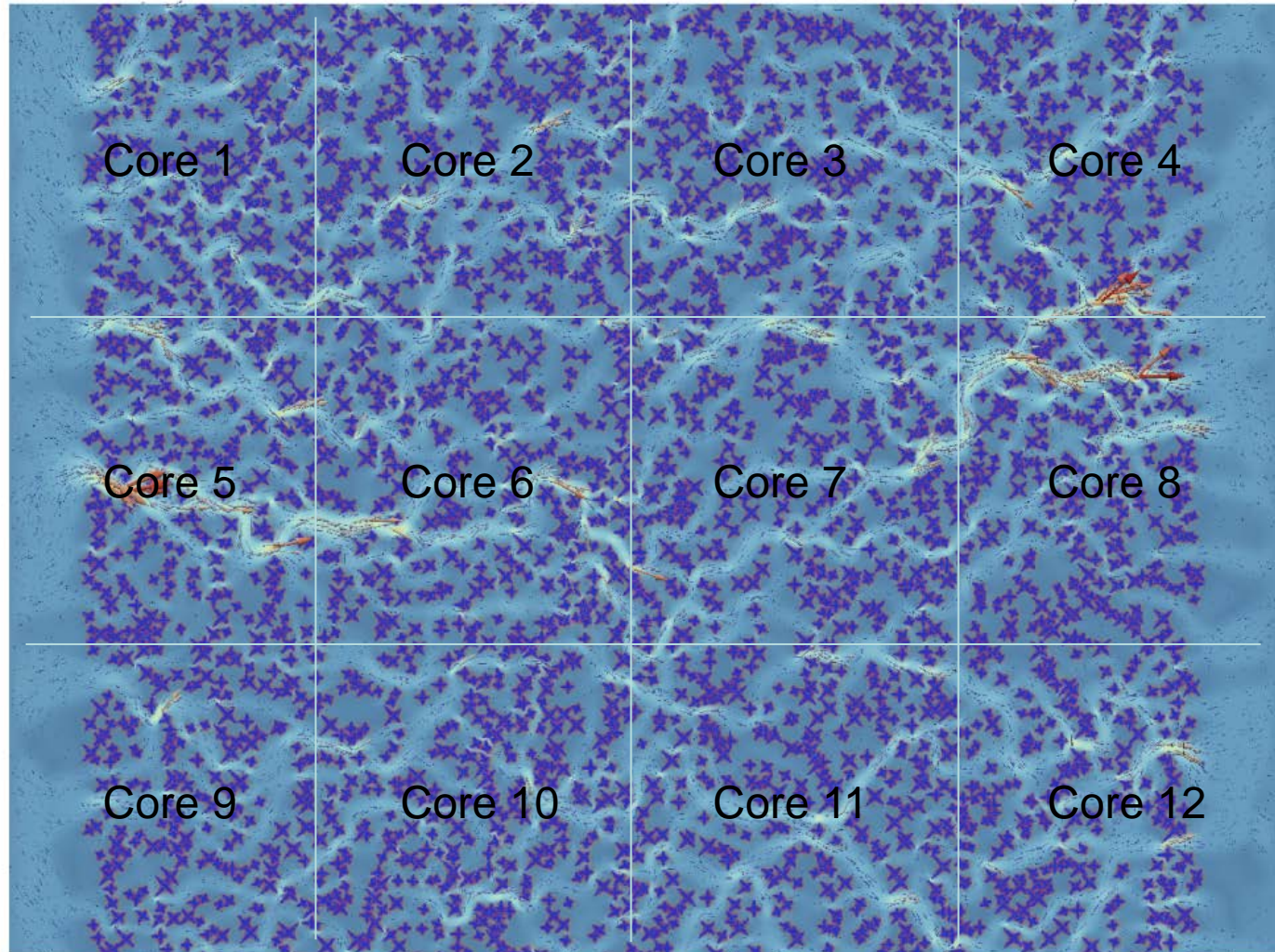
Speed up - constant task, 2 cores



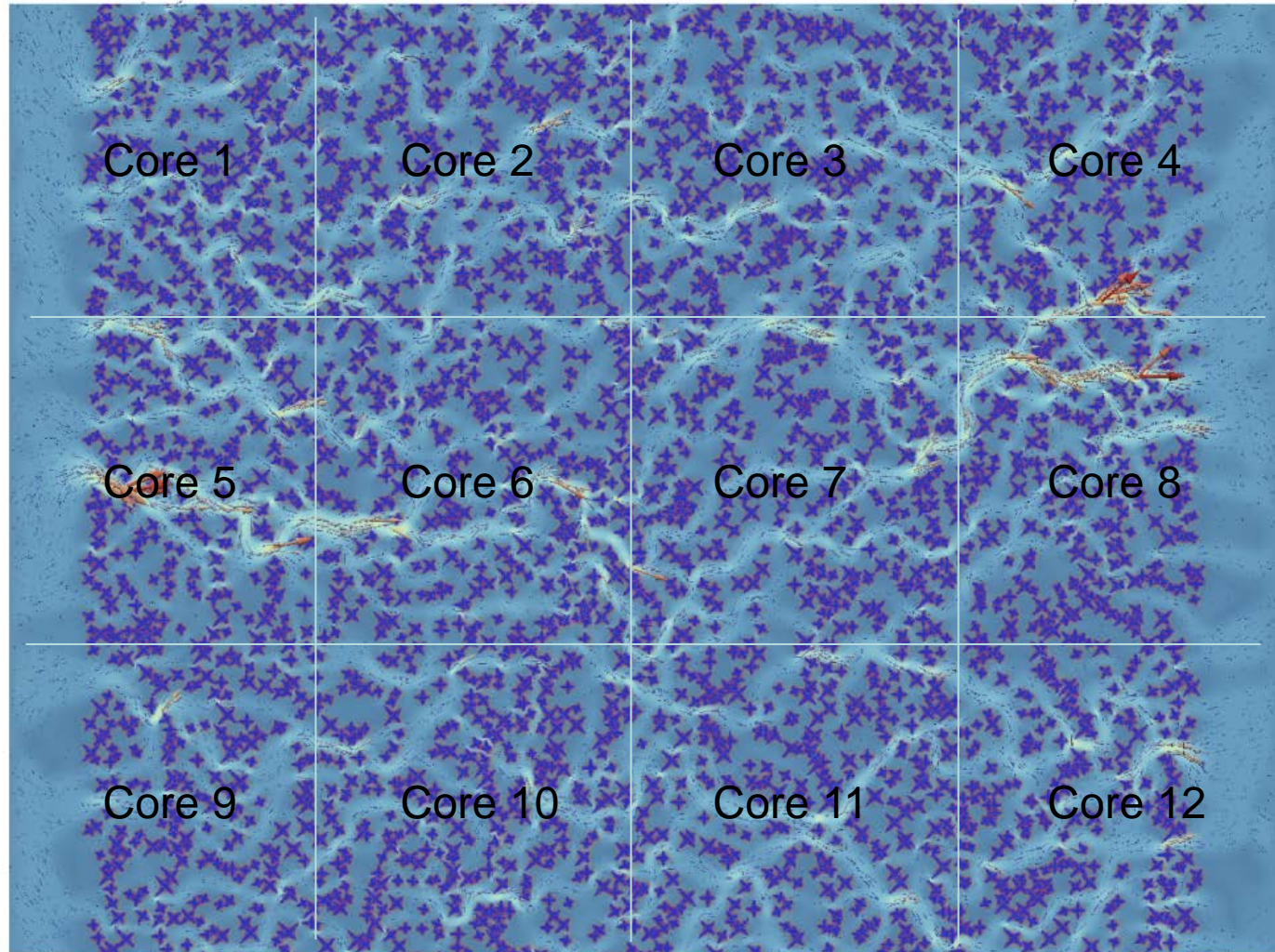
Speed up - constant task, 4 cores



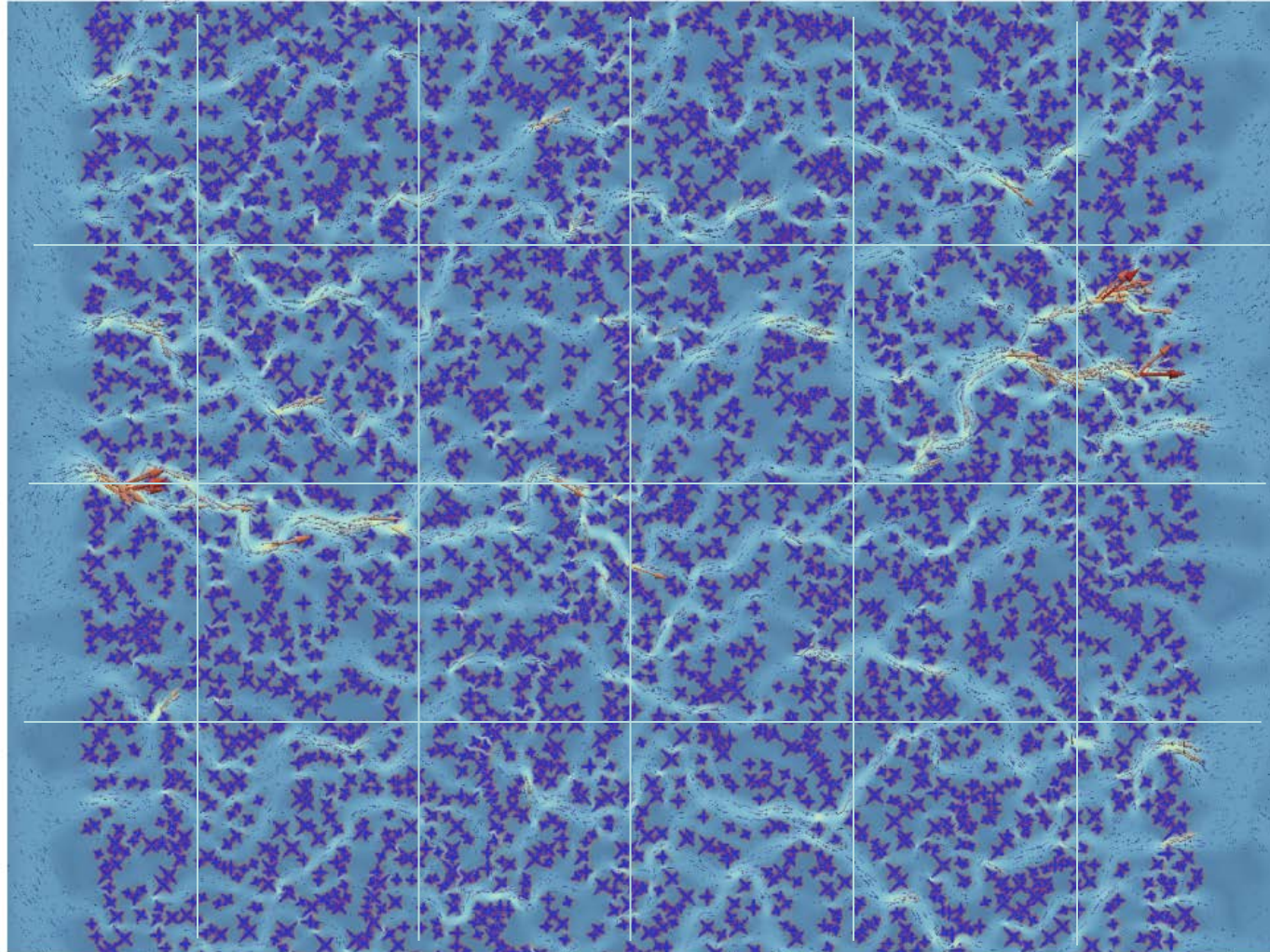
Speed up - constant task, 12 cores



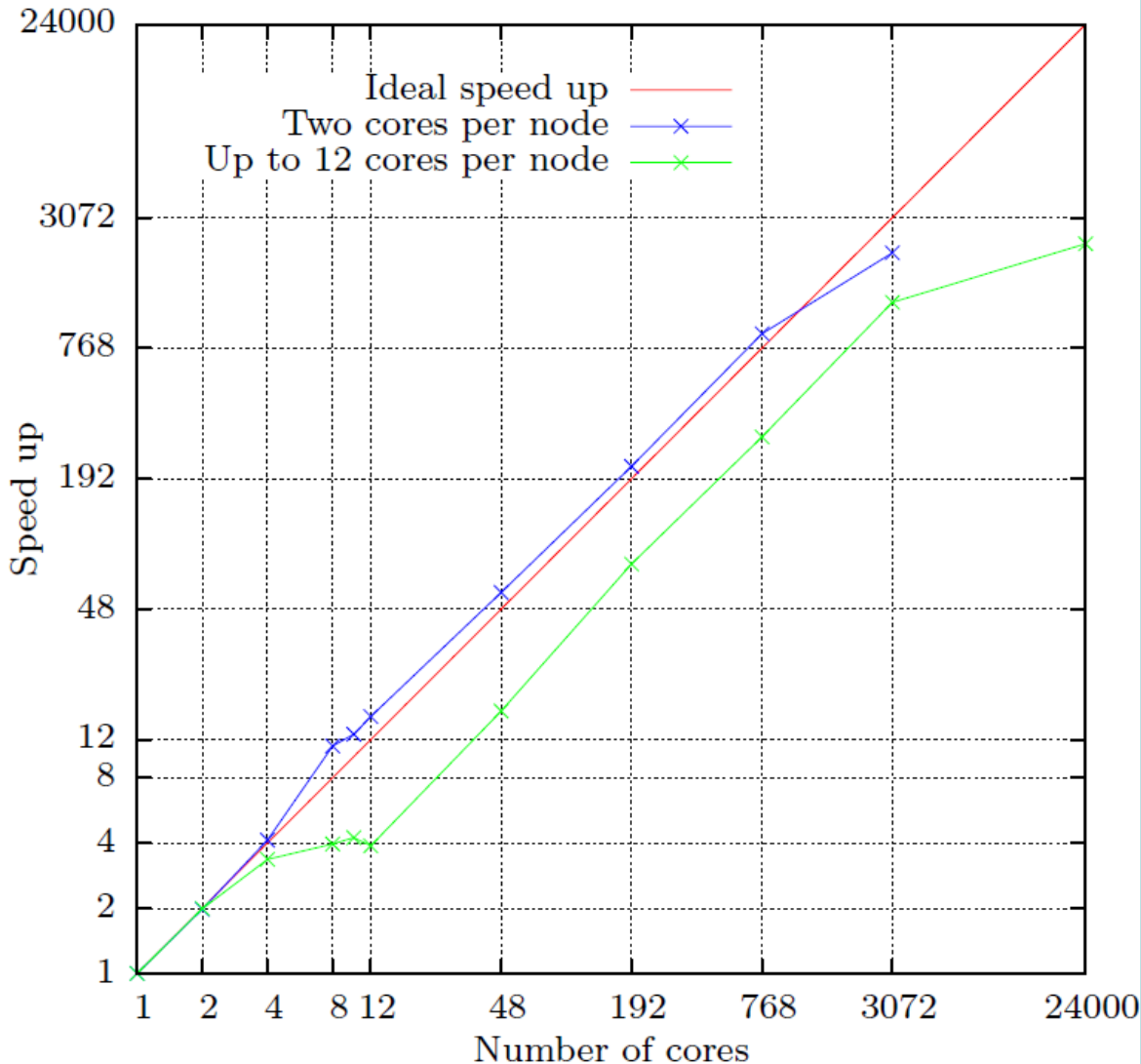
Speed up - constant task, 12 cores



Speed up - constant task, 24 cores



Speed up - results



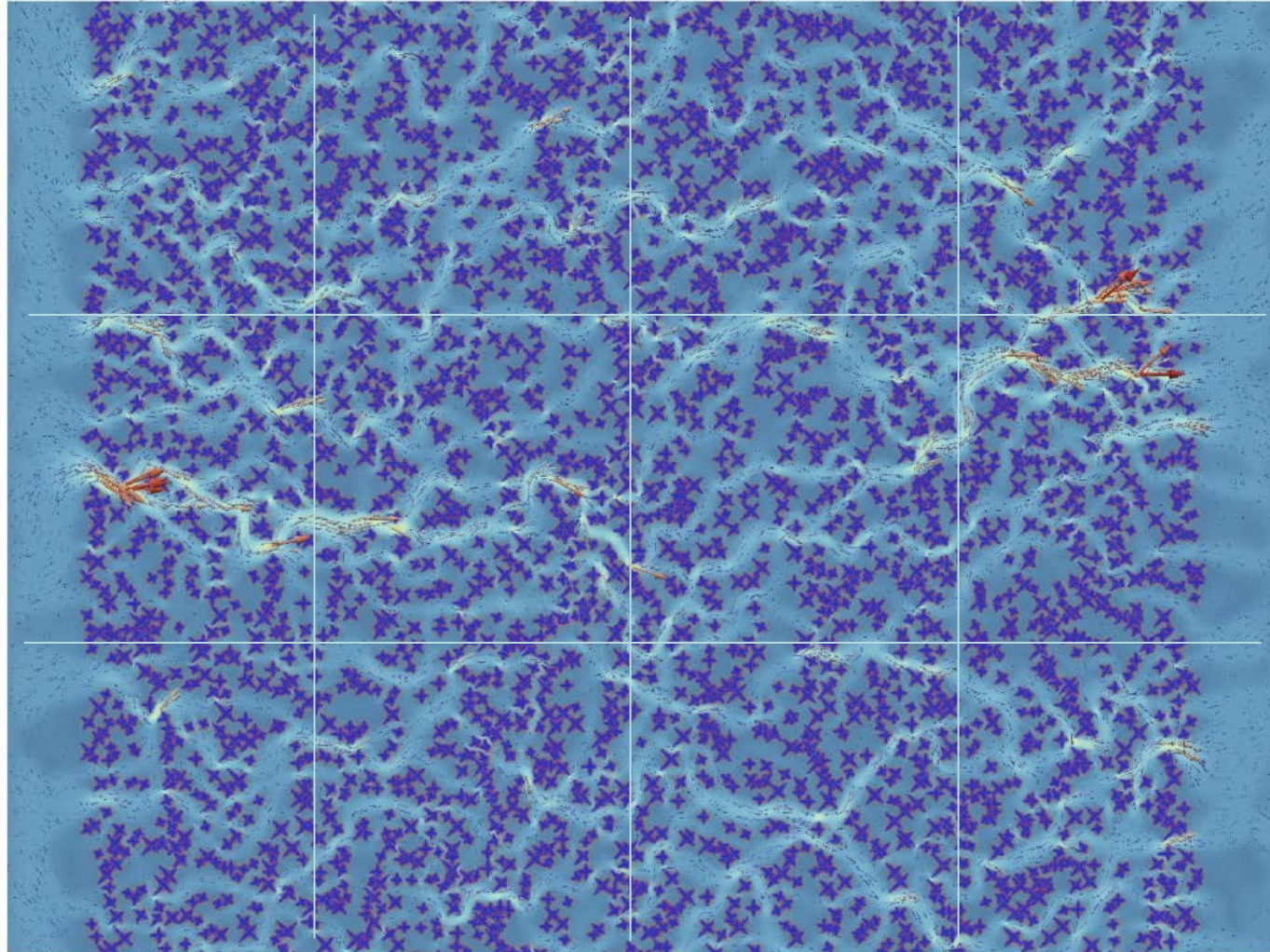
- strong scaling (speed up) near perfect up to 3072 cores
- Algorithm is memory bandwidth limited on multi-core architecture (low FLOP/byte ratio)



Scale up

- Scale up (weak scaling) tests checks if the algorithm can solve larger task when more cores are utilized without a significant performance penalty
- Scale up tests were initialized from the stage when the dendrites were fairly grown in the incubation domain
- Incubated domain was “duplicated” equally onto varying number of nodes, then executed for 587 time steps with a flow forced at the inlet (left) and outlet (right), and with a specified cooling flow rate at all boundaries

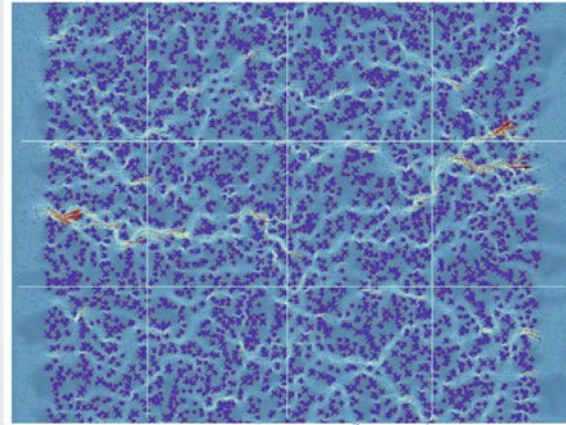
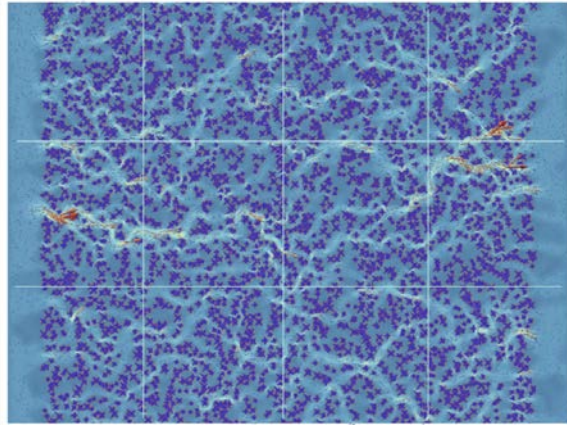
Scale up - constant domain per node



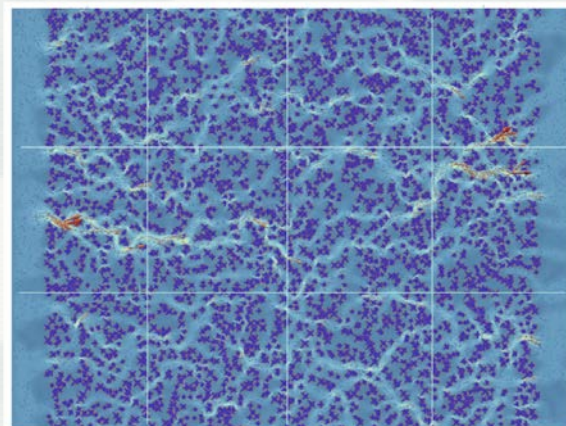
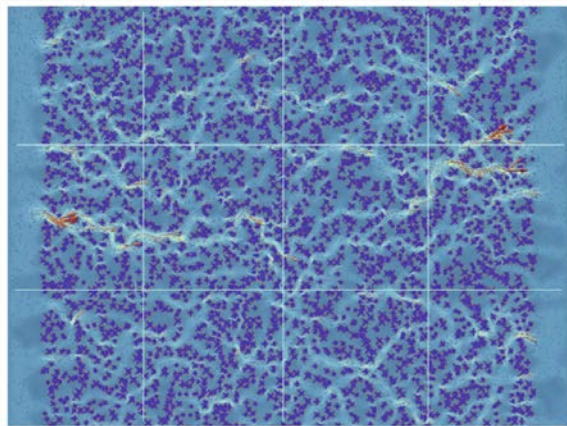
Base domain



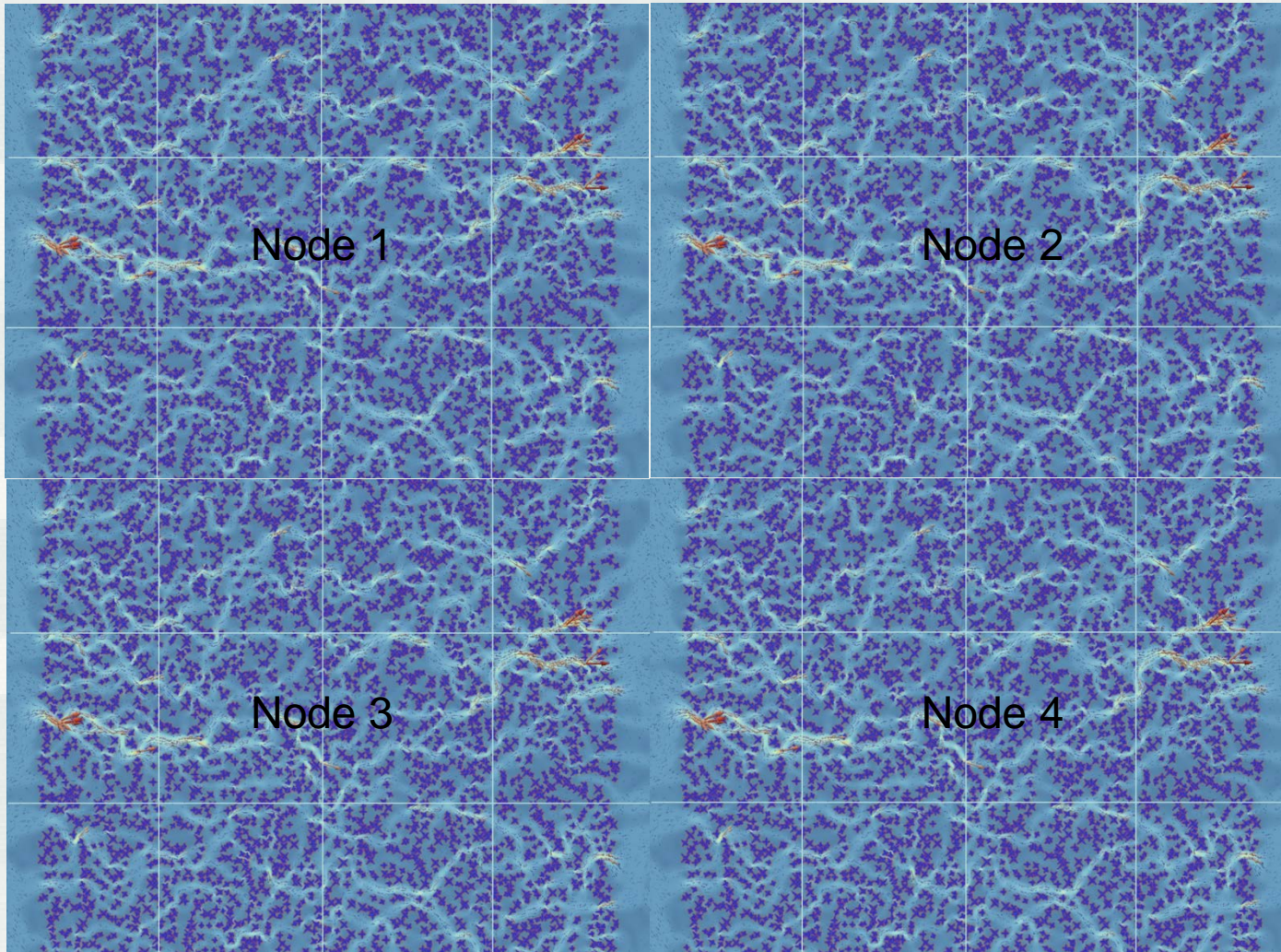
Scale up - constant domain per node



Duplication of the incubation domain onto 4 nodes



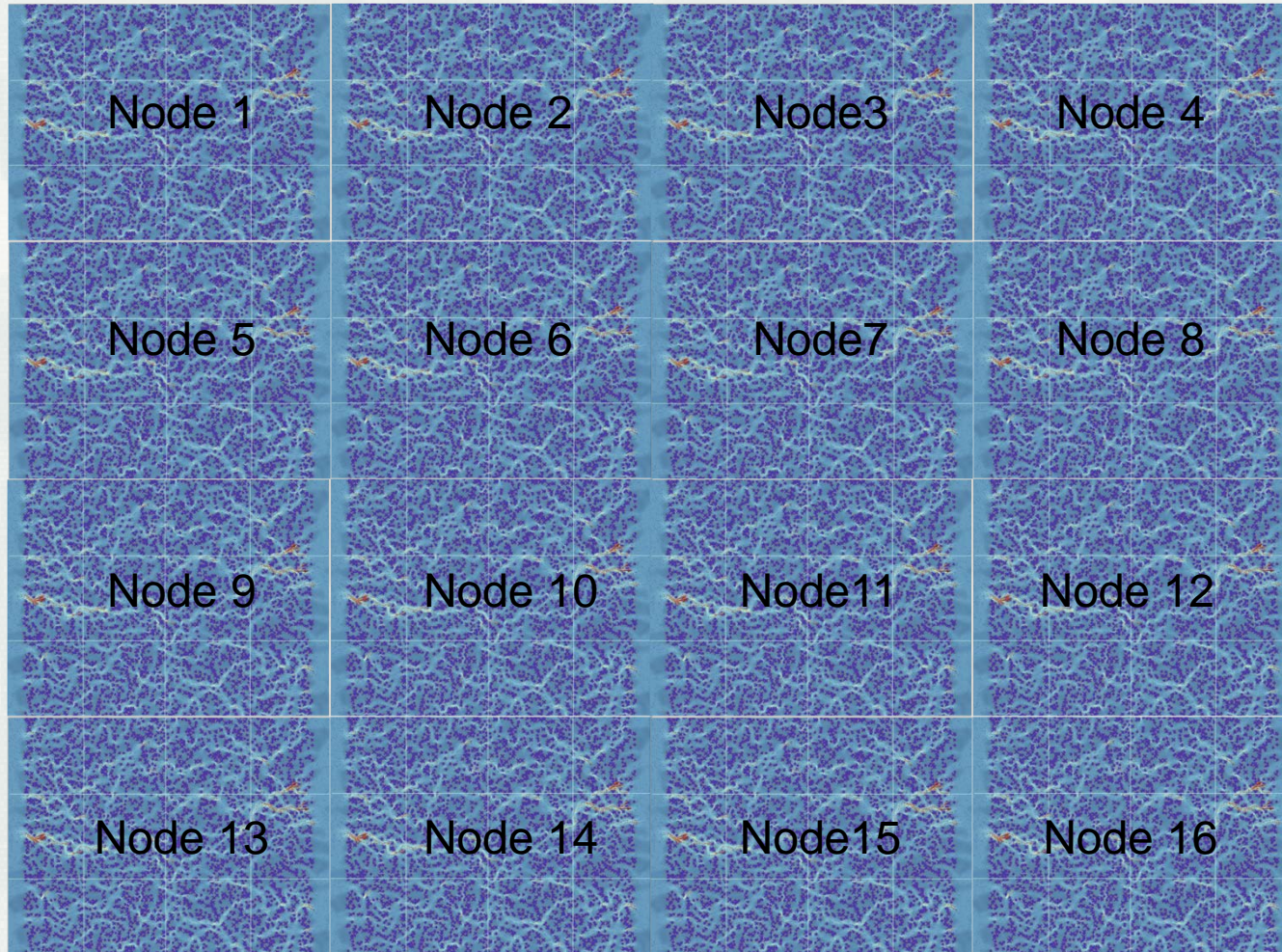
Scale up - constant domain per node



Duplication of the incubation domain onto 4 nodes



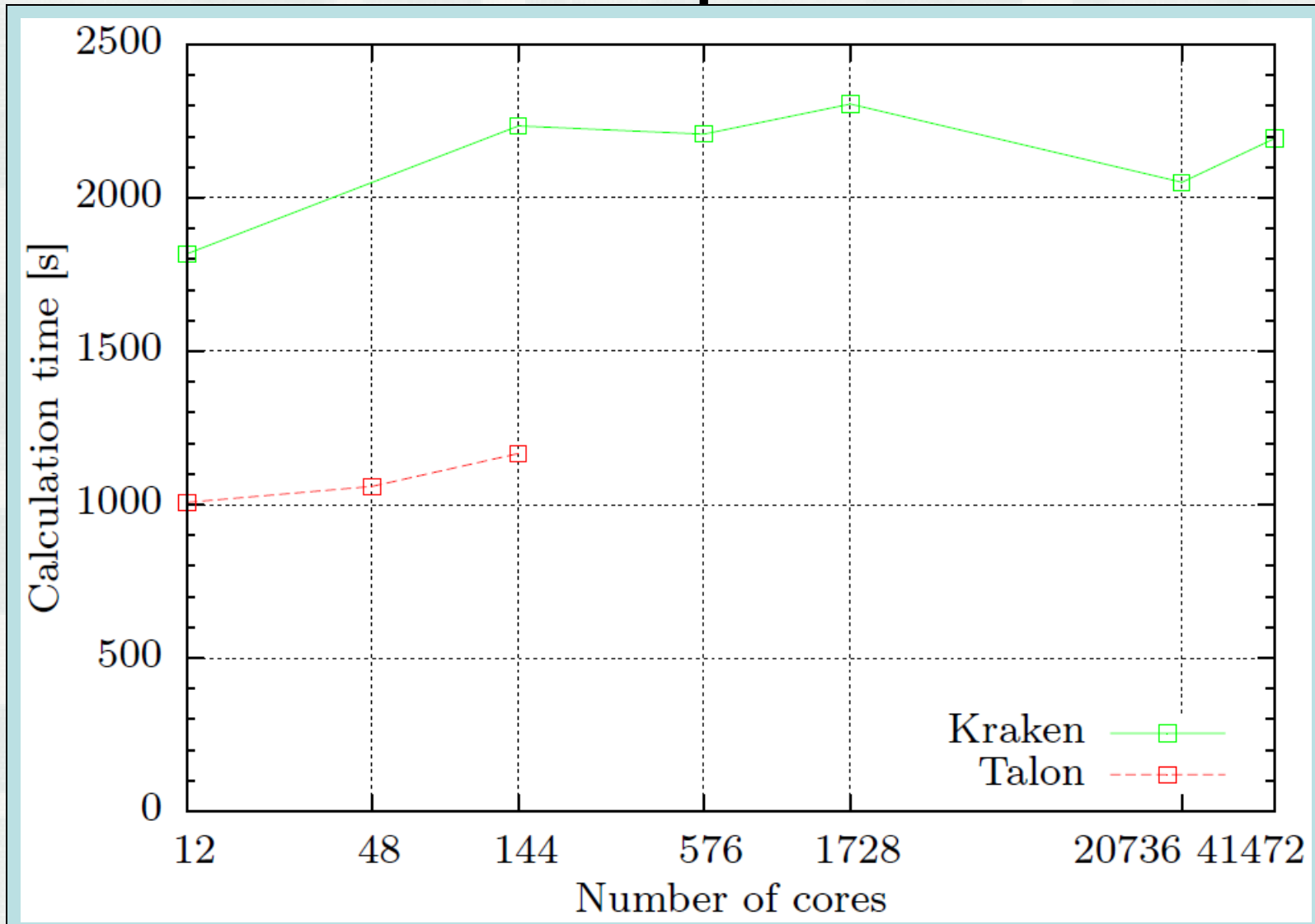
Scale up - constant domain per node



Duplication of the incubation domain onto 16 nodes



Scale up - results



Goal:
constant
calculation
time



Scale up - results

Demonstrated nearly perfect scale up

Largest domain:

- 41472 cores of Kraken
- over 165 billion grid nodes
- 11 millions of dendrites (only hundreds reported before)
- solute diffusion, melt convection, and heat transport
- dimensions 17.28 cm x 8.64 cm
- 587 time steps
- 40 minutes of simulation time

Computational resources

Talon, MSU HPC²:

- 3072 cores, 12 cores/node (user limit 192 cores / job)
- Intel Xeon X5660 @2.8GHz (Westmere) processors
- 24 GByte/node memory
- Voltaire quad data-rate InfiniBand (40Gb/s)
- peak performance of over 34.4 TeraFLOPS

Kraken, NICS/ORNL:

- 112,896 cores, 12 cores/node (user limit cores / job)
- AMD Opteron (Istanbul) @2.6GHz (Istanbul) processors
- 16 GByte/node memory
- Cray SeaStar2+ router
- peak performance of 1.17 PetaFLOPS

XSEDE allocations

1) Simulations for 2D and 3D dendrite growth during alloy solidification:

- SDSC-GORDON 250 kSU
- NICS-KRAKEN 249 kSU
- TACC-LONESTAR 1 kSU
- ECSS

2) Large scale 3D modeling of microstructural evolution during alloy solidification

- SDSC-GORDON 500 kSU
- NICS-NAUTILUS 10 kSU

Progress on the parallelization of the 3D LBM/CA code

Already implemented

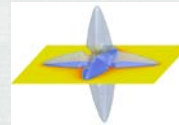
- Solute concentration and dendrite growth in parallel

Recently added

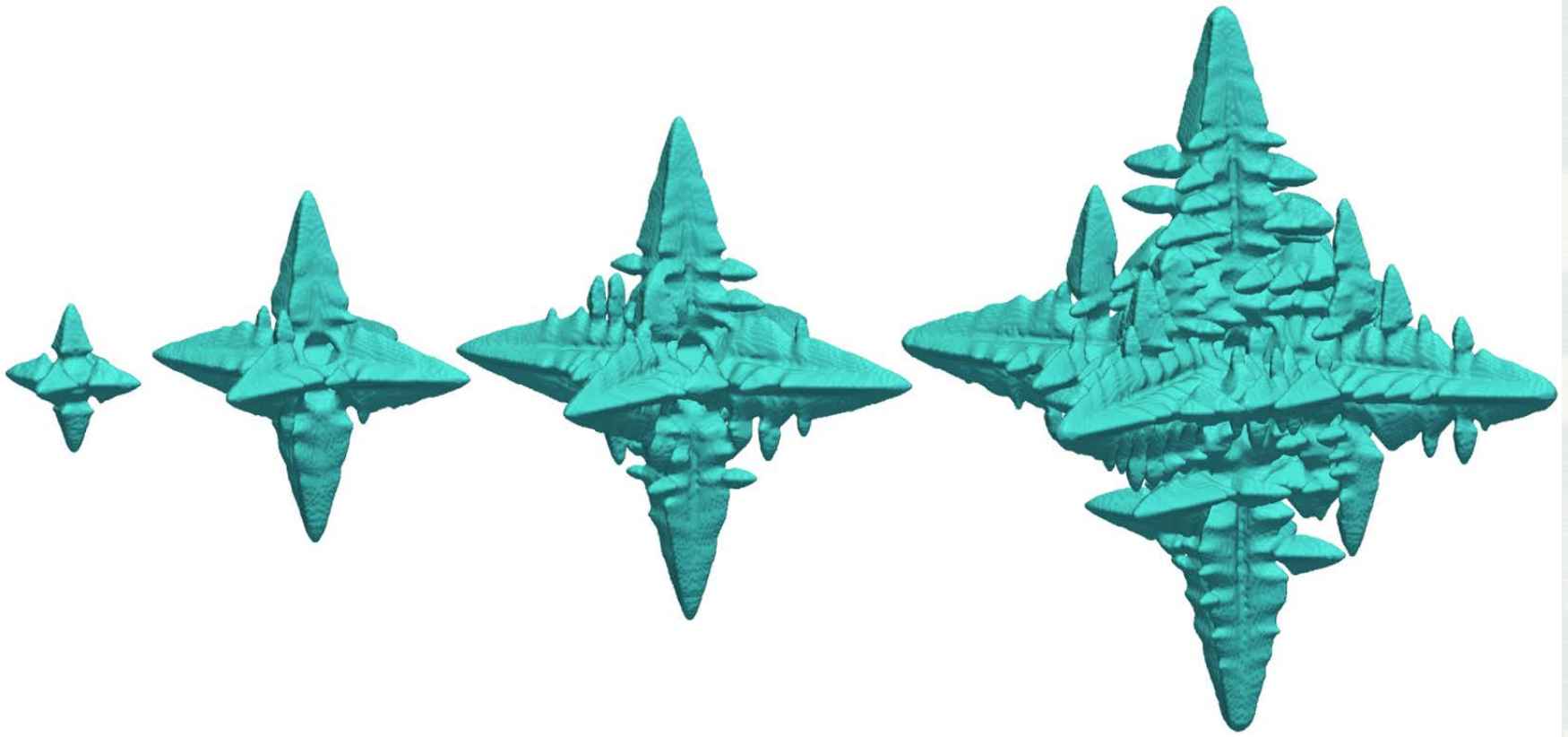
- convection (fluid velocity) in parallel
- output stride to reduce data for visualization
- velocity calculation on a coarser subgrid
- measure tip velocity and solute concentration profiles

Planned (as needed)

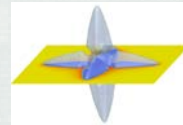
- parallelize full temperature field calculation in 3D



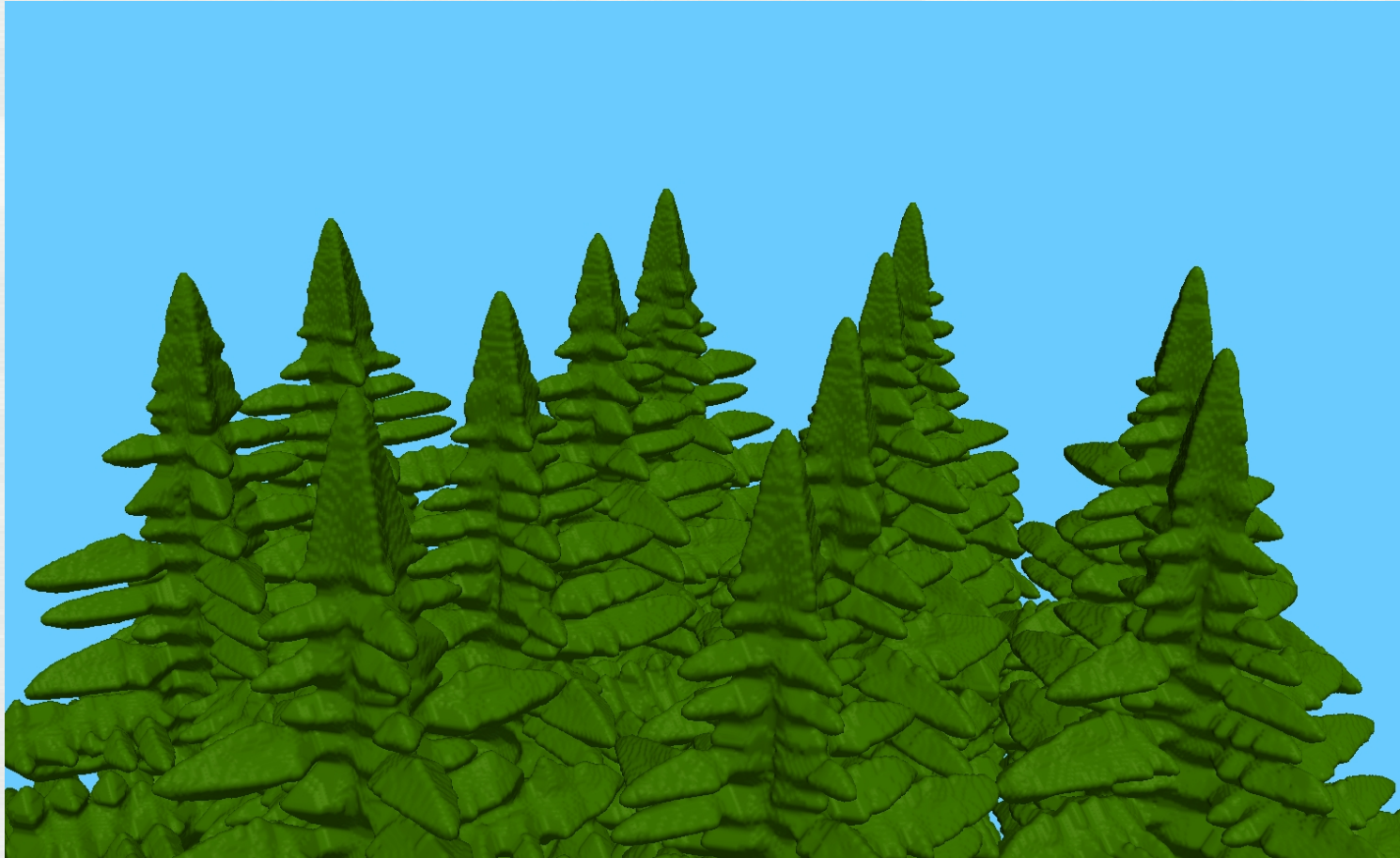
Growth of Al-Cu dendrites in a $120 \times 120 \times 120 \mu\text{m}^3$
with $4.5 \text{ }^\circ\text{C}$ undercooling.
From left to right, after 3, 7, 10, and 15 ms [1].



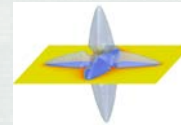
[1] M. Eshraghi, S.D. Felicelli, B. Jelinek, "Three-dimensional simulation of solutal dendrite growth using lattice Boltzmann and cellular automaton methods", Journal of Crystal Growth, Vol 354 (1), pp 129-134, 2012.



Columnar dendrites growing in an undercooled melt of Al-3wt%Cu. Domain size 180x180x144 (μm)³



By Mohsen Eshraghi



Publications

Published:

Journal articles:

- Eshraghi, M., Felicelli, S. D., Jelinek, B. (Jun 2012). Three Dimensional Simulation of Solutal Dendrite Growth Using Lattice Boltzmann and Cellular Automaton Methods. Journal of Crystal Growth Elsevier, 354(1), 129-134

In progress:

Journal articles:

- Jelinek, B., Eshraghi, M., Felicelli, S. D., Peters, J. F. Parallel lattice Boltzmann - cellular automaton model of two-dimensional dendritic growth – for Scripta Materialia (4 page limit)
- Jelinek, B., Eshraghi, M., Felicelli, S. D., Peters, J. F. Parallel lattice Boltzmann - cellular automaton model of two-dimensional dendritic growth – for Computer Physics Communications
- Eshraghi, M., Felicelli, S. D., Jelinek, B. A three-dimensional lattice Boltzmann-cellular automaton model for dendritic solidification under convection

Publications

Presentations, accompanied by articles in proceedings:

- Jelinek, B., Eshraghi, M., Felicelli, S. D., (March 2013). Large scale parallel lattice Boltzmann model of dendritic, 2013 TMS Annual Meeting & Exhibition
- Eshraghi, M., Jelinek, B., Felicelli, S. D., (March 2013). A three-dimensional lattice Boltzmann-cellular automaton model for dendritic solidification under convection, 2013 TMS Annual Meeting & Exhibition

Planned:

Journal articles:

- Jelinek, B., Eshraghi, M., Felicelli, S. D., Peters, J. F. Large scale parallel lattice Boltzmann - cellular automaton model of three-dimensional dendritic growth

Conclusions

Accomplishments

- Implemented tests of the strong and weak parallel scaling of LBM/CA model with dendrites at advanced growth stage
- Parallelized velocity in the 3D lattice Boltzmann / cellular automaton model for dendrite growth
- 3D velocity calculation on a coarser subgrid
- Measuring tip velocity and solute concentration profiles

Plans

- Implement LBM-DEM coupling (in progress)